

King Fahd University of Petroleum & Minerals Computer Engineering Dept

COE 342 – Data and Computer Communications

Term 032

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Lecture Contents

1. Fourier Analysis
 - a. Fourier Series Expansion
 - b. Fourier Transform
 - c. Ideal Low/band/high pass filters
2. Data/Signals
 - a. Audio/Voice
 - b. Video
 - c. Text
3. Transmission
 - a. Analog Transmission
 - b. Digital Transmission
4. Transmission Impairments
 - a. Attenuation and Attenuation Distortion
 - b. Delay Distortion
 - c. Noise
5. Channel Capacity
 - a. Nyquist Formula
 - b. Shannon Capacity Formula
 - c. Eb/No expression

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Analog and Digital Data Transmission

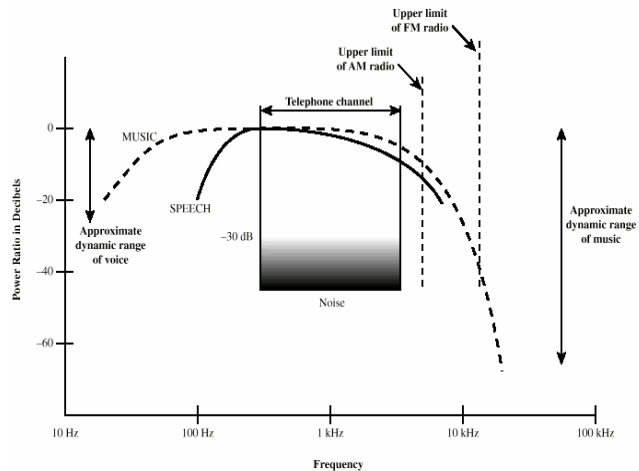
- **The terms:**
 - Analogue ~ continuous
 - Digital ~ discrete
- **They apply to:**
 - **A) Data:** the information to be delivered
 - **B) Signaling:** the electrical or electromagnetic wave that propagates carrying the data
 - **C) Transmission:** the mechanism of delivering the data by processing and propagation of signal

Examples of Data/Signaling: (1) AUDIO

- **Most familiar type of *analogue* data**
- **Human Ear (Receiver) bandwidth is ~10 Hz to ~20KHz**
 - You can not hear sounds with frequencies much higher than 20KHz or much lower than 10 Hz – Some other animals can do that (bats, whales, etc)
- **Human speech (Data) is mostly between 100 Hz and 7K Hz – with most of the energy concentrated in the lower part of this range**

Examples of Data/Signaling: (1) AUDIO – cont'd

- Typical Speech has a dynamic range of 25 dB – ratio of strongest speech signal to weakest speech signal is 25 dB or $10^{25/10} = 300$ (in linear scale)
- The **Telephone Channel** has a bandwidth of about 3.1KHz (from 300 Hz to 3400 Hz)
- Note that Music has a much wider bandwidth than speech (~ 10 Hz to ~ 20 KHz) – Hence a good audio system (CD player, high end speakers, etc) should be able to reproduce these signals
- Music has also a higher dynamic range too – What is the dynamic range of your audio system?



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Examples of Data/Signalling: (2) VIDEO

- Another common example of analog data
- The original scene (source) is scanned and its image recorded by the camera – RASTER image
- In the TV: a moving electron beam scan the screen producing the picture
 - For black and white: the amount of illumination produced (on a scale from black (lowest) to white (highest) at any point is proportional to the beam intensity
- Hence the original brightness is REPRODUCED on the screen
- Video Image \leftrightarrow Time varying analog signal

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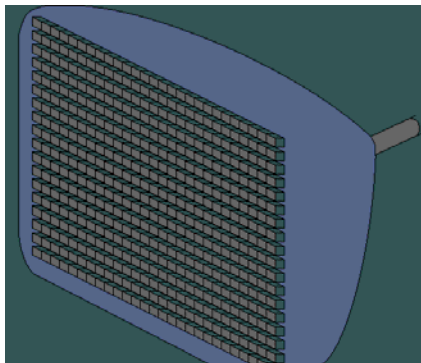
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Examples of Data/Signalling: (2) VIDEO – cont'd

