

1.5  
Reynolds Number

Cross-sectional area

$$A = \frac{\pi D^2}{4} = \frac{\pi \left(\frac{1.05}{12}\right)^2}{4} = 0.00601 \text{ ft}^2$$

Volumetric flow rate

$$Q = \frac{35}{7.48 \times 60} = 0.0780 \frac{\text{ft}^3}{\text{s}}$$

Mean velocity

$$u_m = \frac{Q}{A} = \frac{0.0780}{0.00601} = 12.98 \frac{\text{ft}}{\text{s}}$$

Reynolds number

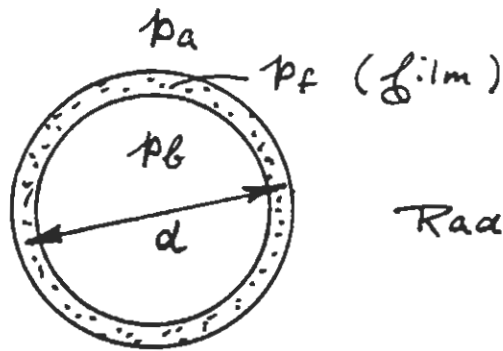
$$Re = \frac{\rho u_m D}{\mu} = \frac{62.3 \times 12.98 \times 1.05/12}{1.2 \times 0.000672}$$

$$\left. \begin{array}{l} \frac{\text{lbm}}{\text{ft}^3} \frac{\text{ft}}{\text{s}} \text{ ft} \\ \text{cP} \frac{\text{cP}}{\text{lbm} \cdot \text{ft} \cdot \text{s}} \end{array} \right\} \text{All units cancel}$$

$$\dot{=} \underline{\underline{87,740}} \quad (\text{dimensionless})$$

1.6  
Pressure in Bubble

Atmosphere



From notes, The increase in pressure as we go inwards across a convex surface is

$$\left. \begin{aligned} p_f - p_a &= \frac{2\sigma}{a} \\ p_b - p_f &= \frac{2\sigma}{a} \end{aligned} \right\} \begin{array}{l} \text{Two surfaces} \\ \text{are involved} \end{array}$$

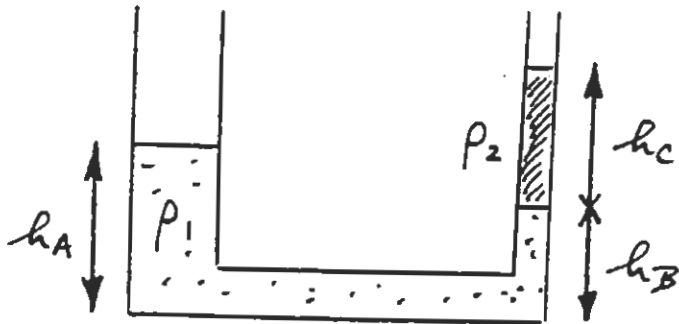
Hence, by addition,

$$p_b - p_a = \frac{4\sigma}{a} = \frac{8\sigma}{d}$$

$$p_b = p_a + \frac{8\sigma}{d}$$

1.10-1

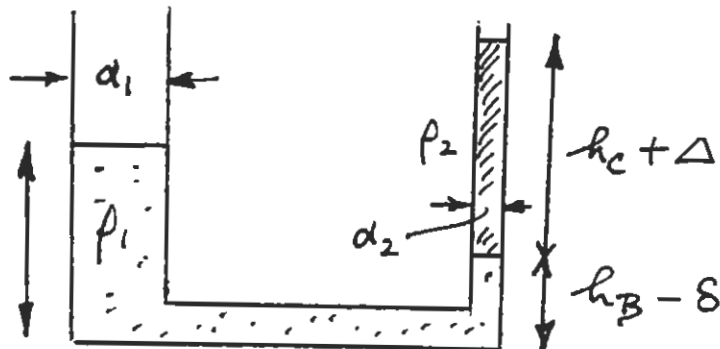
Differential Manometer



$$\rho_1 (h_A - h_B) = \rho_2 h_C \quad (1)$$

Before

Now add  $\Delta$  to  $h_C$  and let  $h_B$  decline by  $\delta$



From volume conservation

$$\rho_1 \left( h_A + \delta \frac{d_2^2}{d_1^2} - (h_B - \delta) \right) = \rho_2 (h_C + \Delta) \quad (2)$$

Subtract (1) from (2)

$$\rho_1 \delta \left( \frac{d_2^2}{d_1^2} + 1 \right) = \rho_2 \Delta = \rho_2 \frac{v_2}{\frac{\pi d_2^2}{4}} \quad (3)$$

Equation (3) gives  $\delta$  as a function of  $v_2$ , and also enables  $\rho_2$  to be found by observing the value of  $\delta$ .

1.10-2

Solution for  $\delta$  gives:

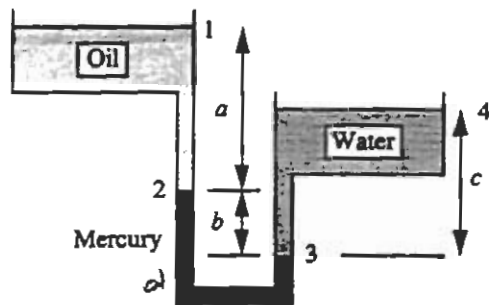
$$\delta = \frac{\rho_2}{\rho_1} \frac{4v_2}{\pi d_2^2} \left( \frac{d_1^2}{d_1^2 + d_2^2} \right)$$

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1.15

Three-Liquid Manometer



From hydrostatics:

$$p_4 = p_1 + \rho_o a g + \rho_m b g - \rho_w c g = p_1$$

Cancel  $p_1$  and divide by  $\rho_w g$ , with  $s = \frac{\rho}{\rho_w}$

$$s_o a + s_m b = c$$

$$b = \frac{c - s_o a}{s_m} = \frac{48 - 0.8 \times 72}{13.6} = -0.706$$

Thus the diagram is incorrect as drawn,  
and the mercury rises on the right by  
0.706 in.