

King Fahd University of Petroleum & Minerals
Chemical Engineering Department
CHE 204 – Transport Phenomena I
2008 - 2009 (081)

HW#11

Due: no submission required

Problem 1. (30 points)

In the analysis of laminar boundary layer flow over a flat plate, a velocity profile is assumed as follows:

$$\frac{v_x}{v_{x\infty}} = f(\zeta),$$

where $\zeta \equiv \frac{y}{\delta(x)}$ and then substituted in the momentum balance equation eqn. (8.4).

Assuming the following form: $f(\zeta) = a + b\zeta + c\zeta^2 + d\zeta^3$, where a , b , c and d are constants. Answer the following questions:

- (a) Use the properties of the function $f(\zeta)$ to evaluate the constants a , b , c and d .
- (b) Obtain an expression for the thickness of the boundary layer, δ , along the plate, as function of x and Re_x where x is the distance from the edge of the plate.
- (c) Show that the drag coefficient c_f is given by: $c_f \sqrt{Re_x} = 0.646$.

Problem 2. (30 points)

Carbon dioxide gas ($\rho = 1.8 \text{ kg/m}^3$ and $\mu = 1.5 \times 10^{-5} \text{ Pa s}$) flows parallel to a flat plate at a velocity 1 km/hr. Use the simplified analysis of the boundary layer flow discussed in sections 8.2 and 8.5 of your textbook to answer the following questions:

- (a) Calculate the distance L_t at which the boundary layer undergoes a transition from laminar to turbulent flow.
- (b) Calculate the thickness of the boundary layer at a distance $L_t - 1$ and $L_t + 1$ meters.
- (c) Calculate the drag force over the flat plate at a distance $L_t + 1$ meters.