

## Physical constants, conversion factors, and useful equations

### Physical Constants

$$\begin{aligned}
 R &= 8.314 \text{ J mol}^{-1} \text{ K}^{-1} \\
 &= 0.08206 \text{ L atm K}^{-1} \text{ mol}^{-1} \\
 &= 0.08314 \text{ L bar K}^{-1} \text{ mol}^{-1} \\
 N_A &= 6.022 \times 10^{23} \text{ mol}^{-1} \\
 k_B &= 1.381 \times 10^{-23} \text{ J K}^{-1} \\
 h &= 6.626 \times 10^{-34} \text{ J s} \\
 F &= 96,485 \text{ C mol}^{-1} \\
 c &= 2.998 \times 10^8 \text{ m s}^{-1} \\
 g &= 9.81 \text{ m s}^{-2} \\
 e &= 1.6022 \times 10^{-19} \text{ C} \\
 \epsilon_0 &= 8.854 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1} \\
 B &= 0.51 \text{ mol}^{-1/2} \text{ dm}^{3/2} \text{ (in H}_2\text{O, 25}^\circ\text{C)}
 \end{aligned}$$

### Other Units

$$\begin{aligned}
 1 \text{ dm}^3 &= 1 \text{ L} \\
 1 \text{ dm}^3 &= 1000 \text{ cm}^3 \\
 1 \text{ J} &= 1 \text{ kg m}^2 \text{ s}^{-2} \\
 1 \text{ atm} &= 1.01325 \times 10^5 \text{ Pa} \\
 1 \text{ atm} &= 760 \text{ mmHg} \\
 1 \text{ Torr} &= 1 \text{ mmHg} \\
 1 \text{ Torr} &= 133.322 \text{ Pa} \\
 1 \text{ bar} &= 10^5 \text{ Pa} \\
 E &= h\nu \\
 c &= \nu\lambda \\
 PV &= nRT \\
 (RT)/F &= 25.6926 \text{ mV at } 25^\circ\text{C} \\
 \ln(x)/\log_{10}(x) &= 2.30259 \text{ for all } x \\
 \ln(1 - \theta) &= -\theta \\
 \text{if } \theta &\ll 1 \\
 \text{Quadratic equation:} \\
 a x^2 + b x + c &= 0 \\
 \text{solutions:} \\
 x_{1,2} &= (1/2a)[-b \pm (b^2 - 4ac)^{1/2}] \\
 RT/F &= 25.70 \text{ mV (at } 25^\circ\text{C for ln)} \\
 &= 59.16 \text{ mV (at } 25^\circ\text{C for log}_{10}) \\
 \text{Michaelis - Menten equation:} \\
 (1/R_0) &= (1/R_{\max}) + (K_m/R_{\max}) \times (1/[S]_0) \\
 \text{Lindemann mechanism:} \\
 k_{\text{uni}} &= k_1 k_2 [M] / (k_{-1} [M] + k_2)^{-1} \\
 \text{Langmuir isotherm:} \\
 \theta &= KP / (1 + KP) \\
 1/R_0 &= 1/R_{\max} + (K_m/R_{\max}) (1/[S]_0) \\
 \text{Sequential reactions:} \\
 A &\xrightarrow{k_1} B \xrightarrow{k_2} C \\
 [B] &= (k_1 / (k_2 - k_{-1})) f(t) [A]_0 \\
 f(t) &= \exp(-k_1 t) - \exp(-k_2 t)
 \end{aligned}$$

### Important Equations

$$\begin{aligned}
 \Lambda &= \frac{\kappa}{c}, \quad \alpha = \frac{\Lambda}{\Lambda_0} \quad \text{and} \quad I = \frac{I}{2} \sum_i c_i z_i^2 \\
 \log_{10} \gamma_i &= -z_i^2 B \sqrt{I} \quad \text{and} \quad \log_{10} \gamma_{\pm} = -z_{\pm} / z_{\pm} / B \sqrt{I} \\
 \Lambda_m &= \Lambda_m^\circ - K (c/c_0)^{1/2} \text{ (strong)} \\
 1/\Lambda_m &= 1/\Lambda_m^\circ + c \Lambda_m / [(\Lambda_m^\circ)^2 K_a] \text{ (weak)} \\
 \Delta G^\circ_{\text{solution}} &= (1/\epsilon_r - 1) z^2 e^2 N_A / (8\pi \epsilon_0 r) \\
 E &= E^\circ - \frac{RT}{zF} \ln \left( \frac{[Y]^y [Z]^z}{[A]^a [B]^b} \right)^u \\
 \Delta G &= -nFE \quad \text{and thus} \quad \Delta G^\circ = -nFE^\circ \\
 \Delta S &= nF(dE/dt)_P \\
 a_{\pm}^{m+n} &= a_+^m a_-^n \text{ for } A_m B_n \\
 \kappa &= [2e^2 N_A \times (1000 \text{ L m}^{-3}) / (\epsilon_0 k_B T)]^{1/2} \times [\rho_{\text{solvent}} / \epsilon_r]^{1/2} \\
 E^\circ_{\text{AgCl/Ag}} &= +0.222 \text{ V} \\
 k &= A e^{-E_a / RT} \\
 k &= \frac{k_B T}{h} e^{-\Delta^\ddagger G^\circ / RT} \\
 E_a &= \Delta^\ddagger H^\circ - P \Delta^\ddagger V^\circ + RT \text{ (sol)} \\
 &= \Delta^\ddagger H^\circ - \Sigma \nu RT + RT \text{ (gas)} \\
 \Delta G^\ddagger &= \Delta H^\ddagger - T \Delta S^\ddagger \\
 t_{1/2} &= (\ln 2) / k \text{ (1}^\text{st} \text{ order)} \\
 \text{fluorescence lifetime } t_f &= (k_f + k_q [Q])^{-1} \\
 R_0 &= k_2 [S]_0 [E]_0 / ([S]_0 + K_m), \\
 K_m &= (k_{-1} + k_2) / k_1 \\
 k_2 [E]_0 &= R_{\max} = V \\
 D &= (1/3) v_{\text{ave}} \lambda \\
 \kappa &= (1/3) (C_{V,m} / N_A) v_{\text{ave}} N_p \lambda \\
 PV &= nRT = (N/N_A) RT, \\
 (C_{V,m} / N_A) &= (3/2) k_B \\
 \eta &= (1/3) v_{\text{ave}} N_p \lambda m \\
 f &= 6\pi \eta r = k_B T / D \\
 v_{\text{ave}} &= (8RT / (\pi M))^{1/2} \\
 N_p \lambda &= 1 / ((\sqrt{2}) \sigma), \\
 \lambda &= RT / (P N_A (\sqrt{2}) \sigma) \\
 N_p &= (N/V) = P N_A / (RT) \\
 \sigma &= \pi d^2 \\
 x_{\text{rms}} &= \sqrt{(2Dt)} \quad \text{(1-Dimension)} \\
 r_{\text{rms}} &= \sqrt{(6Dt)} \quad \text{(3-Dimension)} \\
 \text{Poisseuille equation: } (\Delta V / \Delta t) &= (\pi r^4 / (8\eta)) \Delta P / \Delta L \\
 \text{Stokes-Einstein equation: } D &= k_B T / (6\pi \eta r) \\
 \text{if } r(\text{particle}) &\gg r(\text{solvent molecule}) \\
 \text{Ostwald viscosimeter: } \eta &= A \rho t, \\
 \text{Capillary rise: } h &= 2\gamma / (\rho g r)
 \end{aligned}$$

### Note:

Quantum yield/efficiency =  $\Phi$  = moles of product formed / moles of photons absorbed