

Name: KEY

Id#

COE 202, Term 131
Digital Logic Design

Quiz# 4

Date: Tuesday, Nov. 25

Q1. Design a circuit that accepts two 2-bit unsigned numbers $A = A_1A_0$ and $B = B_1B_0$. The circuit produces $A - B$ when $A > B$, and produces $A + B$ otherwise. Find the following:

(a) The number of outputs produced by the circuit.

$A - B$ result is at most 2 bits, $A + B$ result is at most 3 bits \Rightarrow # outputs = 3

(b) The truth table of the circuit.

A_1	A_0	B_1	B_0	O_2	O_1	O_0
0	0	0	0	0	0	0
0	0	0	1	0	0	1
0	0	1	0	0	1	0
0	0	1	1	0	1	1
0	1	0	0	0	0	1
0	1	0	1	0	1	0
0	1	1	0	0	1	1
0	1	1	1	1	0	0
1	0	0	0	0	1	0
1	0	0	1	0	0	1
1	0	1	0	1	0	0
1	0	1	1	1	0	1
1	1	0	0	0	1	1
1	1	0	1	0	1	0
1	1	1	0	0	0	1
1	1	1	1	1	1	0

(c) The minimal product-of-sums expression for each output.

B ₁ B ₀ \ A ₁ A ₀	00	01	11	10
00	0	0	0	0
01	0	0	1	0
11	0	0	1	0
10	0	0	1	1

$$O_2 = (A_1 + A_0)(\overline{A_0} + B_0)B_1$$

B ₁ B ₀ \ A ₁ A ₀	00	01	11	10
00	0	0	1	1
01	0	1	0	1
11	1	1	1	0
10	1	0	0	0

$$O_1 = (A_1 + A_0 + B_1)(A_1 + B_1 + B_0)(\overline{A_1} + A_0 + \overline{B_0})(\overline{A_1} + \overline{B_1} + B_0)(A_1 + \overline{A_0} + \overline{B_1} + \overline{B_0})$$

B ₁ B ₀ \ A ₁ A ₀	00	01	11	10
00	0	1	1	0
01	1	0	0	1
11	1	0	0	1
10	0	1	1	0

$$O_0 = (A_0 + B_0)(\overline{A_0} + \overline{B_0})$$

Q2. Convert the AND/OR/NOT logic diagram shown below to a NAND logic diagram:

