

COMPUTER ENGINEERING DEPARTMENT

COE-342 – Data and Computer Communication

March 6th, 2004 – Assignment

(Due Date: March 20th, 2004)

- 1) Textbook Problems: 2.7, 3.4, and 3.6
- 2) The Fourier series expansion for any periodic function $s(t)$ with period T , is given by

$$s(t) = \frac{A_0}{2} + \sum_{n=1,2}^{\infty} A_n \cos(2\pi nft) + B_n \sin(2\pi nft)$$

where the fundamental frequency $f = 1/T$. Using the following three trigonometric laws:

$$\frac{1}{T} \int_0^T \cos(2\pi nft) \cos(2\pi mft) dt = \begin{cases} 0 & n \neq m \\ 1/2 & n = m \end{cases}$$

$$\frac{1}{T} \int_0^T \sin(2\pi nft) \sin(2\pi mft) dt = \begin{cases} 0 & n \neq m \\ 1/2 & n = m \end{cases}$$

$$\frac{1}{T} \int_0^T \cos(2\pi nft) \sin(2\pi mft) dt = 0 \quad \forall n, m$$

SHOW that the coefficients A_0 , A_n , and B_n are given by the following expressions:

$$A_0 = \frac{2}{T} \int_{-T/2}^{T/2} s(t) dt$$

$$A_n = \frac{2}{T} \int_{-T/2}^{T/2} s(t) \cos(2\pi nft) dt \quad n = 1, 2, \dots$$

$$B_n = \frac{2}{T} \int_{-T/2}^{T/2} s(t) \sin(2\pi nft) dt \quad n = 1, 2, \dots$$

- 3) Consider the Sawtooth wave function listed in table B.1 of Appendix B (page 793) of the text book.
 - a. Write a mathematical expression for $s(t)$
 - b. Compute the Fourier series expansion for $s(t)$
 - c. Write an expression for $s_e(3)$
 - d. Plot the original $s(t)$ and $s_e(3)$ on the same graph. Is $s_e(3)$ a good approximation for $s(t)$?
 - e. Find the total power of $s(t)$
 - f. Find n^* such that $s_e(n = n^*)$ contains 95% of the total power in the original signal
 - g. Write an expression for the power spectral density function for $s(t)$
 - h. Plot the power spectral density function for $s(t)$