

**King Fahd University of Petroleum & Minerals**  
**Chemical Engineering Department**  
**CHE 560 –Numerical Methods in Chemical Engineering**  
**2010 - 2011 (102)**

**HW#4**

Due: Tue. 3-April-2011

For the IVP's example solved in class:

$$\frac{dy_1}{dt} = -\phi_1 y_1$$
$$\frac{dy_2}{dt} = \phi_1 y_1 - \phi_2 y_2^2$$

Modify code\_3.f to include the following methods

- (a) (10 points) 1<sup>st</sup>-order explicit Euler (for IMETHOD = 4 include new subroutine EXPEULER)
- (b) (15 points) 1<sup>st</sup>-order implicit Euler (backward Euler) (for IMETHOD = 5 include new subroutine IMPEULER)
- (c) (15 points) 4<sup>th</sup>-order Runge-Kutta-Gill (for IMETHOD = 6 include new subroutine RKG4)

Note that for part (b) subroutine residuals and jacobian must be modified.

Send this first program as yourname-HW4-part1.f

- (d) (30 points) If the IVP's are linear :

$$\frac{dy_1}{dt} = -\phi_1 y_1$$
$$\frac{dy_2}{dt} = \phi_1 y_1 - \phi_2 y_2$$

Modify code\_3.f to solve the above problem using 1<sup>st</sup>-order implicit Euler (backward Euler). In this case, you have to solve a system of linear equations at each time step of the form:

$$\underline{\underline{A}} \cdot \underline{y} = \underline{B}$$

Define exactly in your analysis what are the matrix and the right hand side vector.

Send this second program as yourname-HW4-part2.f