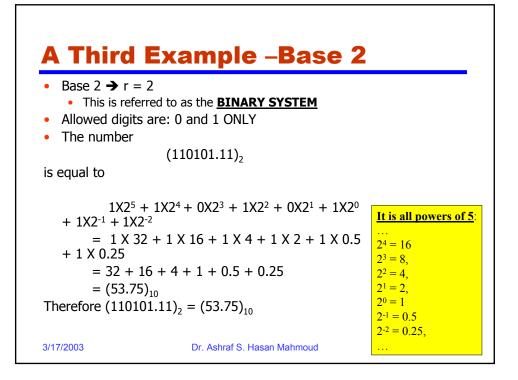
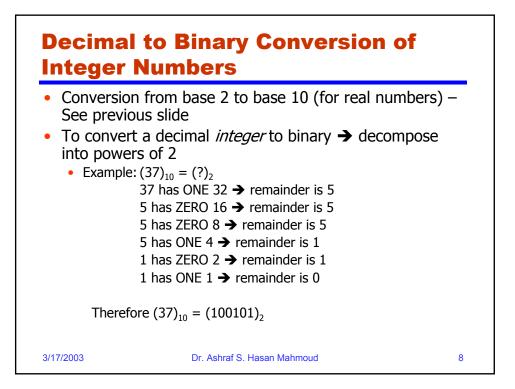
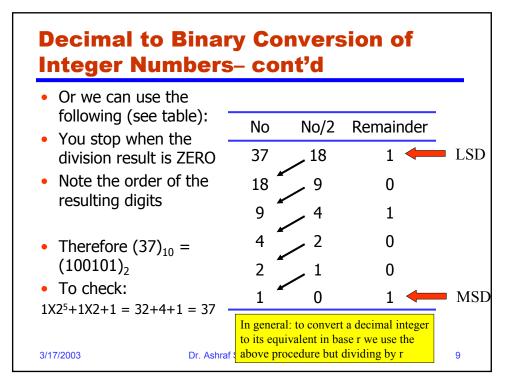


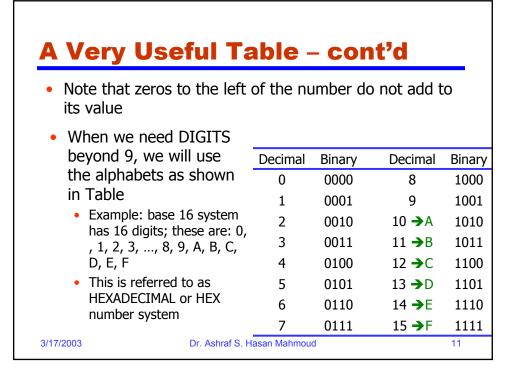
• Base 5 → r	= 5	
20.000 2 1	s are: 0, 1, 2, 3, and 4 ONLY	
	(312.4) ₅	
is equal to		
3X5 ²	+ 1X5 ¹ + 2X5 ⁰ + 4X5 ⁻¹	
= 3 X 2	5 + 1 X 5 + 2 X 1 + 4 X 0.2	It is all powers of
= 75 +	5 + 2 + 0.8	$5^3 = 125$,
= (82.8) ₁₀	$5^2 = 25$,
Therefore (31	$(2.4)_5 = (82.8)_{10}$	$5^{1} = 5,$ $5^{0} = 1$ $5^{-1} = 0.2$ $5^{-2} = 0.04,$
3/17/2003	Dr. Ashraf S. Hasan Mahmoud	







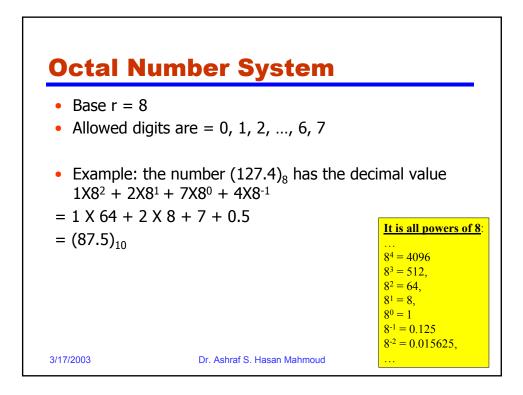
A Very Useful Ta	able			
 To represent decimal num numbers) we need FOUR t In general to represent 			•	
N numbers, we need	Decimal	Binary	Decimal	Binary
$\left\lceil \log_2 N \right\rceil$ bits	0	0000	8	1000
Note how	1	0001	9	1001
 B₀ flipped or COMPLEMENTED 	2	0010	10	1010
at every increment	3	0011	11	1011
• B ₁ flipped or COMPLEMENTED	4	0100	12	1100
 every 2 steps B₂ flipped or COMPLEMENTED 	5	0101	13	1101
every 4 steps	6	0110	14	1110
• B ₃ flipped or COMPLEMENTED	7	0111	15	1111
3/17/2003 every 8 steps Dr. Ashraf S. H	lasan Mahmou	d		10

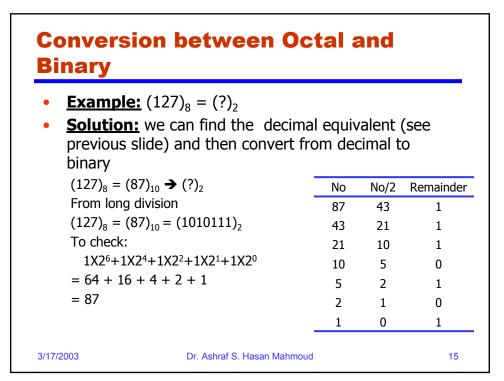


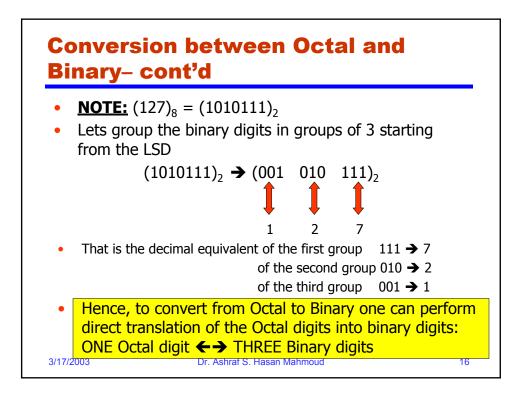
Decimal to Binary Fractions	Conve	ersion	of	
• Example: $(0.234375)_{10} = (?)_2$	No	NoX2	Integer	Part
Solution: We use the following procedure	0.234375	0.46875	0	-
• <u>Note:</u>	0.46875	0.9375	0	MSI
 The binary digits are the integer part of the multiplication process 	0.9375	1.875	1	
The process stops when the	0.875	1.75	1	
number is 0There are situations where the	0.75	1.5	1	
process DOES NOT end – See next slide	0.5 🖌	1.0	1	-
• Therefore $(0.234375)_{10} = (0.001111)_2$	0			LSD
• To check: $(0.001111)_2 = 1X2^{-2}$ +1X2 ⁻³ +1X2 ⁻⁴ +1X2 ⁻⁵ +1X2 ⁻⁵ 3/17/2 D X2 ⁻⁶ = $(0.234375)_{10}$ Dr. Ashraf S.	In general: to to its equivale above procedu	ent in base r w	ve use the	n 12

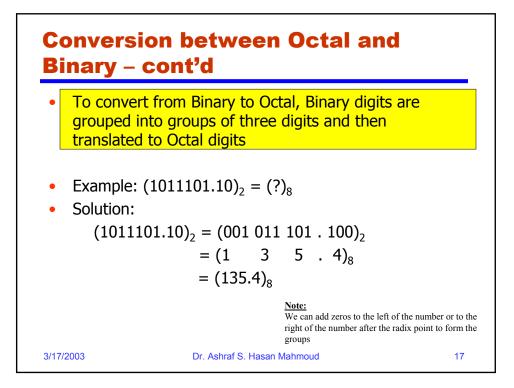
Decimal to	Binary	Conversion of
Fractions –	cont'd	

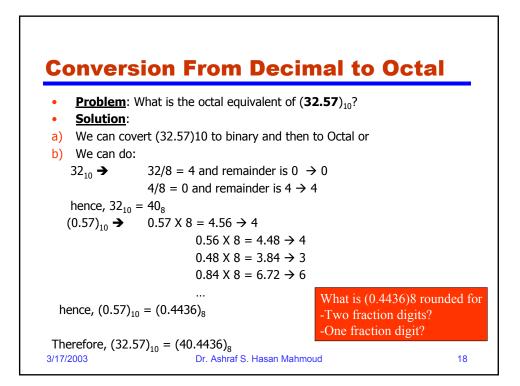
• Example: (0.513)		No	NoX2	Integer Part
 Solution: As in pr 	evious silde	0.513	1.026	1
		0.026	0.052	0
		0.052	0.104	0
Therefore $(0.513)_{10}$	= (0.100000110)	0.104	0.208	0
) ₂		0.208	0.416	0
)2		0.416	0.832	0
If we chose to roun	round to 1 significant	0.832	1.664	1
	iu to i significant	0.664	1.328	1
figure \rightarrow (0.1) ₂		0.328	0.656	0
Or to 7 significant f $(0.1000001)_2$				
Etc.				
3/17/2003	Dr. Ashraf S. Hasan Mahmoud	ł		13