- **Total of 525 horizontal lines (vertical resolution)**
 - 483 visible lines (241.5 even and 241.5 odd)
 - Subjective vertical resolution is $70 \times 483 = 338$ lines
 - Hence, horizontal resolution is $(4/3) \times 338 = 450$ pixels per line
 - 42 blanked during vertical retrace
- **Basic line duration = 63.5 μ sec:**
 - 52.5 μ sec scanning horizontally
 - 11 μ sec for horizontal retrace
- **High number of scans per second \rightarrow smoother picture but expensive hardware**
- **Low number of scans per second \rightarrow jittery picture (flickering)**
- **Interlacing: scan odd lines first at 30 scan per second and then scan even lines at 30 scans per second \rightarrow To the human eye, the screen is 60 refreshed 60 times per second, i.e. no flickering**

Examples of Data/Signalling: (2) VIDEO – cont'd

- **Scanning Process:**
 - Starts at the far left – near top
 - Scans 241.5 lines
 - Ends at middle of screen – lowest part
 - Beam is repositioned at the top again
 - Scanning starts again for the other 241.5 lines (interlaced with the previous lines)



Examples of Data/Signalling: (2) VIDEO – cont'd – Bandwidth Calculation

- 525 lines per scan at 30 scans per second → 15,750 lines/sec or 63.5 μsec per line
 - 52.5 μsec is the actual time spent in illuminating horizontal pixels
- There are 450 horizontal pixels per line
 - For maximum bandwidth calculation
 - Let illumination alternative from white to black and visa versa for consecutive pixels → 225 cycles / line
 - But line scanning is done in 52.5 μsec/line.
 - Hence, the beam does $(225/52.5 \mu\text{sec}) = 4.2 \times 10^6$ cycles per second
 - For minimum bandwidth
 - Let all pixels has same illumination level (no change in picture) → DC component – $f_{\text{min}} = 0 \text{ Hz}$
- Adding audio and color information does not increase bandwidth
- Hence NTSC video signal bandwidth is about 4 MHz

Example:

- **Problem 3.12:** For a video signal, what increase in a) horizontal b) vertical resolution is possible if a bandwidth of 5 MHz is used?

Example:

- **Solution:**

For increase in horizontal resolution - keeping same vertical resolution (483 lines); each horizontal lines occupies 52.5 μsec , therefore new horizontal resolution H is given by

$$5 \text{ MHz} = (H/2) / 52.5 \mu\text{sec} \rightarrow H = 525 \text{ lines}$$

For increase in vertical resolution – keeping same horizontal resolution of H = 450 lines, hence the new time for each horizontal line T is

$$5\text{MHz} = (450/2) / T \rightarrow T = 45 \mu\text{sec}$$

The horizontal retrace still takes 11 μsec , therefore total time for horizontal line is 56 μsec .

$$(1/30 \text{ sec/scan}) / V \text{ lines/scan} = 56 \mu\text{sec/line} \rightarrow V = 595 \text{ lines/scan}$$

Examples of Data/Signalling: (3) TEXT

- **Digital Data (pre-defined set of symbols)**
 - Same as Morse Code
- **IRA (or ASCII in the US) define 128 character using 7-bit words**
- **When transmitted or stored 1B or 8-bit words are used**
 - A parity bit is added as a simple error detection technique
- **The signal representing this data:**
 - One DC level for binary one
 - Another DC level for binary zero
- **Bandwidth representing this signal:**
 - Maximum bandwidth is required when bits alternate between 0 and 1 \rightarrow This results in a periodic square waveform (see Figure 3.15 in text)
 - Theoretical BW is infinite, but most of the energy is located for $f \leq$ fundamental frequency
 - Minimum frequency is zero (DC) – when all bits are equal

