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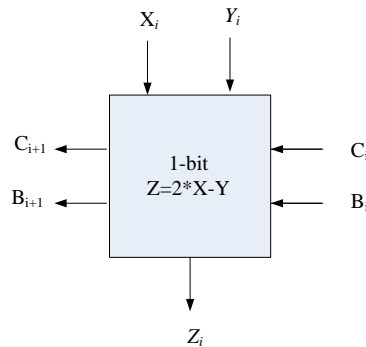
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COE 202, Term 141  
Digital Logic Design

Quiz# 4

Date: Thursday, Nov. 20

**Q1** It is required to design a circuit to compute the equation  $Z=2*X-Y$ , where  $X$  and  $Y$  are two  $n$ -bit unsigned numbers. The circuit can be designed in a modular manner where it is designed for one bit and replicated  $n$  times. A 1-bit circuit block diagram is given below:

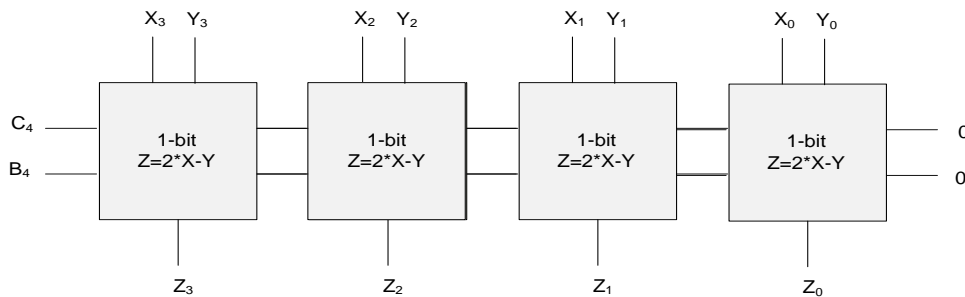


The meaning of the values of  $B_i$  and  $C_i$  is given in the table below:

$B_i$	$C_i$	Meaning
0	0	There is no carry or borrow
0	1	There is a carry of 1
1	0	There is a borrow of 1
1	1	This condition does not occur

For example, if  $X_i=1$  and  $Y_i=1$ , then we should have  $Z_i=1$ ,  $B_{i+1}=0$  and  $C_{i+1}=0$ . If  $X_i=0$  and  $Y_i=1$ , then we should have  $Z_i=1$ ,  $B_{i+1}=1$  and  $C_{i+1}=0$ .

The figure below shows how a 4-bit  $Z=2*X-Y$  circuit is implemented using 4 copies of the basic 1-bit cell.



Derive the truth table for the basic one-bit cell. Derive the equation for the  $Z$  output only.