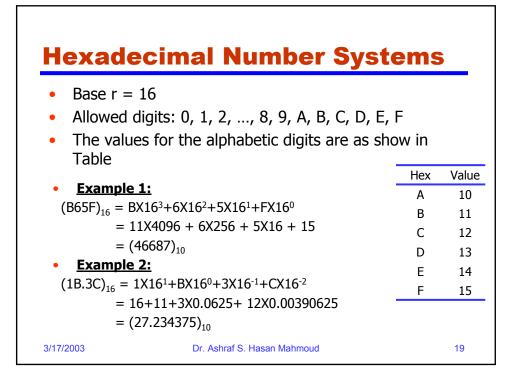


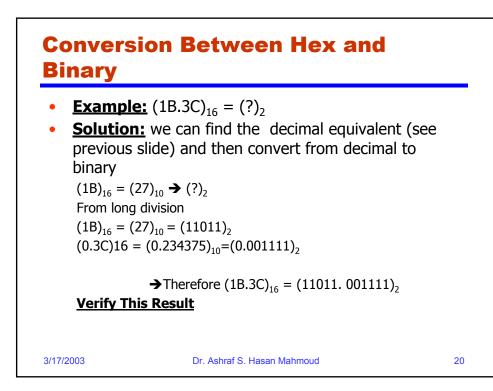


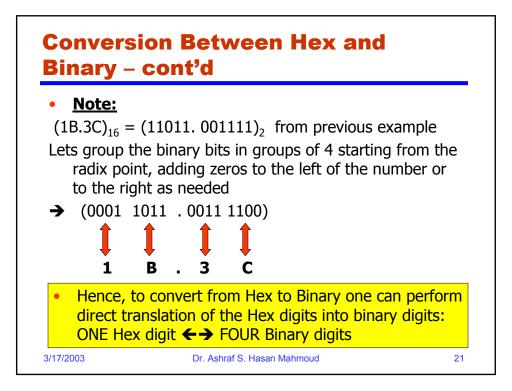


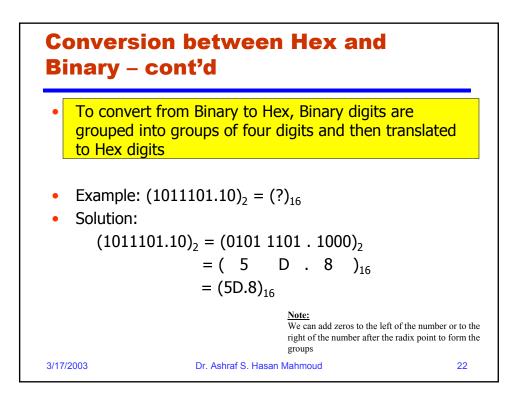




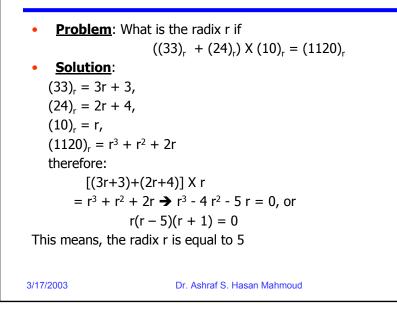




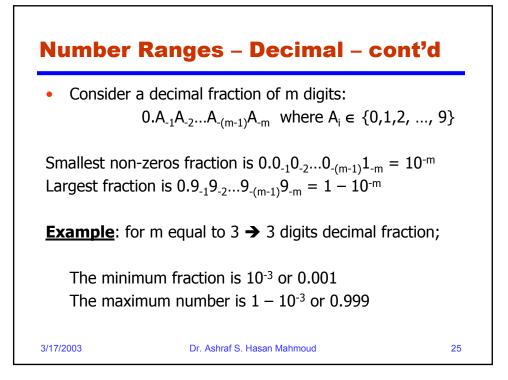


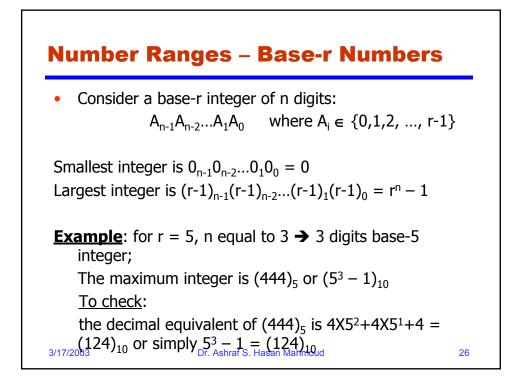


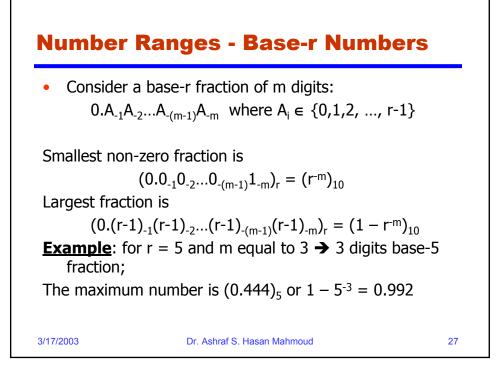
Sample Exam Problem

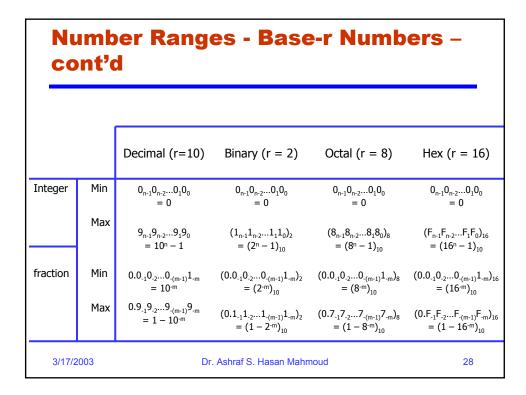


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Exercises

- What is 8^4 equal to in octal? (8^4)₁₀ = (10000)₈
- What is 2⁵ equal to in binary?
 (2⁵) = (100000)₂
- What is 16⁴ 1 equal to in Hex?
- What is $2^3 2^{-2}$ equal to in Binary?
- What is $16^5 16^4$ equal to in Hex?
- What is 3⁴ 3⁻² equal to in base-3?
- What is 2⁴ 2⁻² equal to in base-3?

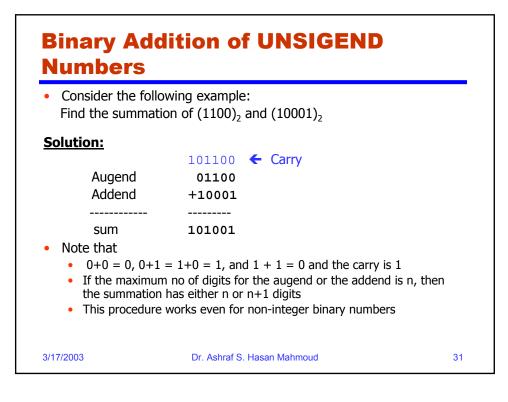
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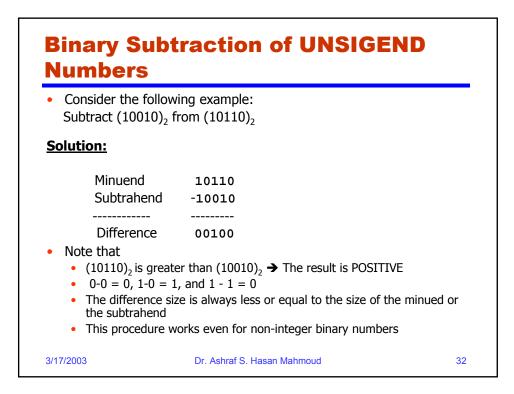
Dr. Ashraf S. Hasan Mahmoud

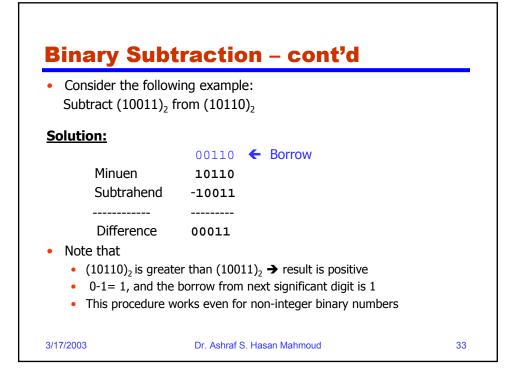
Addition and Subtraction of (Unsigned) Numbers

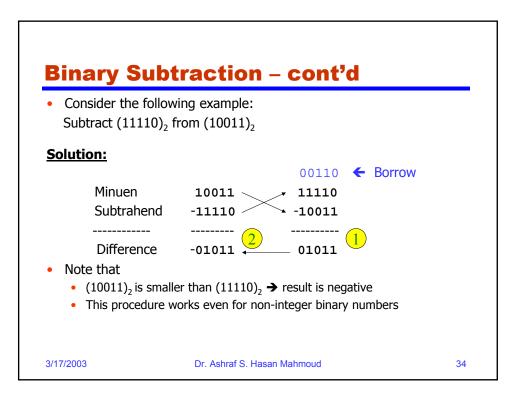
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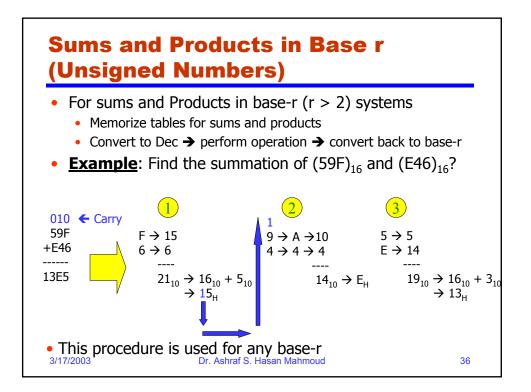


