

Mechanical Properties

ISSUES TO ADDRESS...

- **Stress** and **strain**: Normalized force and displacements.
What are they? Why not use *load* and elongation/*deformation*?

$$\sigma = F / A_0 \quad \varepsilon = \Delta l / l_0$$

- **Elastic** behavior: When loads are small, how much deformation occurs? What materials deform least?

Young's Modulus: E [GPa]

- **Plastic** behavior: At what point do **dislocations** cause **permanent deformation**? What materials are most resistant to permanent deformation?

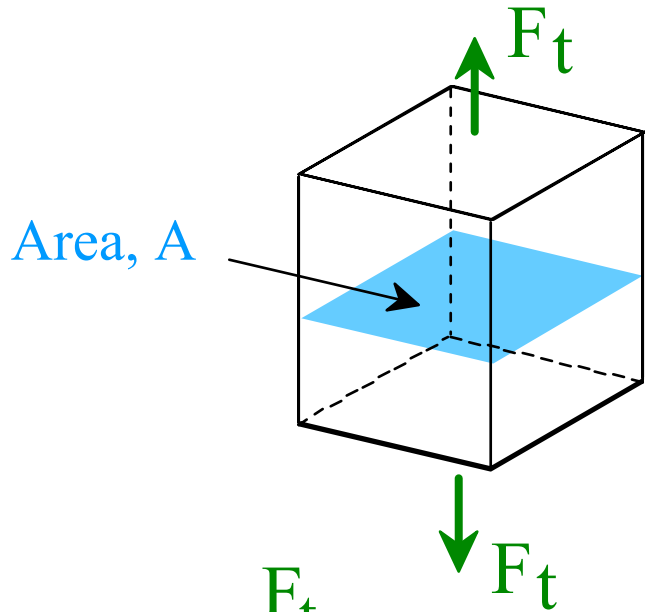
Yield Strength: σ_{YS} [GPa] (*permanent deformation*)

Ultimate Tensile Strength: σ_{TS} [GPa] (*fracture*)

- **Toughness** and **ductility**: What are they and how do we measure them?

Engineering Stress

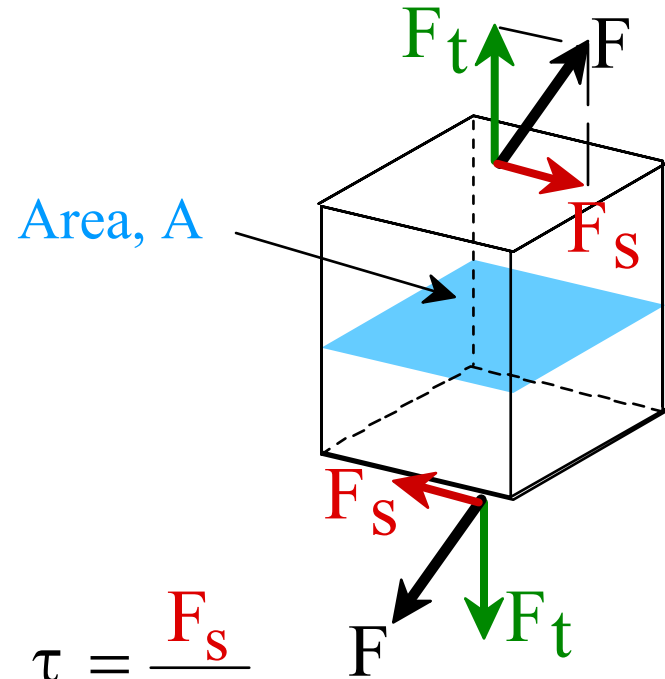
- Tensile stress, σ :



$$\sigma = \frac{F_t}{A_0}$$

original area
before loading

- Shear stress, τ :

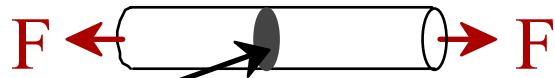


$$\tau = \frac{F_s}{A_0}$$


Stress has units:
 N/m^2 (or lb_f/in^2)

Common States of Stress

- Simple tension: cable



A_0 = cross sectional
Area (when unloaded)

$$\sigma = \frac{F}{A_0}$$


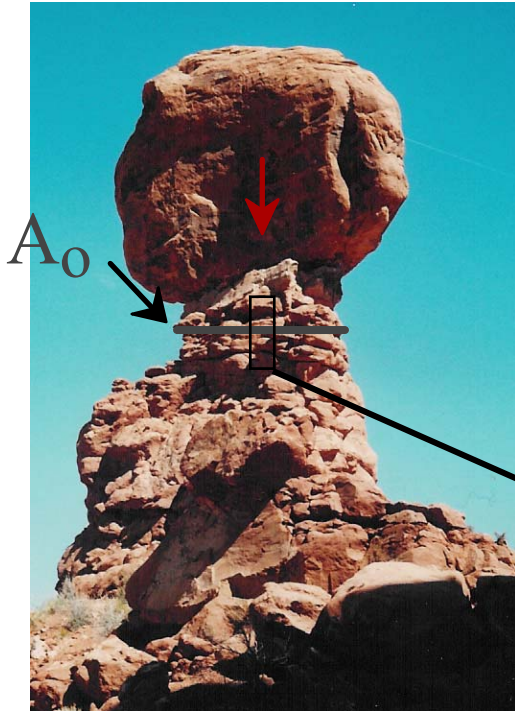
A diagram of a rectangular element under stress. Two red arrows labeled 'σ' point outwards from the left and right sides of the rectangle.



Ski lift (photo courtesy P.M. Anderson)

Common States of Stress

- **Simple** compression:



Balanced Rock, Arches National Park
(photo courtesy P.M. Anderson)



Canyon Bridge, Los Alamos, NM
(photo courtesy P.M. Anderson)

$$\sigma = \frac{F}{A_0}$$



Note: compressive structure member ($\sigma < 0$ here).

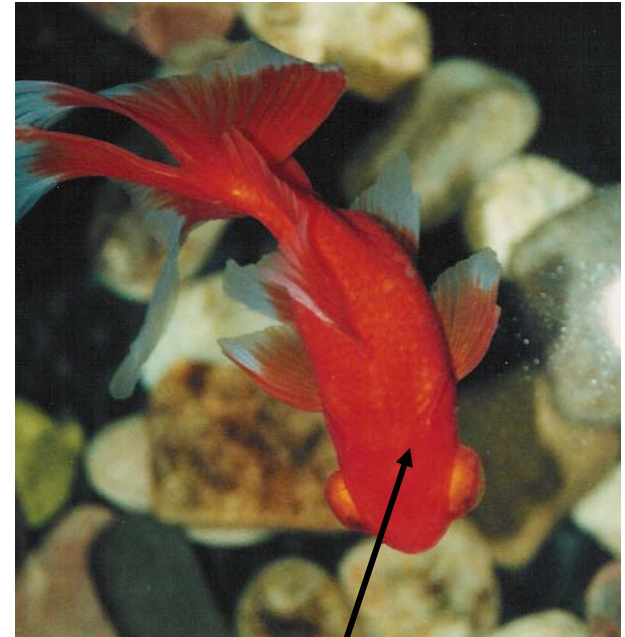
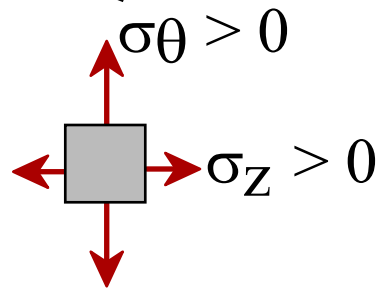
Common States of Stress

- Bi-axial tension:

- Hydrostatic compression:

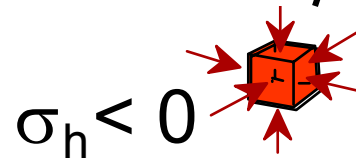


Pressurized tank
(photo courtesy
P.M. Anderson)



Fish under water

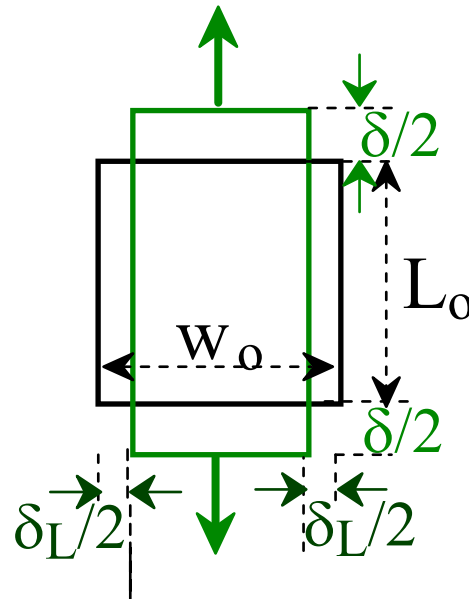
(photo courtesy
P.M. Anderson)



Engineering Strain

- **Tensile strain:**

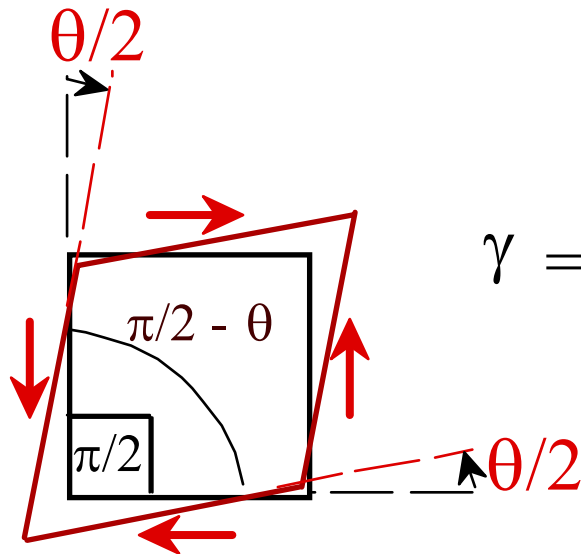
$$\epsilon = \frac{\delta}{L_0}$$



- **Lateral (width) strain:**

$$\epsilon_L = \frac{-\delta_L}{W_0}$$

- **Shear strain:**

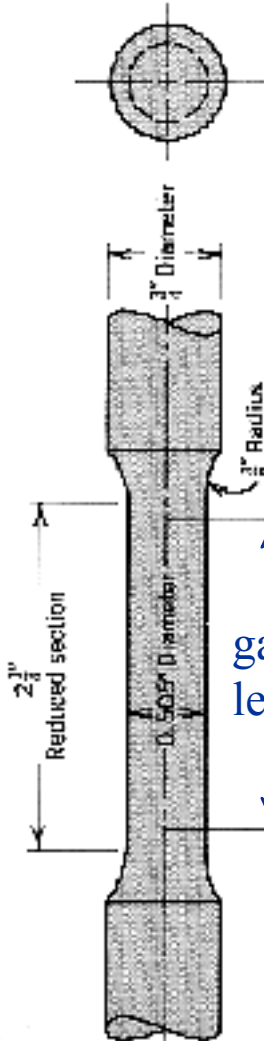


$$\gamma = \tan \theta$$

Strain is always dimensionless.

Strain Testing

- Tensile specimen



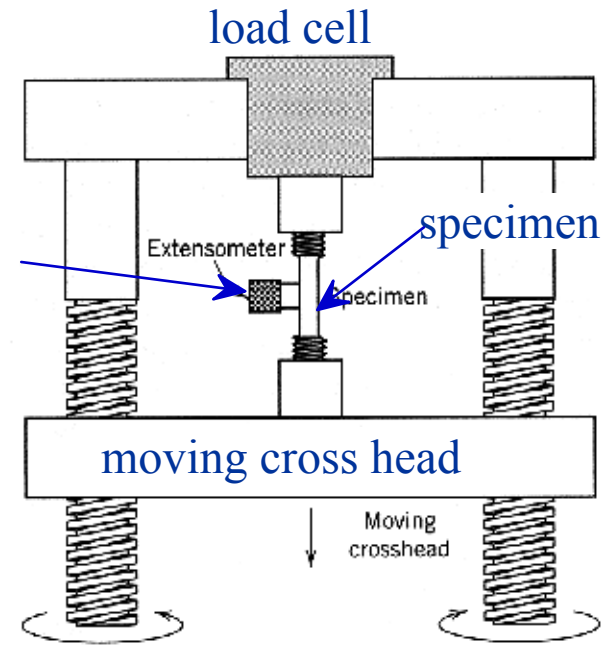
Adapted from Fig. 6.2, Callister 6e.

Often 12.8 mm x 60 mm

extensometer

gauge length = (portion of sample with reduced cross section)

- Tensile test machine

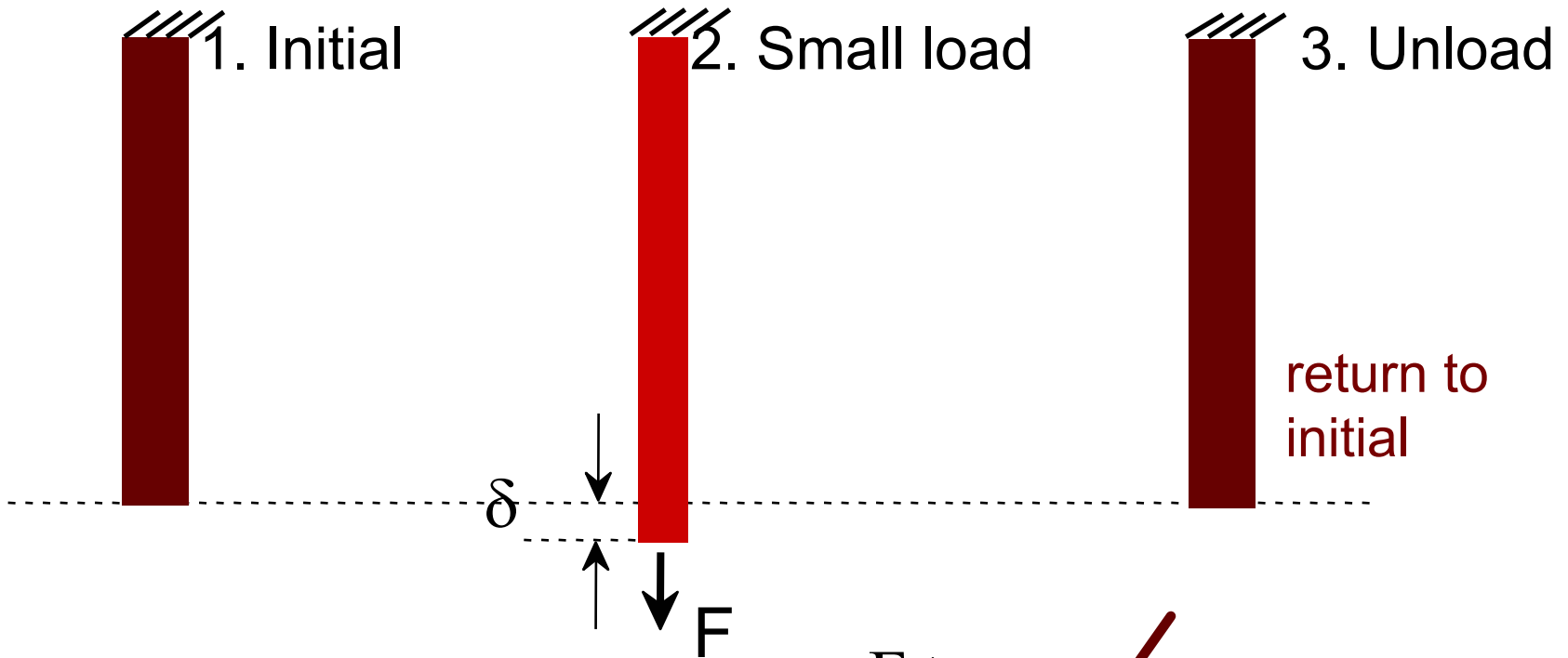


Adapted from Fig. 6.3, Callister 6e.

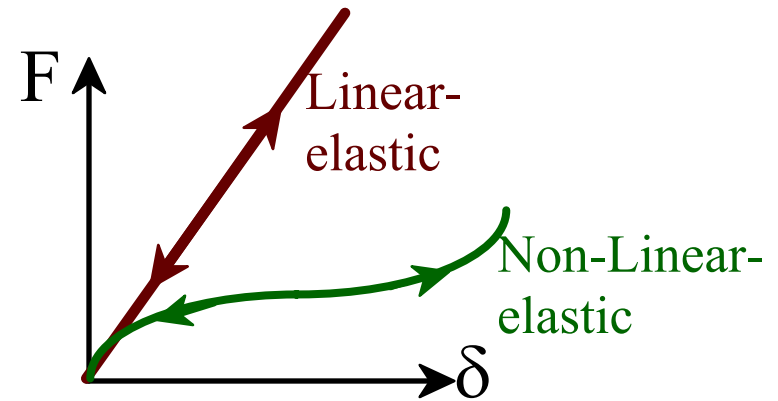
- Other types:

- compression: brittle materials (e.g., concrete)
- torsion: cylindrical tubes, shafts.