Transmission

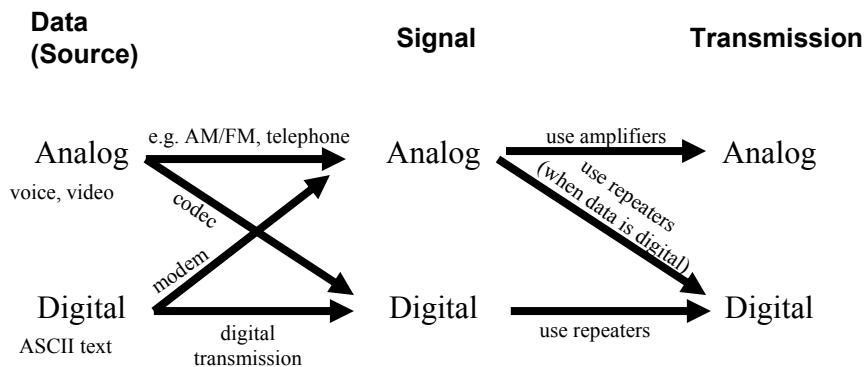
- **Analog Transmission:**
 - Analog signal is propagated through amplifiers to compensate for attenuation and to achieve longer distance
 - **Amplifiers:**
 - Boost signal and noise equally
 - May distort original signal
 - Can not be used indefinitely
- **Digital Transmission:**
 - To overcome the higher attenuation, repeaters are used at appropriately spaced points
 - **Repeaters:**
 - Recover original digital data
 - Transmit new signal
 - Can be used indefinitely

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Transmission (2)



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Transmission (3)

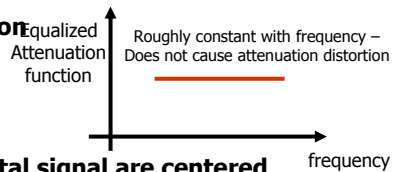
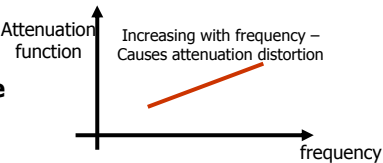
- **Digital Transmission is the prevailing technology:**
 - **Digital Technology:** Capitalize on advances in digital circuitry
 - **Data Integrity:** With the use of repeaters, the effects of noise and other signal impairments are not cumulative
 - **Capacity Utilization:** It is easier to multiplex several digital signals (using TDM) on one high capacity link as opposed to multiplexing analog sources using FDM
 - **Security and Privacy:** Use of encryption
 - **Integration:** Provides a uniform vehicle to transport both analog and digital data

Transmission Impairments

- **Impairments can degrade the quality of an analog signal or cause a bit (symbol) error for a digital signal**
- **Types of Impairments:**
 - **Attenuation and Attenuation Distortion**
 - **Delay Distortion**
 - **Noise**

Attenuation and Attenuation Distortion

- A received signal must have sufficient strength for proper detection at receiver
- For error-free communication signal strength relative to noise must be high
- **Attenuation is an increasing function of frequency:**
 - Different components of signal are subject to different attenuation → Distortion in time domain
- **Solution: Equalize transmission**
 - Results in almost equal attenuation (gain) for all frequencies of interest
- **Attenuation Distortion is less of a problem for digital signals:**
 - Frequencies of interest for a digital signal are centered around the fundamental frequency, f
 - Attenuation function has to be flat around f only



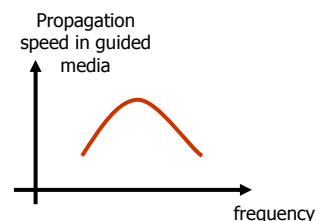
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Delay Distortion

- For guided media – different frequency components have different propagation speeds
- For unguided media – multipath (signal being received through more than one path) causes delay distortion
- Received signal is distorted due to varying delays experienced at its constituent frequencies
- **Critical for digital data: Causes Intersymbol interference – a major limitation on maximum bit rate over a transmission channel**
- **Solution: Equalization**



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Noise

- Major limiting factor in communication system performance
- Types of Noise:
 - Thermal Noise
 - Intermodulation Noise
 - Crosstalk
 - Impulse Noise