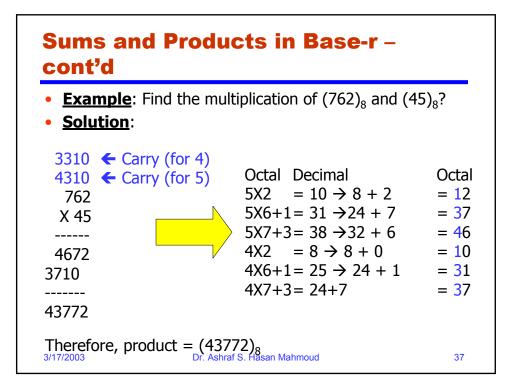


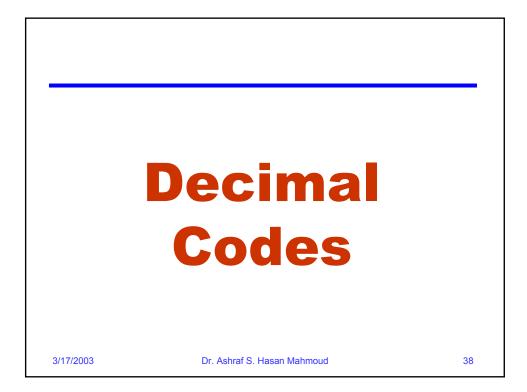


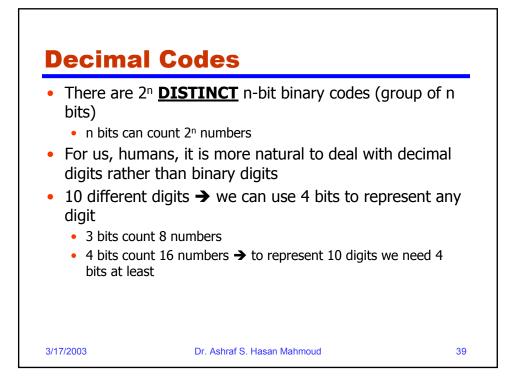


 Consider the follow Multiply (1011)₂ by 		
Solution:		
Multiplicand	1011	
Multiplier	X 101	
	1011	
	0000	
	1011	
Product	110111	

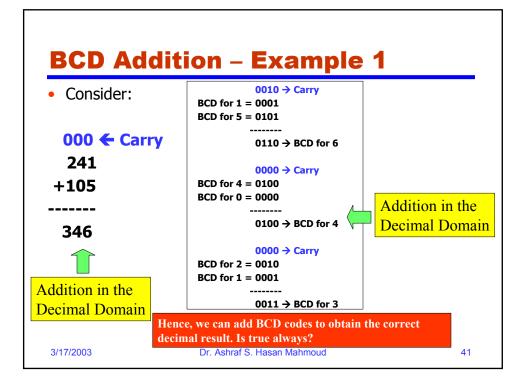


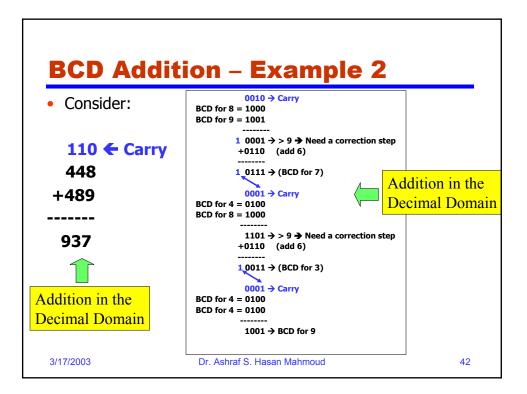


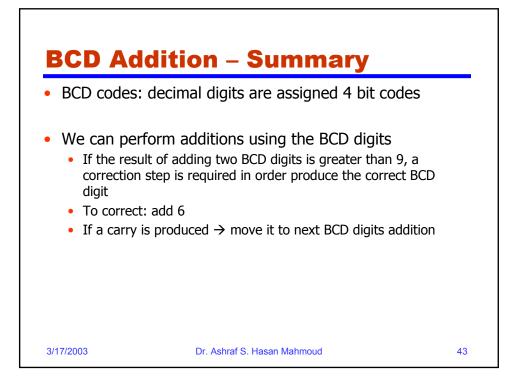


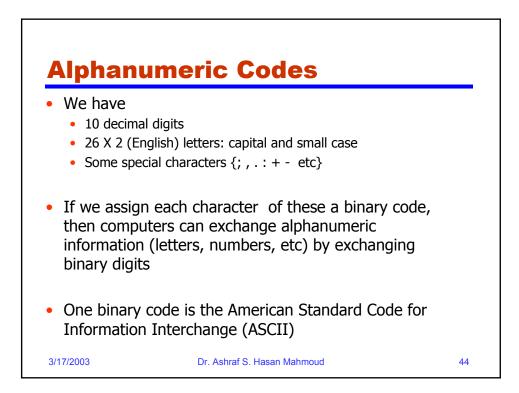


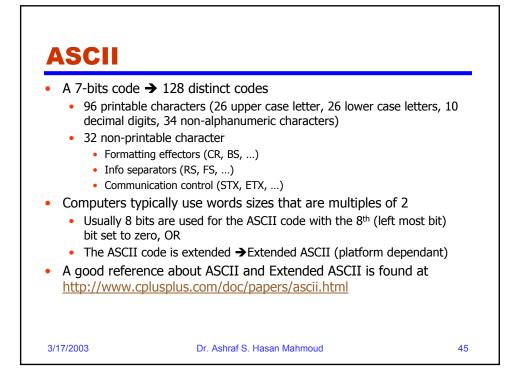
Binary Coded D	ecim	al (B	CD)	
 Let the decimal digits be coded as show in table 	Decimal Digit	Binary Code	Decimal Digit	Binary Code
• Then we can write	0	0000	5	0101
 Inen we can write numbers as 	1	0001	6	0110
	2 0010		7	0111
	3	0011	8	1000
	4	0100	9	1001
$(396)_{10} = (0011\ 1003)$ Since 3 $\rightarrow 0011$, 9 = 1001,		but the	igh we are using the ey are not equal in the natical sense; this is	e
Note that $(396)_{10} = (110001100)_{Dr. Ashraf Strain St$, ≠ (0011 Hasan Mahmo	1001 0110) _{BCD}	40











ASCII – cont'd

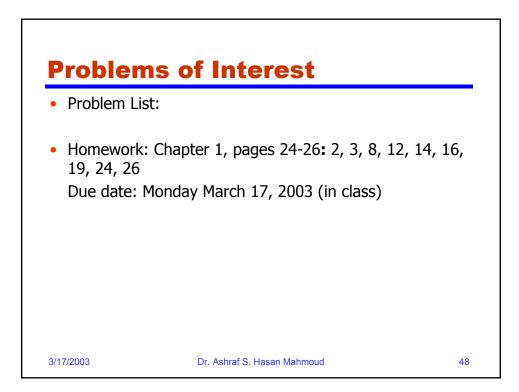
- A 7-bits code → 128 distinct codes
- The American Standard Code for Information Interchange (ASCII) uses seven binary digits to represent 128 characters as shown in the table.

