

**COE 202, Term 132**  
**Digital Logic Design**

**Quiz# 2**

Date: Tuesday, Feb. 25

**Q1.** Prove the identity of each of the following Boolean functions using algebraic manipulation. Start with the left-hand side expression and derive from it the right-hand side expression.

**i.**  $\bar{a}\bar{c} + ad + b\bar{c}d = \bar{a}\bar{c} + ad$

$$\begin{aligned} A\bar{C} + AD + BC\bar{D} &= A\bar{C} + AD + BC\bar{D} + C\bar{D} \text{ (by consensus between } A\bar{C} + AD) \\ &= A\bar{C} + AD + C\bar{D} \text{ (by absorption of } BC\bar{D} \text{ in } C\bar{D}) \\ &= A\bar{C} + AD \text{ (by consensus between } A\bar{C} + AD) \end{aligned}$$

Another Solution:

$$\begin{aligned} A\bar{C} + AD + BC\bar{D} &= A\bar{C} + AD + BC\bar{D}(A + A') \\ &= A\bar{C} + AD + ABC\bar{D} + A'BC\bar{D} \\ &= A\bar{C} + AD \text{ (by absorption of } ABC\bar{D} \text{ in } AD \text{ and absorption of } A'BC\bar{D} \text{ in } A\bar{C}) \end{aligned}$$

**ii.**  $\overline{(\bar{a}[\bar{c} + d] + c[\bar{b} + \bar{d}] + \bar{c}\bar{d})} = ad(b + \bar{c})$

$$\begin{aligned} &= (a + c\bar{d})(c' + b d)(c + d) \text{ (by Demorgan's Law)} \\ &= (a c' + a b d)(c + d) \text{ (by distributive law)} \\ &= (a c' d + a b c d + a b d) \text{ (by distributive law)} \\ &= a c' d + a b d \text{ (by absorption of } a b c d \text{ in } a b d) \\ &= a d (c' + b) \text{ (by distributive law)} \end{aligned}$$

**Q2.** Given the Boolean functions  $F(A, B, C) = \sum m(0, 2, 4, 7)$  and  $G(A, B, C) = \prod M(0, 3, 5, 6)$ .

**i.** Give the algebraic sum of minterms expression for  $F$ .

$$F = \bar{A} \bar{B} \bar{C} + \bar{A} B \bar{C} + A \bar{B} \bar{C} + A B C$$

**ii.** Express the function  $G$  as a sum of minterms,  $G = \sum m(\dots)$

$$G = \sum m(1, 2, 4, 7)$$

**iii.** Express the function  $F \cdot G$  as a sum of minterms,  $F \cdot G = \sum m(\dots)$

$$F \cdot G = \sum m(2, 4, 7)$$

**iv.** Express the function  $F+G$  as a product of maxterms,  $F + G = \prod M(\dots)$

$$F + G = \sum m(0, 1, 2, 4, 7) = \prod M(3, 5, 6)$$