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Thermal Noise

- Due to agitation of electrons
- Function of temperature (energy of electrons)
- Can not be eliminated → limits communication system performance
- Noise power density (noise power found in 1 Hz), N_0 , is given by

$$N_0 = kT \quad (\text{Watts/Hz})$$

Where k is Boltzman constant = 1.3803×10^{-23} J/degree Kelvin

T is the temperature in degrees Kelvin

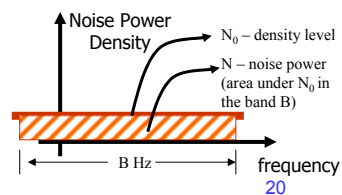
- Hence, the thermal noise power in a bandwidth B Hz is given by

$$N = N_0 \times B = kT \times B \quad (\text{Watts})$$

- In decibels:

$$NdB = 10\log k + 10\log T + 10\log B$$

$$= -228.6 \text{ dBW} + 10\log T + 10\log B$$



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Examples:

- **Problem 3.14:** Given an amplifier with effective noise temperature of 10,000 degrees Kelvin, and a 10-MHz bandwidth, what thermal noise we expect at the output

Examples:

- **Solution:**

$$N = kT \times B$$

$$k = 1.38 \times 10^{-23} \text{ J/Kelvin}, T = 10,000 \text{ degrees Kelvin}, B = 10 \times 10^6 \text{ Hz},$$

$$N = 1.38 \times 10^{-12} \text{ Watts}$$

$$N_{\text{dBW}} = 10 \log N = -118.6 \text{ dBW}$$

In dBmW, one can write

$$N_{\text{dBmW}} = 10 \log N \times 1000 = -88.6 \text{ dBmW or simply, } N_{\text{dBmW}} = N_{\text{dBW}} + 30$$

Intermodulation Noise

- **Lineal System:** $H_L(S) = A_1xS + A_0$

E.g. Consider the input S_1+S_2 , where $S_1 = \cos(2\pi*f_1*t)$ and $S_2 = \cos(2\pi*f_2*t)$. The system output is

$$H_L(S_1+S_2) = A_1x \cos(2\pi*f_1*t) + A_1x \cos(2\pi*f_2*t) + A_0$$

Note the output signal has frequencies f_1 and f_2 **ONLY**.

- **NonLinear System:** $H_{NL}(S) = A_2xS^2 + A_1xS + A_0$

The output (for the same input) is

$$H_{NL}(S_1+S_2) = A_2x [\cos(2\pi*f_1*t) + \cos(2\pi*f_2*t)]^2 + A_1x [\cos(2\pi*f_1*t) + \cos(2\pi*f_2*t)] + A_0$$

Note that $[\cos(2\pi*f_1*t)]^2 = 1/2 + 1/2 \cos(2\pi*2f_1*t)$, and

$$\cos(2\pi*f_1*t) \cos(2\pi*f_2*t) = 1/2 \cos(2\pi*(f_1+f_2)*t) + 1/2 \cos(2\pi*(f_1-f_2)*t)$$

Output signal contain terms with multiples of (f_1+f_2) and (f_1-f_2)

- **Intermodulation noise:** *undesired* signals at the frequency that is multiples of sum or difference of the two original input frequencies
- **Caused by nonlinearity**

Crosstalk/Impulse Noise

- **Crosstalk:**
 - Unwanted coupling between signal paths
 - E.g. electrical coupling between near by twisted pair wires
 - Coax cables are more immune to cross talk compared to twisted pairs
- **Impulse Noise:**
 - Unlike previous types of noise, this one is:
 - Noncontinuous – irregular pulses or spikes for short duration and high amplitude
 - **Causes:**
 - Lightening
 - Faults or flaws in communication systems
 - **Major concern for digital data**

Effect of Noise on Digital Signal

- **Figure 3.16**

Channel Capacity

- **Terminology:**
 - **Data Rate (R):** bit rate of channel – bits per second
 - **Bandwidth (B):** bandwidth of transmitted signal – Hz
 - **Noise power (N):** average noise power level for communication channel – Watt/Hz for density or Watt for noise power
 - **Error rate (Pe):** rate at which an erroneous detection is made (detecting 0 for 1 and 1 for 0)