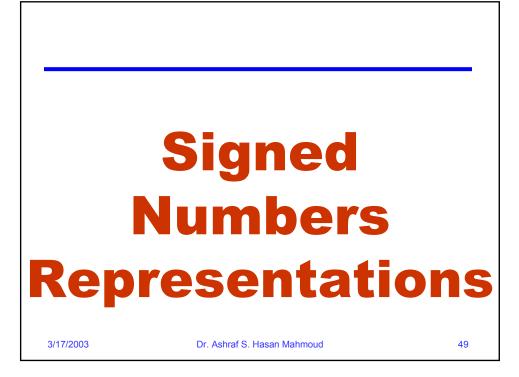
00	NUL	01	SOH	02	STX	03	ETX	04	EOT	05	ENQ	06	ACK	07	BEL
08	BS	09	HT	0A	NL	0B	VT	0C	NP	0D	CR	0E	SO	0F	SI
10	DLE	11	DC1	12	DC2	13	DC3	14	DC4	15	NAK	16	SYN	17	ETB
18	CAN	19	EM	1A	SUB	1B	ESC	1C	FS	1D	GS	1E	RS	1F	US
20	SP	21	!	22	"	23	#	24	\$	25	%	26	&	27	
28	(29)	2A	*	2в	+	2C	,	2D	-	2E	.	2F	/
30	0	31	1	32	2	33	3	34	4	35	5	36	6	37	7
38	8	39	9	3A	:	3B	;	3C	<	3D	=	3E	>	3F	?
40	@	41	A	42	в	43	С	44	D	45	Е	46	F	47	G
48	H	49	I	4A	J	4B	K	4C	L	4D	М	4E	Ν	4F	0
50	P	51	Q	52	R	53	S	54	Т	55	U	56	V	57	W
58	X	59	Y	5A	Z	5B	[5C	$\langle \rangle$	5D]	5E	^	5F	_
60	`	61	a	62	b	63	С	64	d	65	е	66	f	67	g
68	h	69	i	бA	j	6B	k	6C	1	6D	m	6E	n	бF	0
70	рļ	71	q	72	r	73	s	74	t	75	u	76	v	77	w
78	x	79	У	7A	z	7B	{	7C		7D	}	7E	~	7F	DEL
3/1	7/200	3					Dr. A	Ashra	fS.H	asan	Mahn	noud			

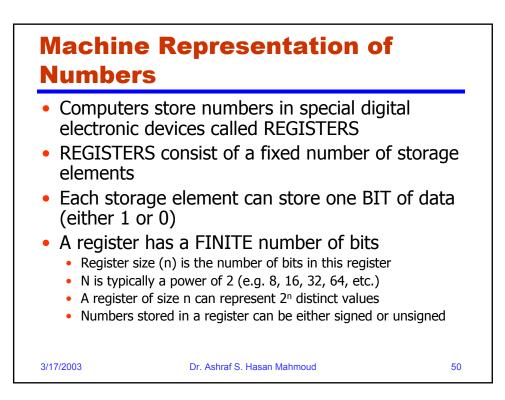
Unicode

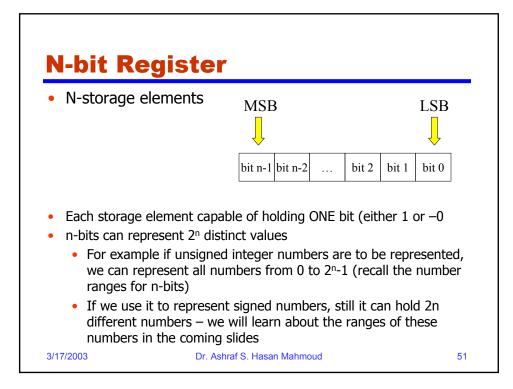
Unicode describes a 16-bit standard code for representing symbols and ideographs for the world's languages.

	Co	ntrol	ASCII						Cor	ntrol	Latin 1					
	000	001	002	003	004	005	006	007	008	009	00A	00B	00C	00D	00E	00F
0	CTRL	CTRL	SPACE	0	@	Р	•	р	CTRL	CTRL	NB SP	0	À	Ð	à	D
1	CTRL	CTRL	1	1	А	Q	а	q	CTRL	CTRL	1	±	Á	Ñ	á	ñ
2	CTRL	CTRL		2	В	R	Ь	г	CTRL	CTRL	¢	2	Â	Ò	â	ò
3	CTRL	CTRL	#	3	С	S	с	s	CTRL	CTRL	£	3	Ă	Ó	ã	ó
4	CTRL	CTRL	S S	4	D	Т	d	t	CTRL	CTRL	п	1	Ä	Ô	ä	ô
5	CTRL	CTRL	%	5	Е	U	е	u	CTRL	CTRL	¥¥	μ	Å	Õ	å	õ
6	CTRL	CTRL	&	6	F	V	f	v	CTRL	CTRL	- E	¶	Æ	Ö	æ	ö
7	CTRL	CTRL	,	7	G	W	g	w	CTRL	CTRL	§		Ç	\times	ç	÷
8	CTRL	CTRL	(8	Н	Х	h	х	CTRL	CTRL			È	Ø	è	ø
9	CTRL	CTRL)	9	Ι	Υ	i	у	CTRL	CTRL	C	i	É	Ù	é	ù
А	CTRL	CTRL	*	:	J	Ζ	j	z	CTRL	CTRL	а	0	Ê	Ú	ê	ú
В	CTRL	CTRL	+	;	Κ]	k	{	CTRL	CTRL	«	>>	Ë	Û	ë	û
С	CTRL	CTRL	,	<	L	\	1	1	CTRL	CTRL	~	$\frac{1}{4}^{1/4}$	Ì	Ü	ì	ü
D	CTRL	CTRL	-	=	Μ	1	m	}	CTRL	CTRL	-	1/2	Í	Ý	í	ý
Е	CTRL	CTRL		>	Ν	^	n	~	CTRL	CTRL	®	3 3/4	Î	þ	î	þ
F	CTRL	CTRL	/	?	0	_	0	CTRL	CTRL	CTRL	-	ż	Ĭ	ß	ï	ÿ
We		., The Unicode hing Company,		orldwid			-	Version 1.0, V		-	nicode, Inc.	Reprinte	d by pe	rmission	of Add	ison-

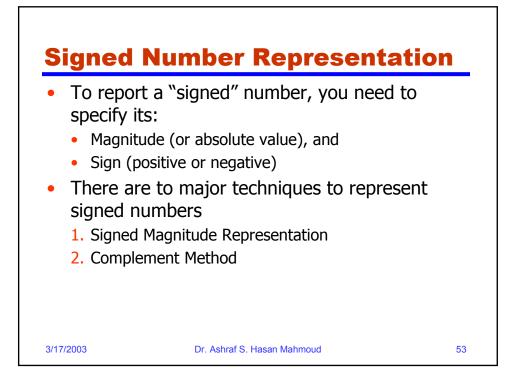


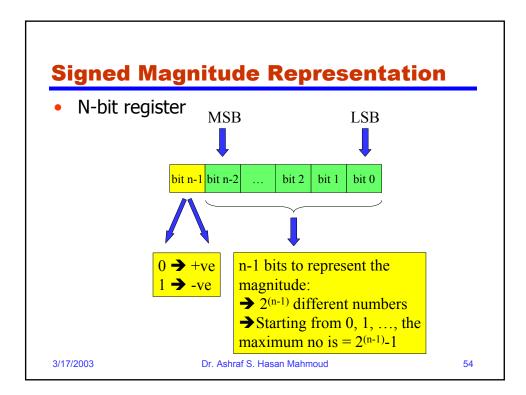


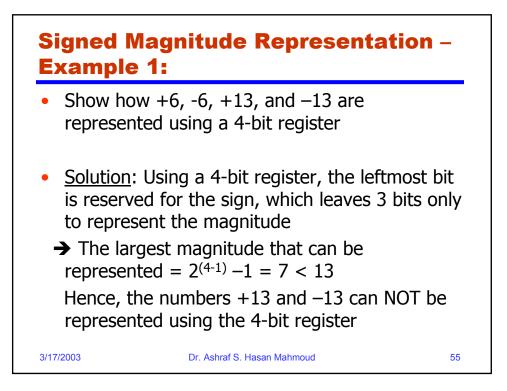


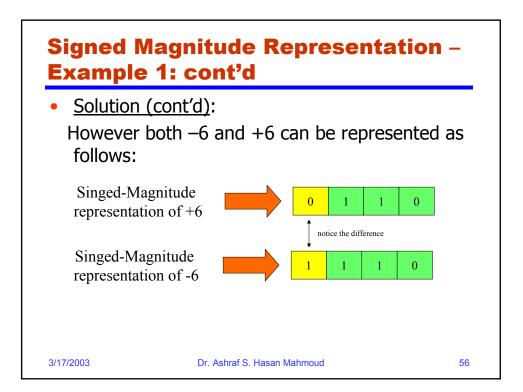


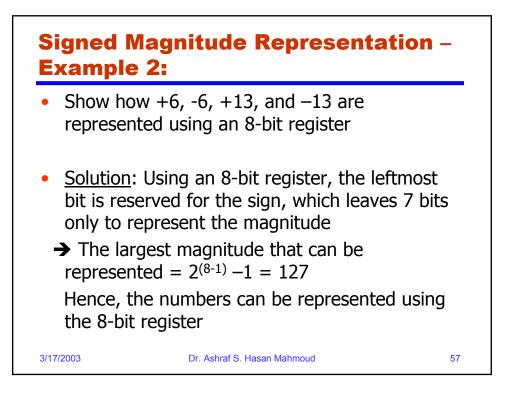
follows:	t register, $(13)_{10}$ or $(D)_{H}$ is represented as
101101131	1 1 0 1
Using an 8-t	bit register, $(13)_{10}$ or $(D)_{H}$ is represented as
	0 0 0 0 1 1 0 1
	EROS are used to pad the binary ion of 13 in the 8-bit register

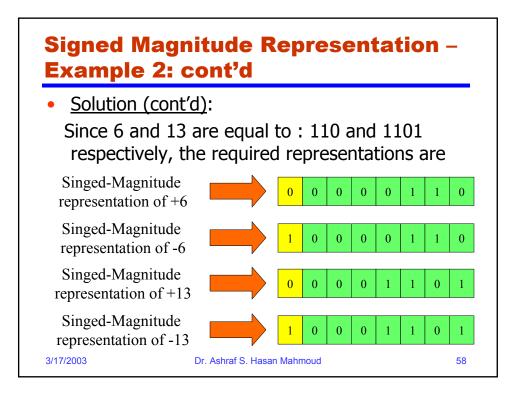


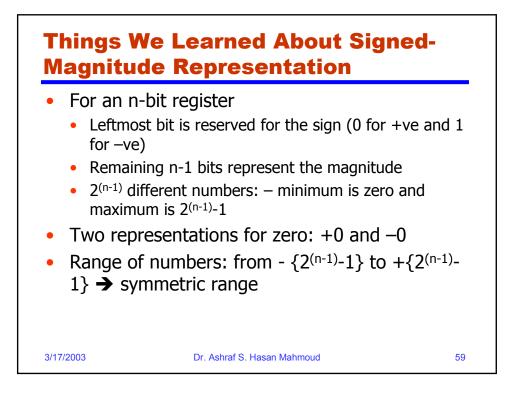


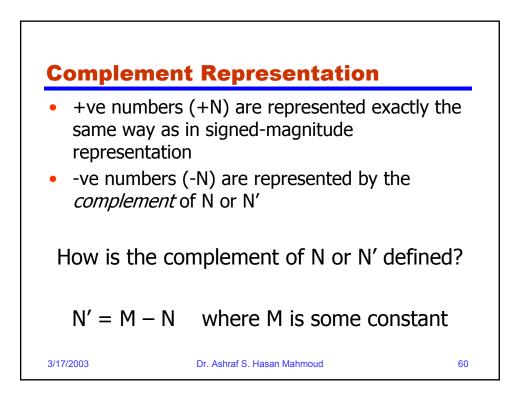




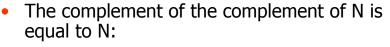








Properties of the Complement Representation



<u>Proof</u>: (N')' = M - (M - N) = -(-N) = N

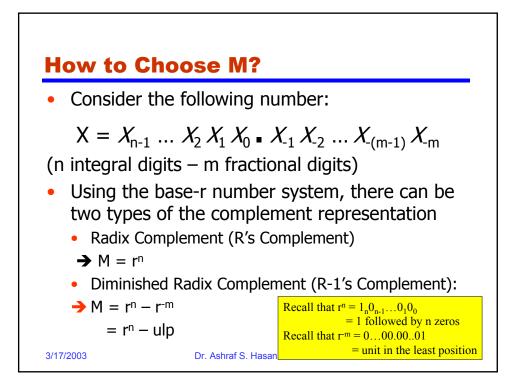
Same as with -ve numbers definition!

