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COE 202, Term 121
Digital Logic Design

Quiz# 3

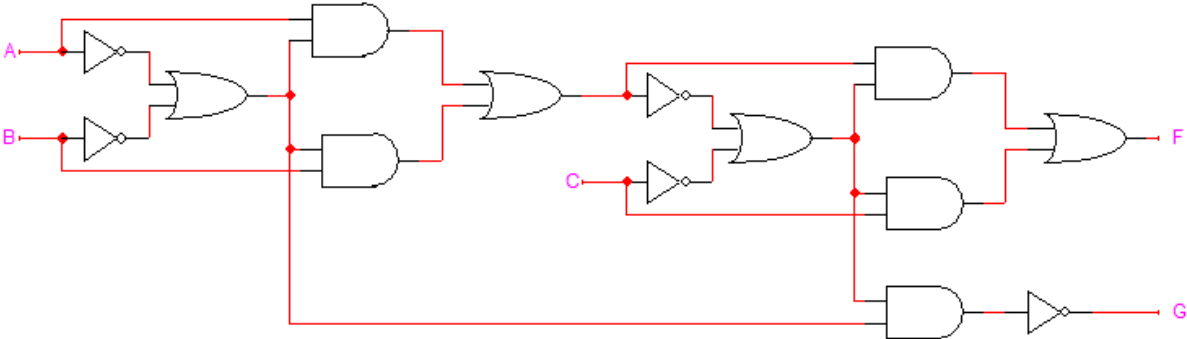
Date: Saturday, Nov. 10

Q1. For the Boolean function $F(W, X, Y, Z) = \sum m(0, 1, 2, 3, 7, 8, 10)$, $d(W, X, Y, Z) = \sum m(5, 6, 11, 15)$ shown in the k-map below:

YZ WX	00	01	11	10
00	1	1	1	1
01	0	x	1	x
11	0	0	x	0
10	1	0	x	1

- (i) Identify all the *prime implicants* and the *essential prime implicants* of F.
- (ii) Simplify the Boolean function **F** into a minimal sum-of-products expression.

Q2. Implement the logic circuit given below using only NOR and NOT gates



Q3. Design a 3-bit decremter using only basic gates (AND, OR, and NOT). The circuit takes a 3-bit unsigned number $\mathbf{I} = \mathbf{I}_2\mathbf{I}_1\mathbf{I}_0$ as input and generates a 3-bit output number $\mathbf{Z} = \mathbf{Z}_2\mathbf{Z}_1\mathbf{Z}_0$ and a **Valid** output \mathbf{V} . Whenever $\mathbf{I} > \mathbf{0}$ the output $\mathbf{Z} = \mathbf{I} - \mathbf{1}$ and $\mathbf{V} = \mathbf{1}$. If $\mathbf{I} = \mathbf{0}$, the output is invalid which is indicated by an output $\mathbf{V} = \mathbf{0}$. Derive the simplified Boolean expressions of all outputs.