Nyquist Bandwidth

- For a noise-free channel → data rate is limited by B of channel
- A bandwidth of B Hz is enough to support 2B bits per second
- Example: B = 3100 Hz (telephone channel) → C = 6200 b/s
- What if we use multilevel signaling :

$$C = 2B \log_2 M$$

Where M is the number of discrete levels used

- Example: for M = 8, same telephone channel can support C = 2X3100X log₂8 = 18.6 kb/s
- M = 2 – receiver recognizes two signal levels 1s and 0s
- M > 2 – receiver recognizes discrete levels other than 1 and 0
- In general, multilevel signaling requires more sophisticated receiver structure and perhaps more power for the same bandwidth

Shannon Capacity Formula

- Capacity in the presence of noise

$$C = B \log_2(1 + \text{SNR})$$

where SNR is the ratio of signal power to noise power – a measure of the signal quality

- Example: f_{min} = 3 MHz, f_{max} = 4 MHz, SNR = 24 dB, C = ?

$$B = 4 - 3 = 1 \text{ MHz}$$

$$\text{SNR} = 10^{24/10} = 251 \text{ (on the linear scale)}$$

$$C = 1 \times 10^6 \log_2(1 + 251) \sim 8 \times 10^6 \text{ b/s or } 8 \text{ M b/s}$$

One can also calculate the required signaling levels, M, using Nyquist formula: $C = 2B \log_2(M) \rightarrow M = 2^{C/(2B)} = 16$

- Note the C (calculated by Shannon formula) is the theoretical limit of the channel for the given B and SNR

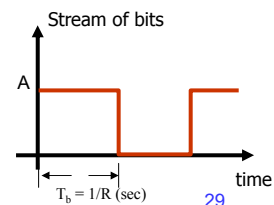
E_b/N_0 Expression

- An alternative representation of SNR
- Consider the bit stream shown in figure – for bit of rate R, then each bit duration is equal to $T_b = 1/R$ seconds
- Energy of signal for the bit duration is equal to $A^2 \times T_b$, where its power is equal to bit energy / T_b or A^2 .
- Noise power is equal to $N_0 \times B$ (refer to thermal noise section)
- Hence, SNR is given by signal power / noise power or

$$SNR = \frac{\text{signal power}}{N_0 B} = \frac{E_b}{N_0} \times \frac{R}{B}$$

- One can also write

$$\left(\frac{E_b}{N_0} \right)_{dB} = \text{Signal Power}(dBW) - 10 \log R - 10 \log k - 10 \log T$$



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Examples:

- **Problem 3.19:** Given a channel with the intended capacity of 20 Mb/s, the bandwidth of the channel is 3 MHz. What signal to noise ratio is required to achieve this capacity?

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Examples:

- **Solution:**

Shannon Limit: $C = B \log_2(1 + \text{SNR})$, $C = 20 \times 10^6$ b/s, $B = 3 \times 10^6$ Hz

$\log_2(1 + \text{SNR}) = 6.67 \rightarrow \text{SNR} = 101 = 20$ dB

Examples:

- **Problem 3.21:** If the received signal level for a particular digital system is -151 dBW and the receiver system effective noise temperature is 1500 degrees Kelvin. What is the E_b/N_0 for a link transmitting 2400 b/s

Examples:

- **Solution:**

$$E_b/N_0 = (\text{signal power} / \text{noise power}) * (B/R)$$

$$\text{Noise power} = kT \times B$$

$$\text{Hence } E_b/N_0 = (\text{signal power}) / (kT R)$$

$$= 10^{-151/10} / (1.38 \times 10^{-23} \times 1500 \times 2400)$$

$$= 15.99$$

$$= 12 \text{ dB}$$

$$\text{Or } (E_b/N_0)_{\text{dB}} = \text{Signalpower}_{\text{dBW}} - 10\log k - 10\log T - 10\log R$$

$$= -151 - 10\log(1.38 \times 10^{-23}) - 10\log 1500 - 10\log 2400$$

$$= 12 \text{ dB}$$