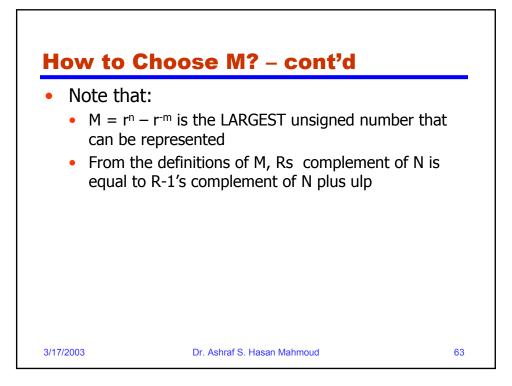
- The complement method representation of signed numbers simplifies implementation of arithmetic operations like subtraction:
- e.g.: A B can be replaced by A + (-B) or A + B' using the complement method

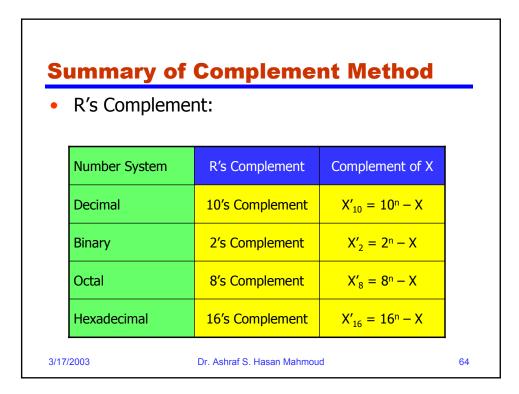
Therefore to perform subtraction using computers we complement and add the subtrahend

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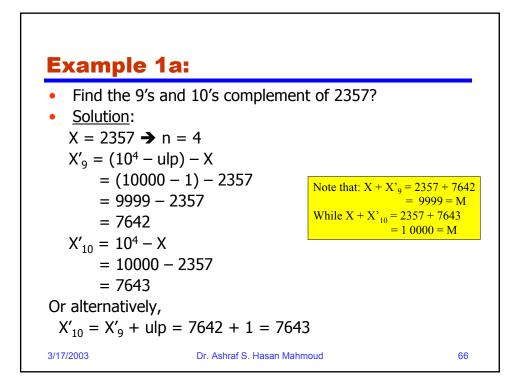
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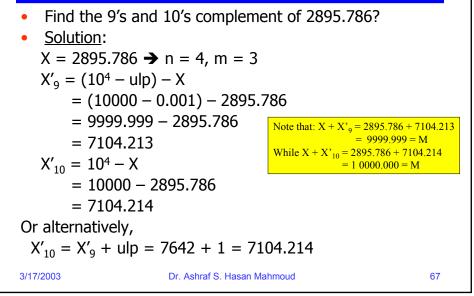


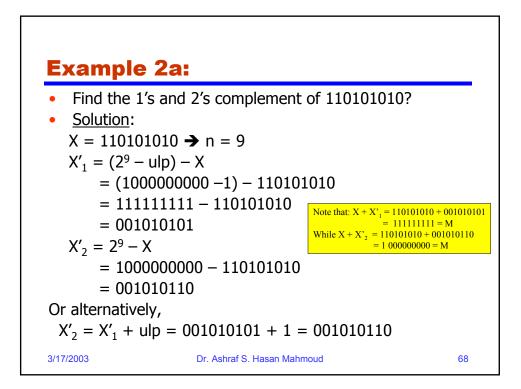


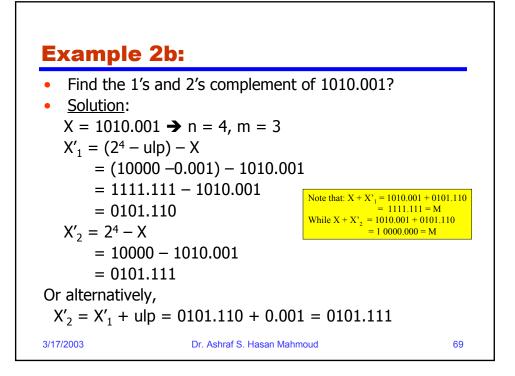
	Summary of Complement Method – cont'd R-1's Complement:							
•	It is comple	ment.						
	Number System	R-1's Complement	Complement of X					
	Decimal	9's Complement	$X'_9 = (10^n - 10^{-m}) - X$ = 9999.9999 - X					
	Binary	1's Complement	$X'_1 = (2^{n}-2^{-m}) - X$ = 1111.1111 - X					
	Octal	7's Complement	X' ₇ = (8 ⁿ - 8 ^{-m})- X = 7777 . 7777 - X					
	Hexadecimal	15's Complement	$X'_{15} = (16^n - 16^{-m}) - X$ = FFFF.FFFF - X					
3/17	3/17/2003 Dr. Ashraf S. Hasan Mahmoud 65							

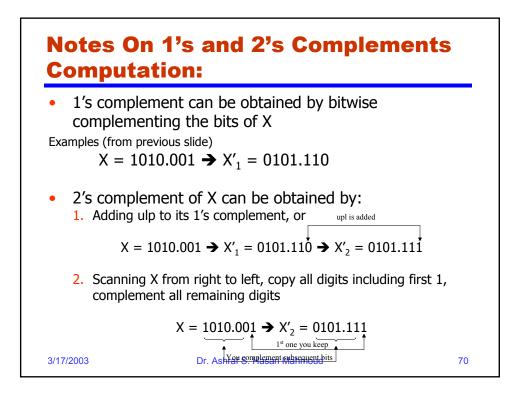






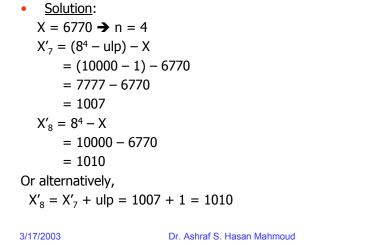






Example 3a:

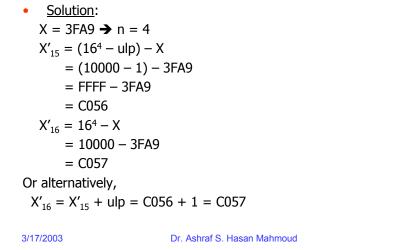
• Find the 7's and the 8's complement of the following octal number 6770?



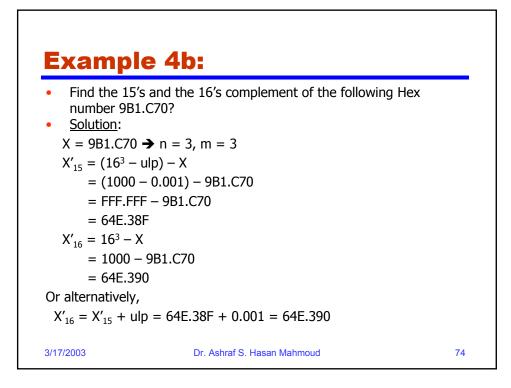
Example 3b: Find the 7's and the 8's complement of the following octal number 541.736? Solution: X = 541.736 → n = 3, m = 3 $X'_7 = (8^3 - ulp) - X$ =(10000 - 0.001) - 541.736= 777.777 - 541.736 = 236.041 $X'_{8} = 8^{3} - X$ = 10000 - 541.736= 236.042Or alternatively, $X'_8 = X'_7 + ulp = 236.041 + 0.001 = 236.042$ 3/17/2003 Dr. Ashraf S. Hasan Mahmoud 72

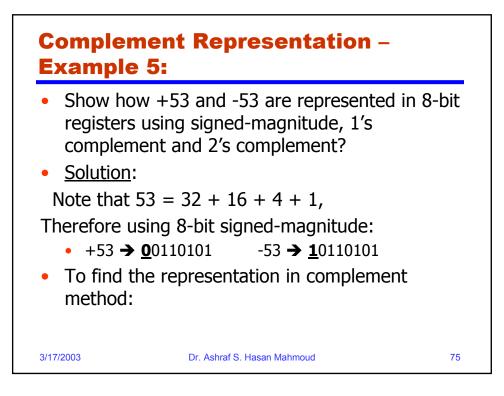


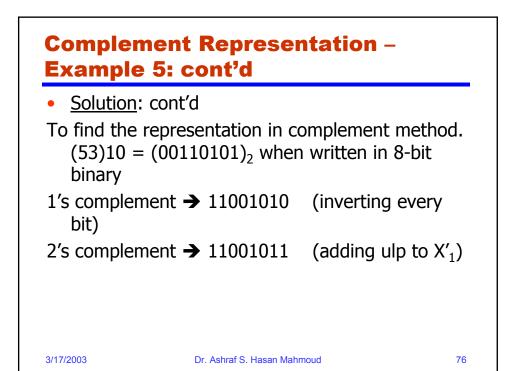
• Find the 15's and the 16's complement of the following Hex number 3FA9?

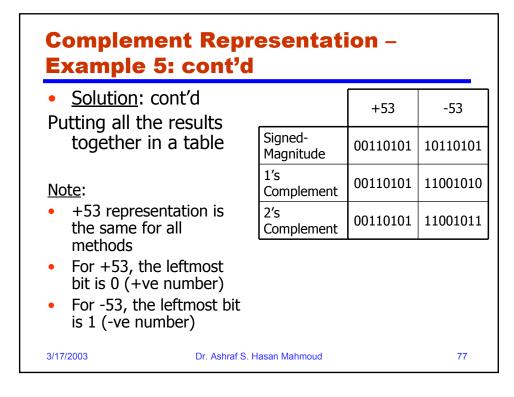


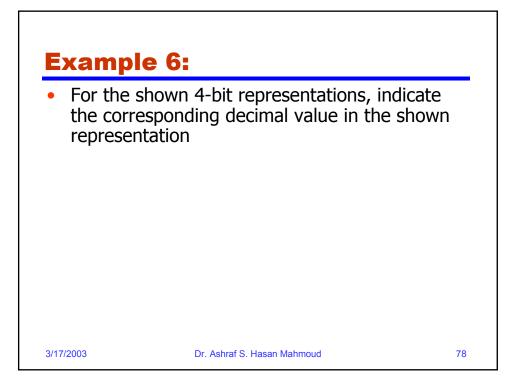
73





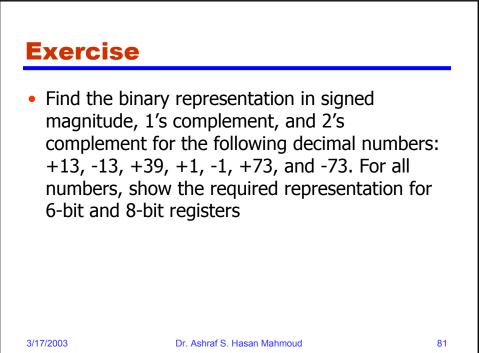






-		nt'd			
 Signed-Magnitude and 1's complement 		Unsigned	Signed- Magnitude	1's Complement	2's Compleme
are symmetrical representations with TWO representations	0000	0	0	0	0
	0001	1	1	1	1
for ZERO	0010	2	2	2	2
	0011	3	3	3	3
 Range from signed- magnitude and 1's 	0100	4	4	4	4
complement is from -	0101	5	5	5	5
7 to +7	0110	6	6	6	6
 2's complement 	0111	7	7	7	7
representation is not	1000	8	-0	-7	-8
symmetrical • Range for 2's complement is from - 8 to +7 – with one representation for ZERO	1001	9	-1	-6	-7
	1010	10	-2	-5	-6
	1011	11	-3	-4	-5
	1100	12	-4	-3	-4
	1101	13	-5	-2	-3
ZERO	1110	14	-6	-1	-2
	1111	15	-7	-0	-1

Summa	Summary				
	 The following table summarizes the properties and ranges for the studied signed number representations 				
		Signed- Magnitude	1's Complement	2's Complement	
Symme	etric	Y	Y	N	
No of Z	eros	2	2	1	
Largest		2 ⁽ⁿ⁻¹⁾ -1	2 ⁽ⁿ⁻¹⁾ -1	2 ⁽ⁿ⁻¹⁾ -1	
Smalles	st	-{2 ⁽ⁿ⁻¹⁾ -1}	-{2 ⁽ⁿ⁻¹⁾ -1}	-2 ⁽ⁿ⁻¹⁾	
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10's (Complei	men	t	
	= 1 and 2		X′ ₁₀ (n=2)	X' ₁₀ using+/- in decimal
		_	00	0
X' ₁₀ (n=1			01	1
	in decimal		02	2
0	0			
1	1		09	9
			10	10
2	2		11	11
3	3		12	12
4	4			
-			49	49
5	-5		50	-50
6	-4		51	-49
7	-3		52	-48
8	-2			
			98	-2
9	-1	Ashraf S H	99	-1

