

● **Queuing Models (1)**

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Recap

- Probability
- Traffic characterization

Today's lecture

- Queuing systems
- M/M/1
- Little's Formula
- examples

Queuing models

- Many phenomena in life can be thought of as queues
 - Cashier line in grocery store
 - Waiting for a teller in a bank
 - Bus stop
 - Getting a ticket in a theatre
 - Etc

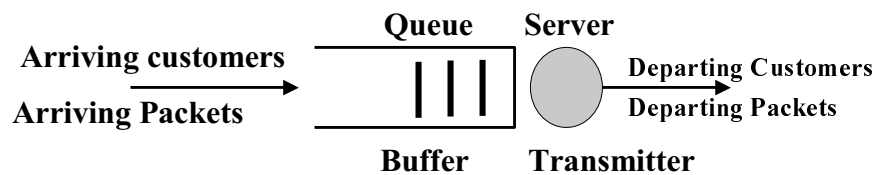
Queuing models

- In data networks, we can find queues in many spots:
 - From DLL to network
 - From network to DLL
 - From L3 to L4
 - Between switches/routers
 - etc

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Basic Queue Model



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Example

- A 56 kbps transmission line can serve 1000-bit packets as a rate of
 - 56 pkts/sec

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Little's Formula

- It is very general and can be applied to almost all types of queues and network of queues
 - The time spent by a customer, while waiting and being served, by the arrival rate of customers gives the number of customers in the Qing system (including the customer being currently serviced)

$$T = N$$

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Kendall Notation

- $X/Y/m/k$ where
 - X is a symbol representing the interarrival process:
 - M = Poisson (EXPO interarrival times)
 - D = Deterministic (Constant interarrival times)
 - Y is a symbol representing the service distribution
 - M = exponential
 - D = Deterministic
 - G = General
 - m is the number of servers
 - k is the buffer size (omitted when $k = \infty$)

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M/M/1 Queue

- Is the most basic and important queueing model
 - Poisson arrival with rate λ
 - Exponential service time with mean $1/\mu$ (μ is service rate)
 - Single server
 - Infinite buffer

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M/M/1 Results

- normalized offered load or utilization (ρ)
 $\rho = \lambda / \mu = 1 - p_0$ = prob system is non-empty (busy)
- Avg number of customers in the Q=
 $E(n) = \rho / (1 - \rho)$
- Average waiting time $E(t) = E(n) / \mu$

Example

A switching node receives packets at a rate of 2000 pkt/sec with exponential interarrival times and sends them on a link with capacity of 1.5 Mb/s. The packet lengths are exponentially distributed with mean 515 bit/pkt. Find the average packet waiting time in this node?

Example

Solution:

Packet service time is exponential
with mean

$$1/\mu = \text{pkt_len}/\text{capacity} = 0.33\text{ms}/\text{pkt}$$

$$\text{Packet service rate} = \mu = 3000\text{pkt/s}$$

$$\text{From } M/M/1; \rho = \lambda/\mu = .67 \text{ (unitless)}$$

$$E(n) = 2 \text{ pkts/sec}$$

$$E(t) = 1 \text{ ms !}$$