

Name: KEY

Id#

COE 202, Term 112
Digital Logic Design

Quiz# 4

Date: Saturday, April 7

Q1.

i. Determine the decimal value of the 8-bit binary number (11010100) when interpreted as:

An unsigned number	A signed-magnitude number	A signed-1's complement number	A signed-2's complement number
212	-84	-43	-44

ii. Represent the decimal value (- 40) in binary using a total of 8 bits in the following notations:

A signed-magnitude number	A signed-1's complement number	A signed-2's complement number
10101000	11010111	11011000

iii. Perform the following signed-2's complement arithmetic operations in binary using 5 bits. All numbers given are represented in the signed-2's complement notation. Indicate clearly the carry values from the last two stages. For each of the three operations, check and indicate whether overflow occurred or not.

	a. $\begin{array}{r} 01001 \\ +10111 \\ \hline 00000 \end{array}$	b. $\begin{array}{r} 01000 \\ -10010 \\ \hline 01000 \\ +01110 \\ \hline 10110 \end{array}$	c. $\begin{array}{r} 11010 \\ -01101 \\ \hline 11010 \\ +10011 \\ \hline 01101 \end{array}$
Overflow Occurred? (Yes/No)	No	Yes	Yes

Q2. Design a combinational circuit that receives a 4-bit unsigned number $I = I_3I_2I_1I_0$ as input and generates the remainder of dividing this number by 3.

I3	I2	I1	I0	R1	R0
0	0	0	0	0	0
0	0	0	1	0	1
0	0	1	0	1	0
0	0	1	1	0	0
0	1	0	0	0	1
0	1	0	1	1	0
0	1	1	0	0	0
0	1	1	1	0	1
1	0	0	0	1	0
1	0	0	1	0	0
1	0	1	0	0	1
1	0	1	1	1	0
1	1	0	0	0	0
1	1	0	1	0	1
1	1	1	0	1	0
1	1	1	1	0	0

Using K-map, we will get the equations for R1 and R0 as follows:

$$\begin{aligned}
 R1 &= I_3'I_2'I_1I_0' + I_3'I_2I_1'I_0 + I_3I_2I_1I_0' + I_3I_2'I_1'I_0' + I_3I_2'I_1I_0 \\
 &= I_1I_0' (I_3 \oplus I_2)' + I_3I_2'(I_1 \oplus I_0)' + I_3'I_2I_1'I_0
 \end{aligned}$$

$$\begin{aligned}
 R0 &= I_3'I_2'I_1'I_0 + I_3'I_2I_1'I_0' + I_3'I_2I_1I_0 + I_3I_2I_1'I_0 + I_3I_2'I_1I_0' \\
 &= I_1'I_0 (I_3 \oplus I_2)' + I_3'I_2(I_1 \oplus I_0)' + I_3I_2'I_1I_0'
 \end{aligned}$$