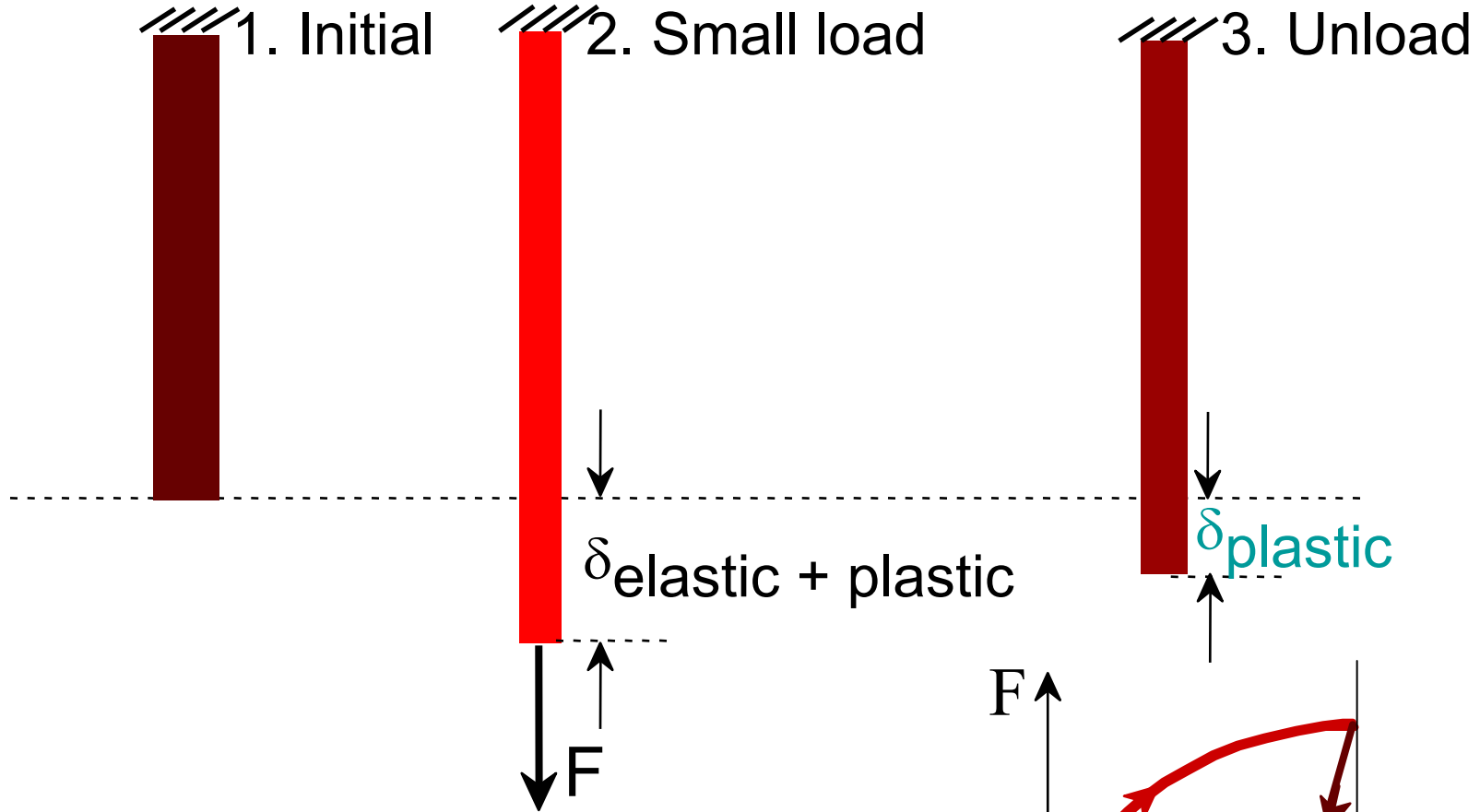
Elastic Deformation



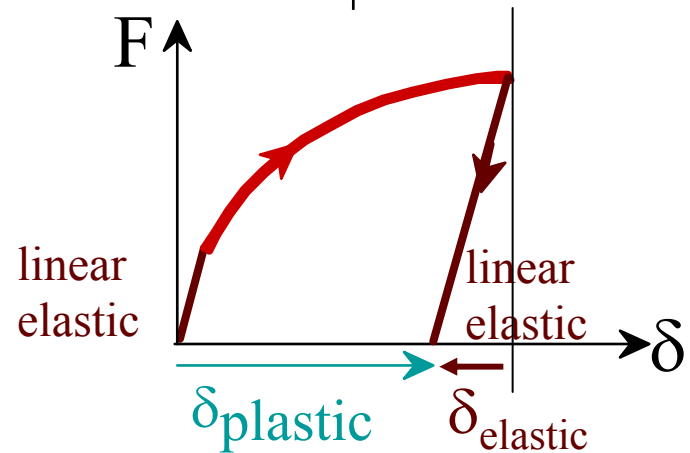
Elastic means **reversible!**



Plastic Deformation



Plastic means **permanent!**



Linear Elasticity

- **Modulus of Elasticity, E:**
(also known as Young's modulus)
- **Hooke's Law:** $\sigma = E \varepsilon$
- **Poisson's ratio, ν :**

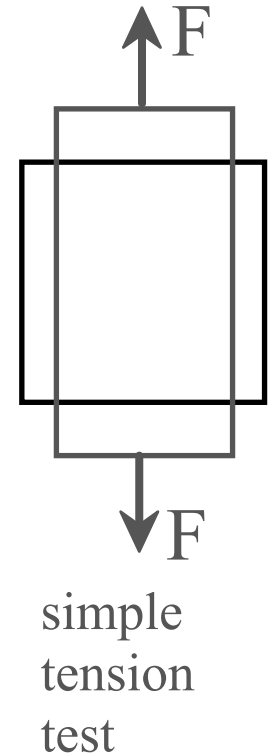
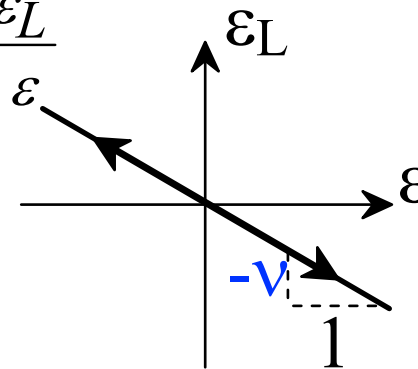
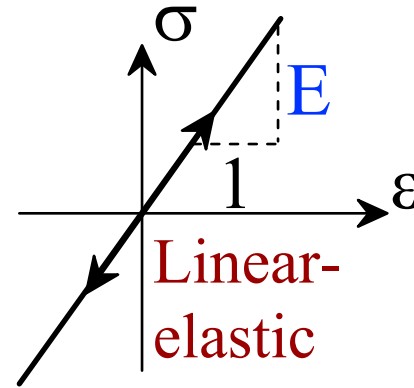
$$\nu = -\frac{\text{width strain}}{\text{axial strain}} = -\frac{\Delta w / w}{\Delta \ell / \ell} = -\frac{\varepsilon_L}{\varepsilon}$$

metals: $\nu \sim 0.33$
ceramics: ~ 0.25
polymers: ~ 0.40

Units:

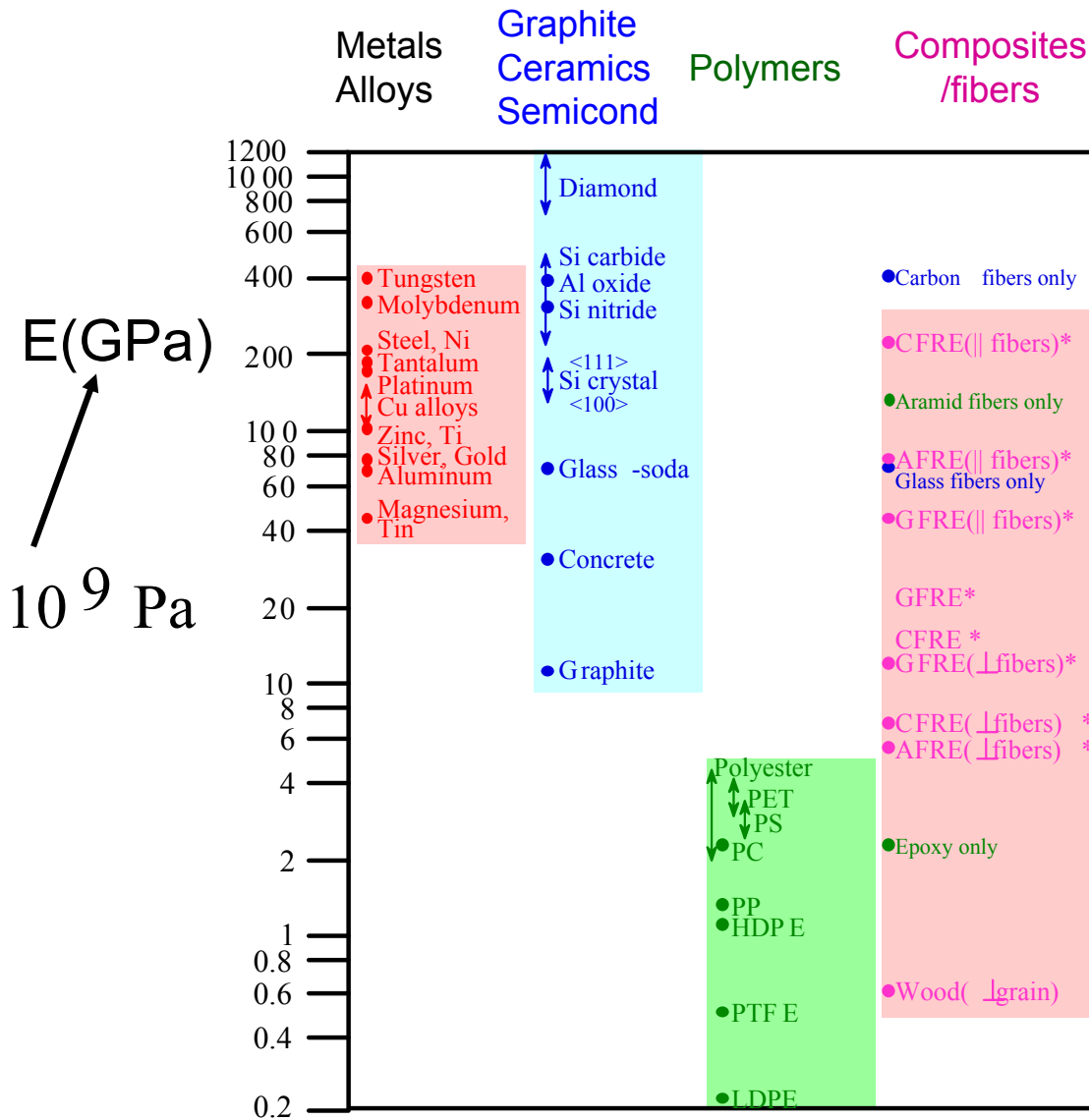
E: [GPa] or [psi]

ν : dimensionless



Why does ν have minus sign?

Young's Modulus, E



E_{ceramics}

$> E_{\text{metals}}$

$>> E_{\text{polymers}}$

Based on data in Table B2, *Callister 6e*.

Composite data based on reinforced epoxy with 60 vol% of aligned carbon (CFRE), aramid (AFRE), or glass (GFRE) fibers.

Poisson Ratio: materials specific

Metals:

| | | | | | | |
|------|------|------|------|------|------|------|
| Ir | W | Ni | Cu | Al | Ag | Au |
| 0.26 | 0.29 | 0.31 | 0.34 | 0.34 | 0.38 | 0.42 |

generic value ~ 1/3

Solid Argon: 0.25

Covalent Solids:

| | | | |
|------|------|--------------------------------|------|
| Si | Ge | Al ₂ O ₃ | TiC |
| 0.27 | 0.28 | 0.23 | 0.19 |

generic value ~ 1/4

Ionic Solids: MgO 0.19

Silica Glass: 0.20

Polymers: Network (Bakelite) 0.49

Chain (PE) 0.40

Elastomer: Hard Rubber (Ebonite) 0.39 (Natural) 0.49

Example: Hooke's Law

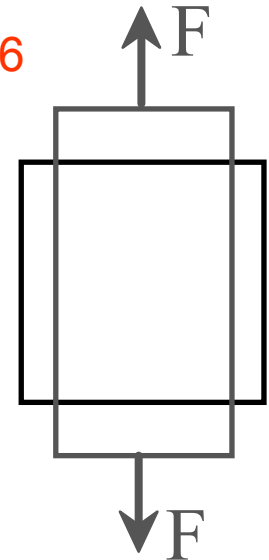
- Hooke's Law: $\sigma = E \varepsilon$

Copper sample (305 mm long) is pulled in tension with stress of 276 MPa. If deformation is elastic, what is elongation?

For Cu, $E = 110 \text{ GPa}$.

$$\sigma = E\varepsilon = E\left(\frac{\Delta l}{l_0}\right) \Rightarrow \Delta l = \frac{\sigma l_0}{E}$$

$$\Delta l = \frac{(276 \text{ MPa})(305 \text{ mm})}{110 \times 10^3 \text{ MPa}} = 0.77 \text{ mm}$$



simple
tension
test

Hooke's law involves axial (parallel to applied tensile load) elastic deformation.

Example: Poisson Effect

Tensile stress is applied along cylindrical brass rod (10 mm diameter). Poisson ratio is $\nu = 0.34$ and $E = 97 \text{ GPa}$.

- Determine load needed for $2.5 \times 10^{-3} \text{ mm}$ change in diameter if the deformation is entirely elastic?

Width strain: (note reduction in diameter)

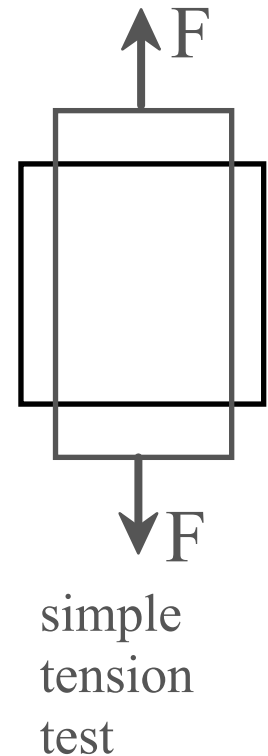
$$\varepsilon_x = \Delta d/d = -(2.5 \times 10^{-3} \text{ mm})/(10 \text{ mm}) = -2.5 \times 10^{-4}$$

Axial strain: Given Poisson ratio

$$\varepsilon_z = -\varepsilon_x/\nu = -(-2.5 \times 10^{-4})/0.34 = +7.35 \times 10^{-4}$$

Axial Stress: $\sigma_z = E\varepsilon_z = (97 \times 10^3 \text{ MPa})(7.35 \times 10^{-4}) = 71.3 \text{ MPa}$.

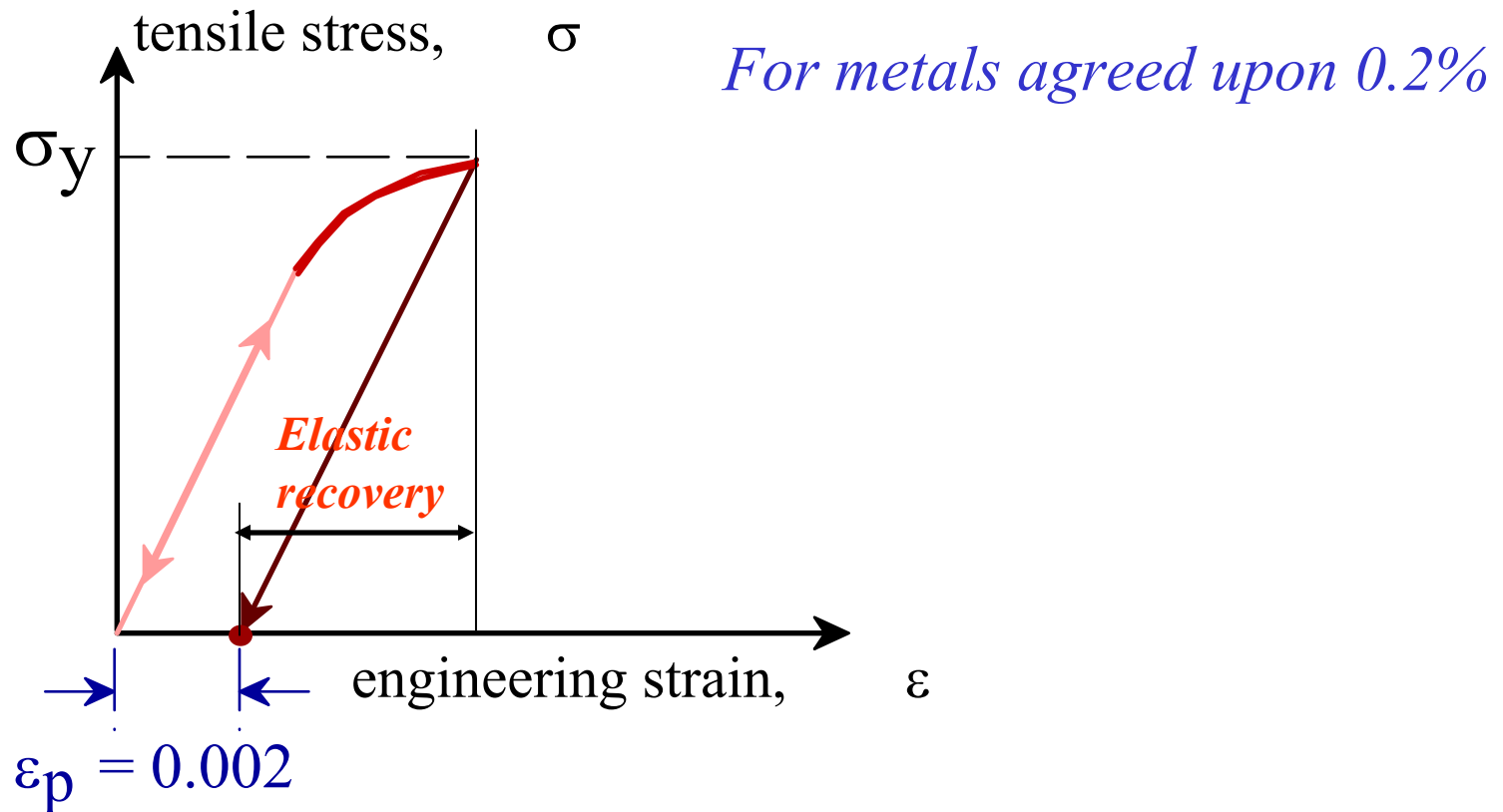
Required Load: $F = \sigma_z A_0 = (71.3 \text{ MPa})\pi(5 \text{ mm})^2 = 5600 \text{ N}$.



Yield Strength, σ_{YS}

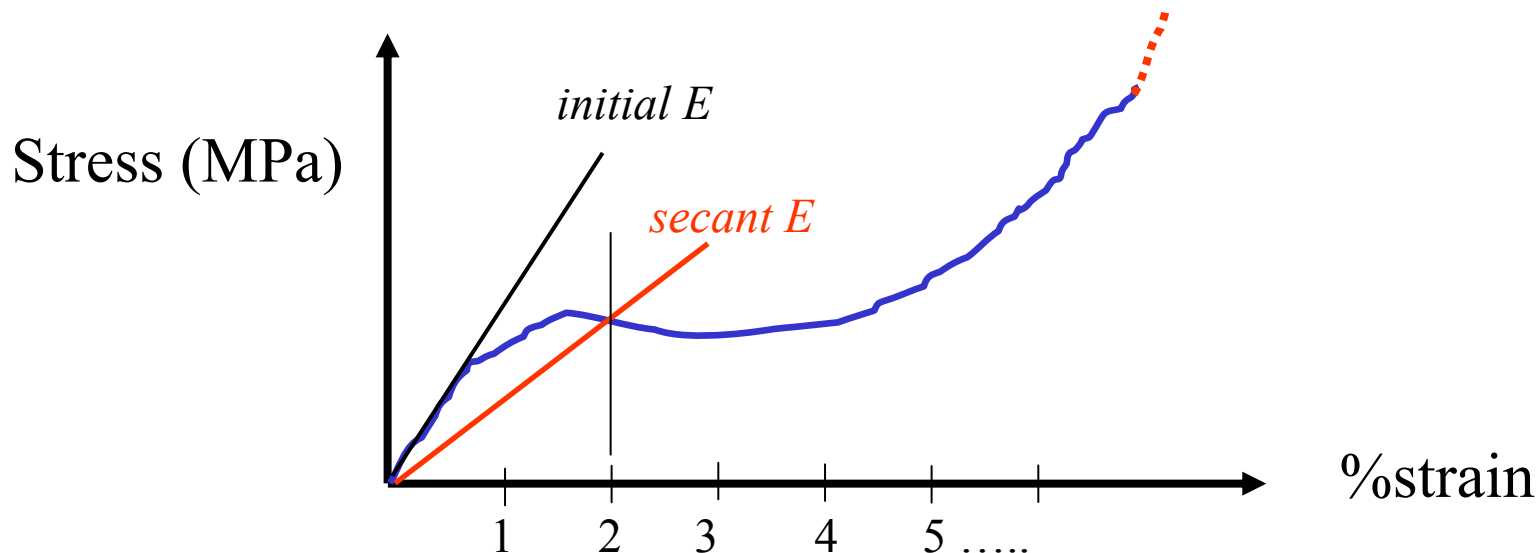
- Stress where *noticeable* plastic deformation occurs.

when $\epsilon_p = 0.002$

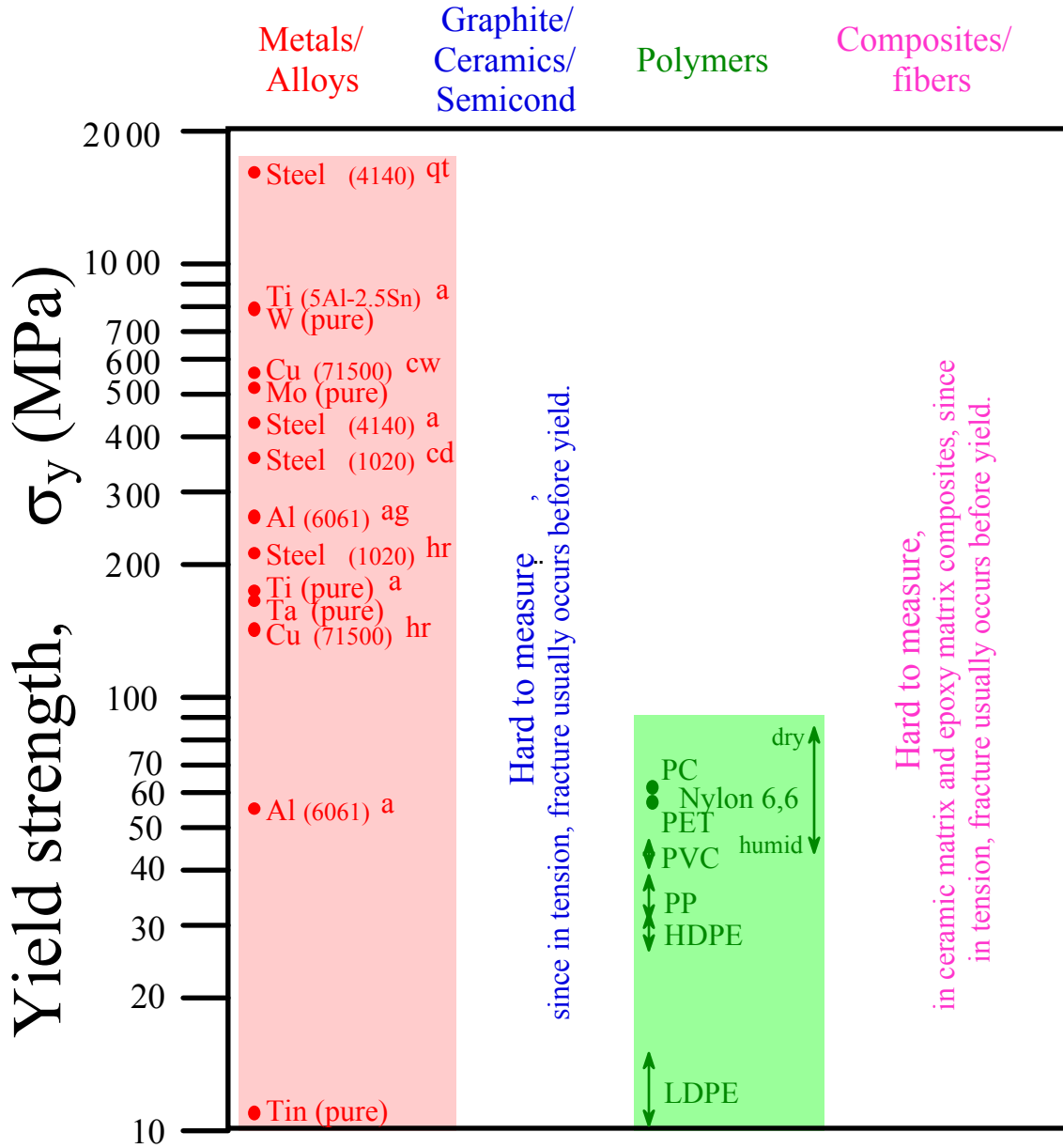


Polymers: Secant Modulus

- **Secant Modulus** is effective modulus at 2% strain.
- Modulus of polymer changes with *time* and *strain-rate*.
 - must report **strain-rate** $d\varepsilon/dt$ for polymers.
 - must report **fracture strain** ε_f **before** fracture.



Compare Yield Strength, σ_{YS}



$\sigma_y(\text{ceramics})$
 $\gg \sigma_y(\text{metals})$
 $\gg \sigma_y(\text{polymers})$

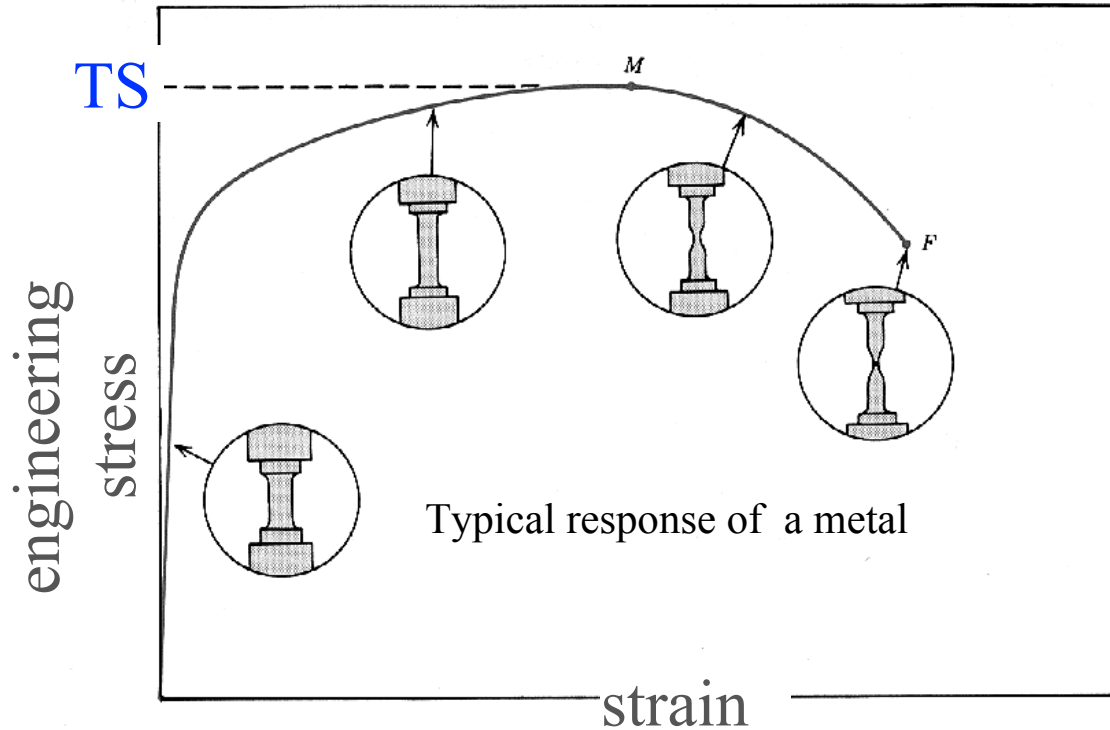
Room T values

Based on data in Table B4, *Callister 6e*.

- a = annealed
- hr = hot rolled
- ag = aged
- cd = cold drawn
- cw = cold worked
- qt = quenched & tempered

(Ultimate) Tensile Strength, σ_{TS}

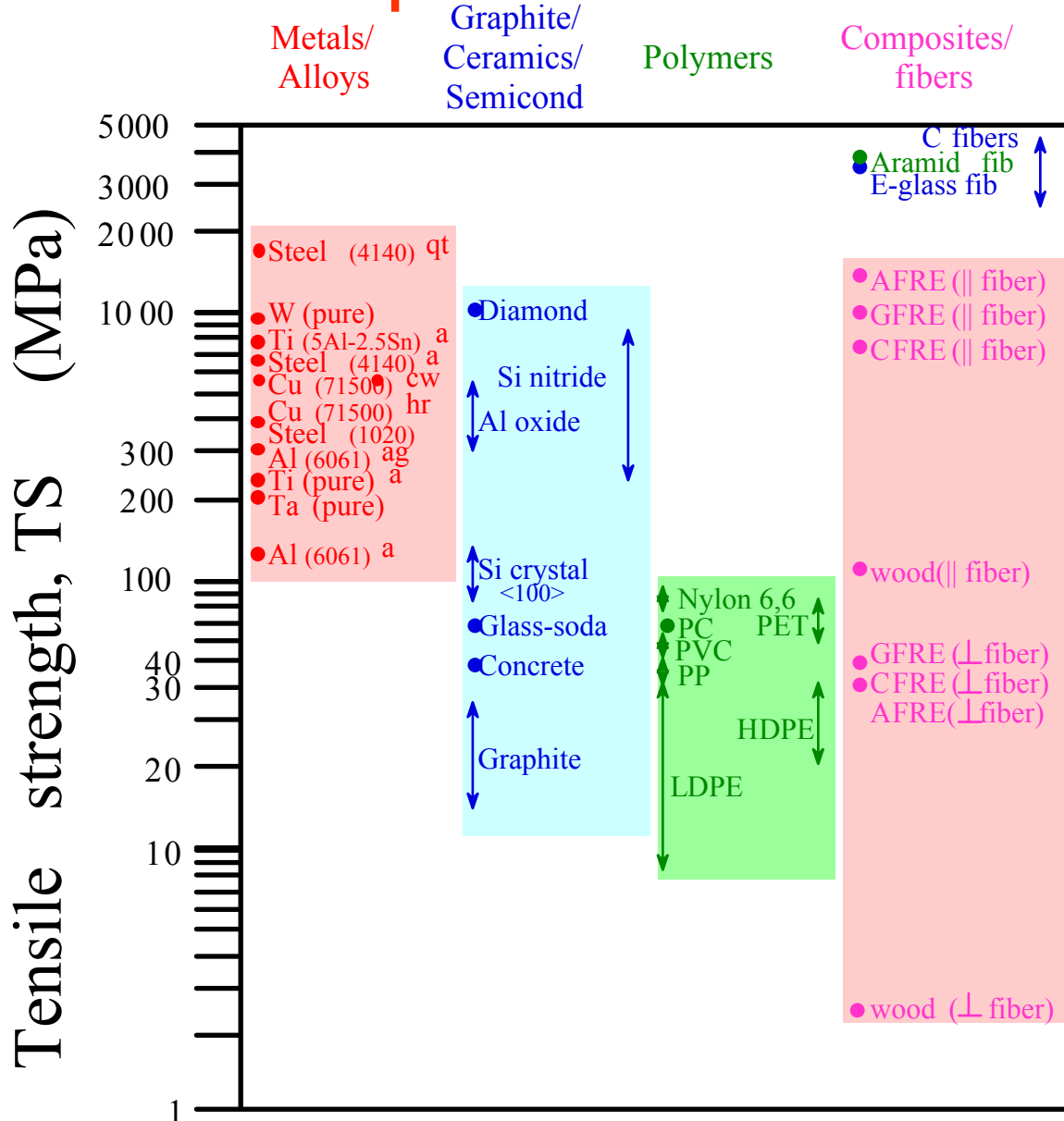
- Maximum possible engineering stress in tension.



Adapted from Fig. 6.11,
Callister 6e.

- Metals: occurs when **necking** starts.
- Ceramics: occurs when **crack propagation** starts.
- Polymers: occurs when **polymer backbones** are aligned and about to break.

Compare Tensile Strength, σ_{TS}



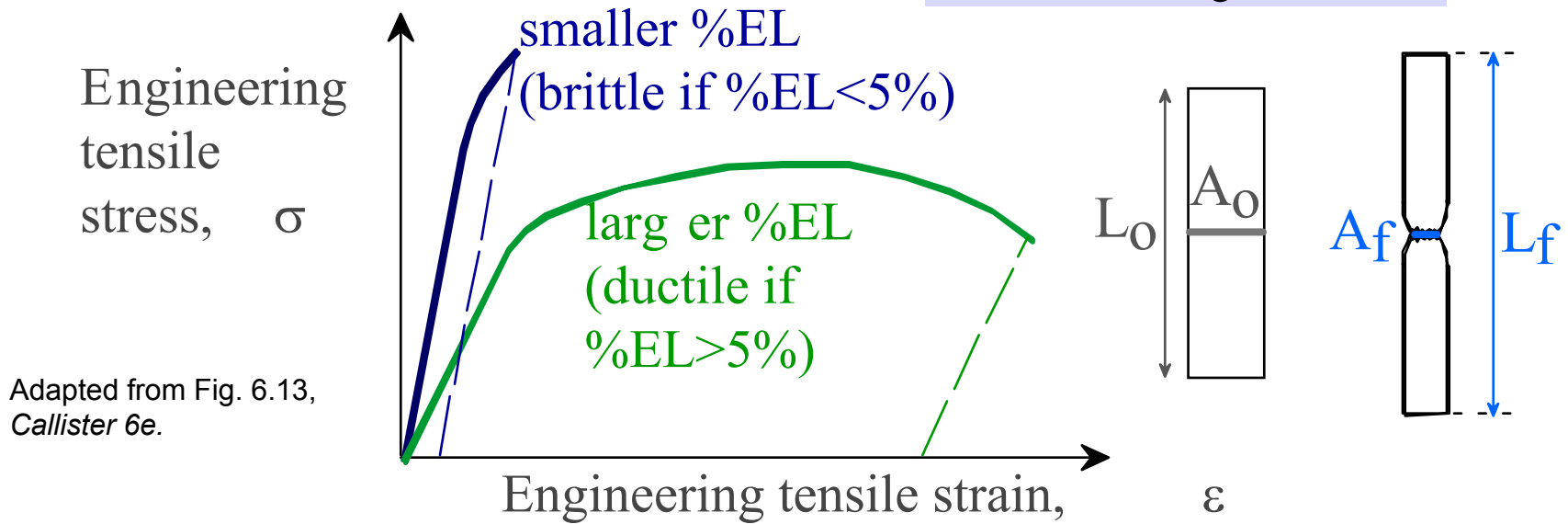
TS (ceram)
 \sim TS (met)
 \sim TS (comp)
 \gg TS (poly)
 Room T values

Based on data in Table B4, Callister 6e.

Ductility or %EL

- Plastic tensile strain at failure:

$$\%EL = \frac{L_f - L_o}{L_o} \times 100$$



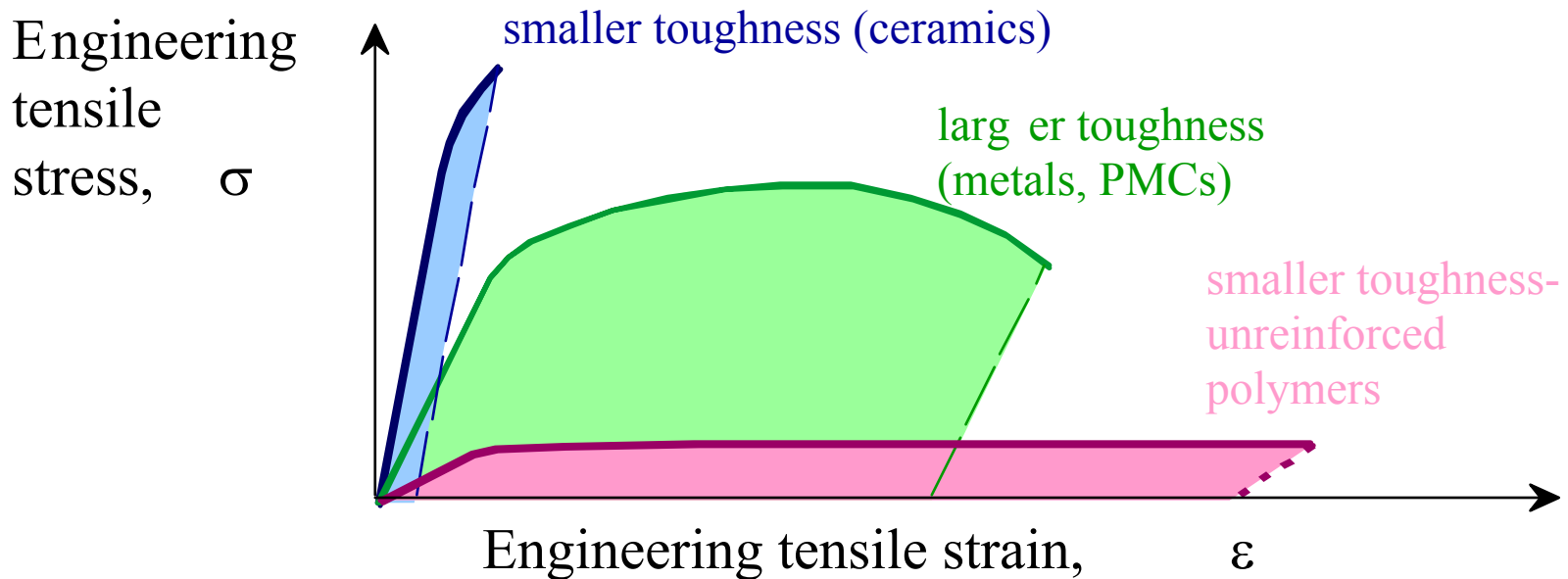
- Another ductility measure:

$$\%AR = \frac{A_o - A_f}{A_o} \times 100$$

- Note: %AR and %EL are often comparable.
 - Reason: crystal slip does not change material volume.
 - %AR > %EL possible if internal voids form in neck.

Toughness

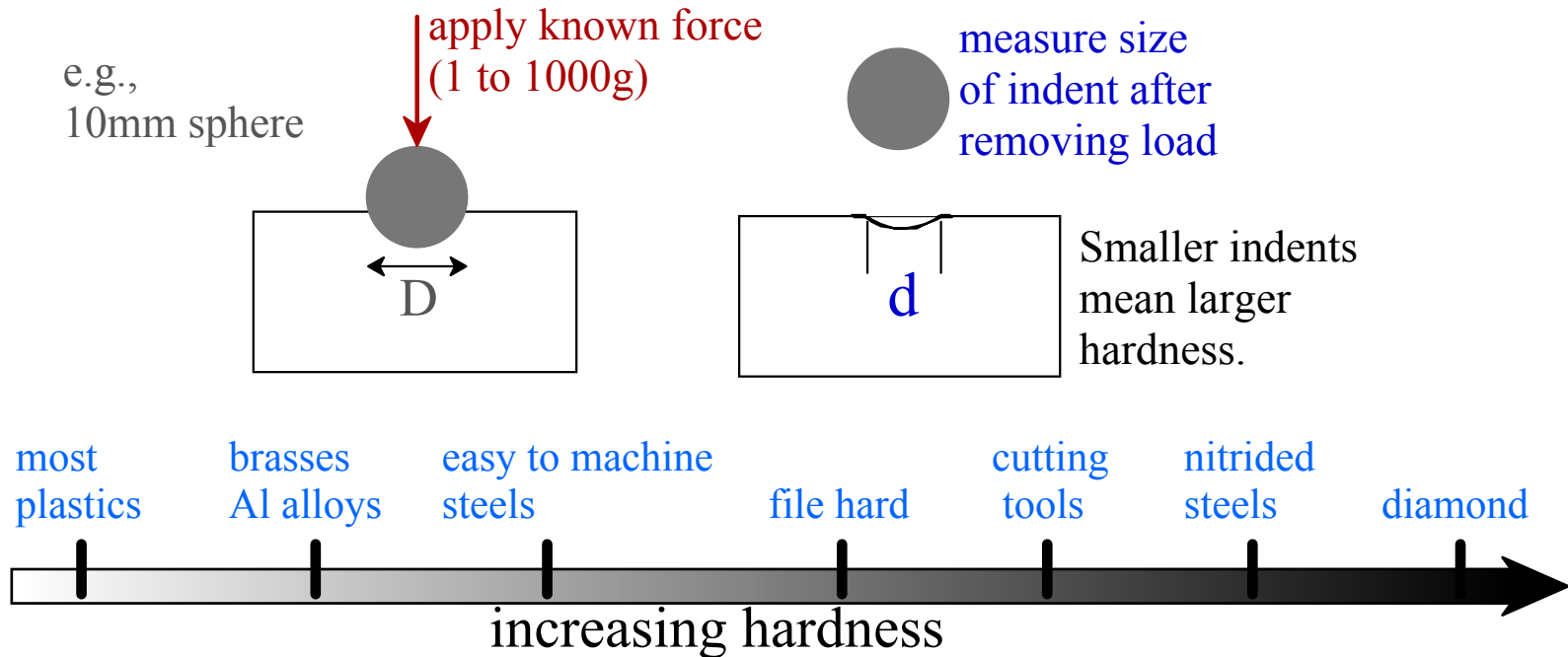
- Energy to break a unit volume of material,
or absorb energy to fracture.
- Approximate as area under the stress-strain curve.



Resilience is capacity to absorb energy when deformed *elastically* and *recover* all energy when unloaded.

Hardness

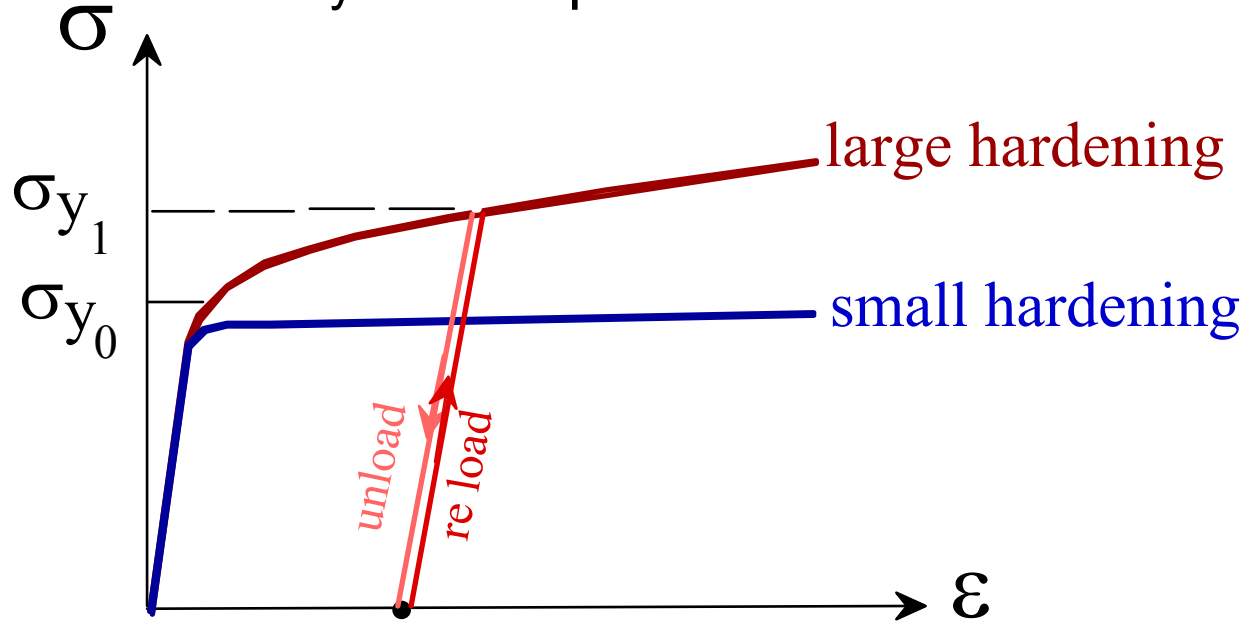
- Resistance to permanently indenting the surface.
- Large hardness means:
 - resistance to plastic deformation or cracking in compression.
 - better wear properties.



Adapted from Fig. 6.18, *Callister 6e*.

Hardening

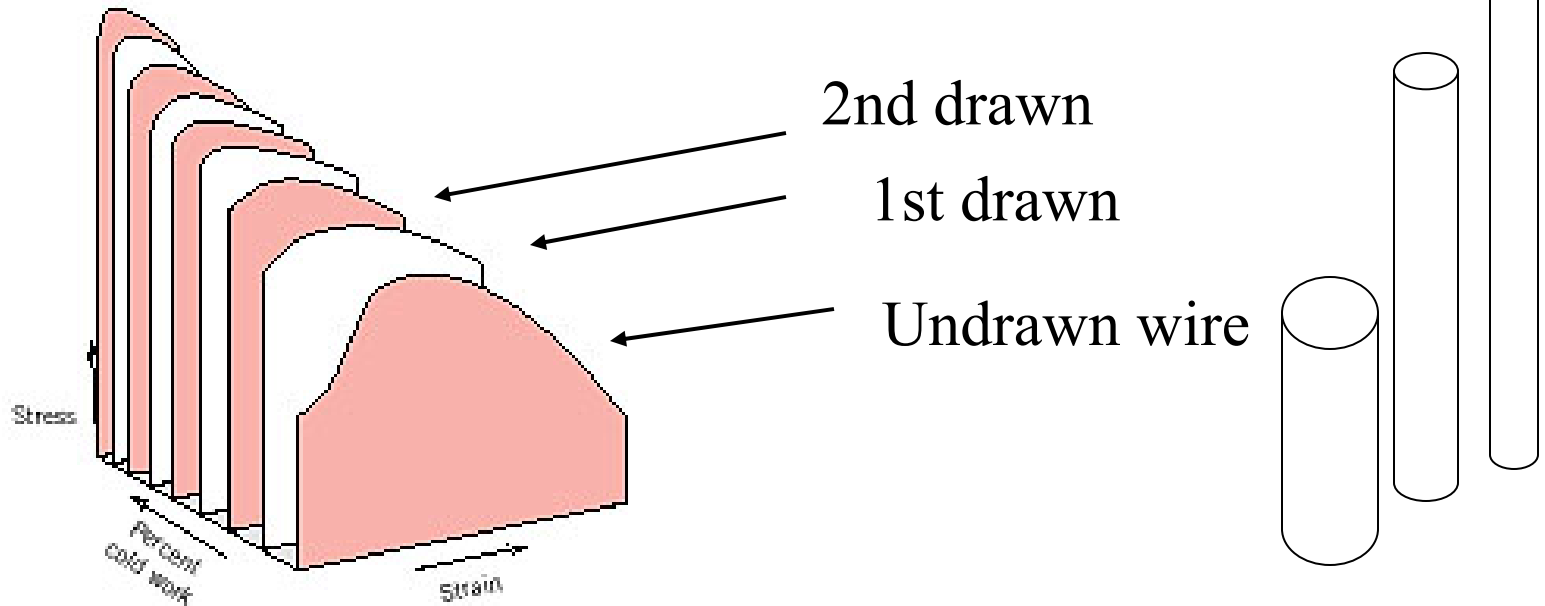
- An increase in σ_y due to plastic deformation.



Using Work-Hardening

Influence of “cold working” on low-carbon steel.

Stress-Strain plots as a function of % cold work applied



Processing: Forging, Rolling, Extrusion, Drawing,...

- Each draw of the wire *decreases* ductility, *increases* YS.
- Use drawing to strengthen and thin “aluminum” soda can.

Design Safety Factors

- Design uncertainties mean we do not push the limit.
- Factor of safety, N

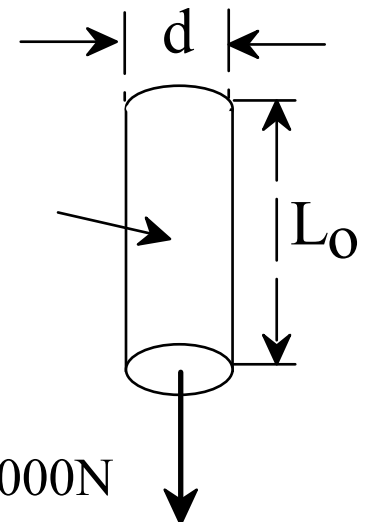
$$\sigma_{\text{working}} = \frac{\sigma_y}{N}$$

Often N is between 1.2 and 4

- Ex: Calculate diameter, d , to ensure that no yielding occurs in the 1045 carbon steel rod for an applied load of 220 kN. Use safety factor of 5.

$$\frac{220,000\text{N}}{\pi\left(d^2/4\right)} = \frac{\sigma_y}{N}$$

1045 plain
carbon steel:
 $\sigma_y=310\text{MPa}$
TS=565MPa



Summary

- **Stress** and **strain**: These are size-independent measures of load and displacement, respectively.
- **Elastic** behavior: This reversible behavior often shows a linear relation between stress and strain. To minimize deformation, select a material with a large elastic modulus (E or G).
- **Plastic** behavior: This permanent deformation behavior occurs when the tensile (or compressive) uniaxial stress reaches σ_y .
- **Toughness**: The energy needed to break a unit volume of material.
- **Ductility**: The plastic strain at failure.

Viscoelastic Behavior of Polymers

Perfectly elastic (Hookean)

$$\sigma = \text{constant} \times \varepsilon$$

(Energy stored, it can be recovered, e.g. metals.)

(Some thermosets like epoxies exhibit close to linear elastic behavior.)

Perfectly viscous (Newtonian)

$$\tau = \text{constant} \times \dot{\gamma}$$

(Energy completely dissipated, it can not be recovered, e.g. water.)

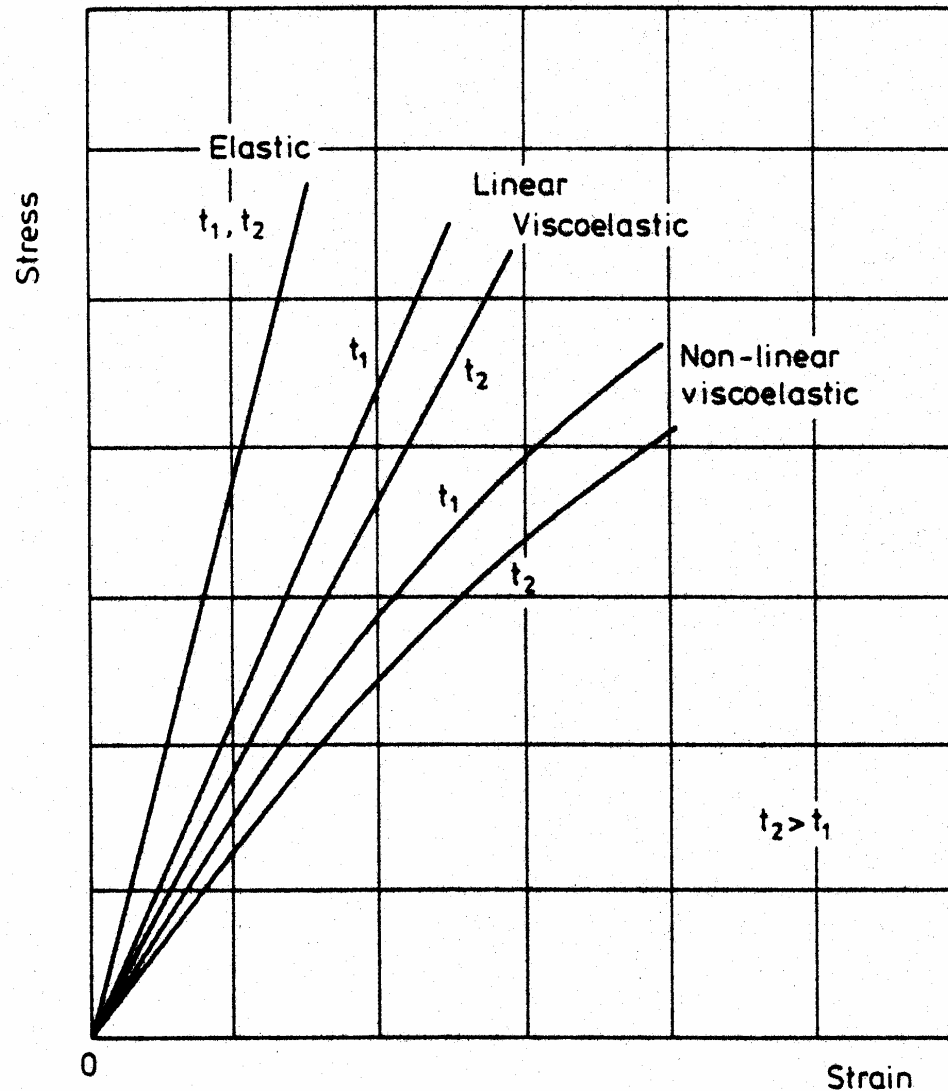
Viscoelastic

Non-linear viscoelasticity: $\sigma = f(\varepsilon, t)$

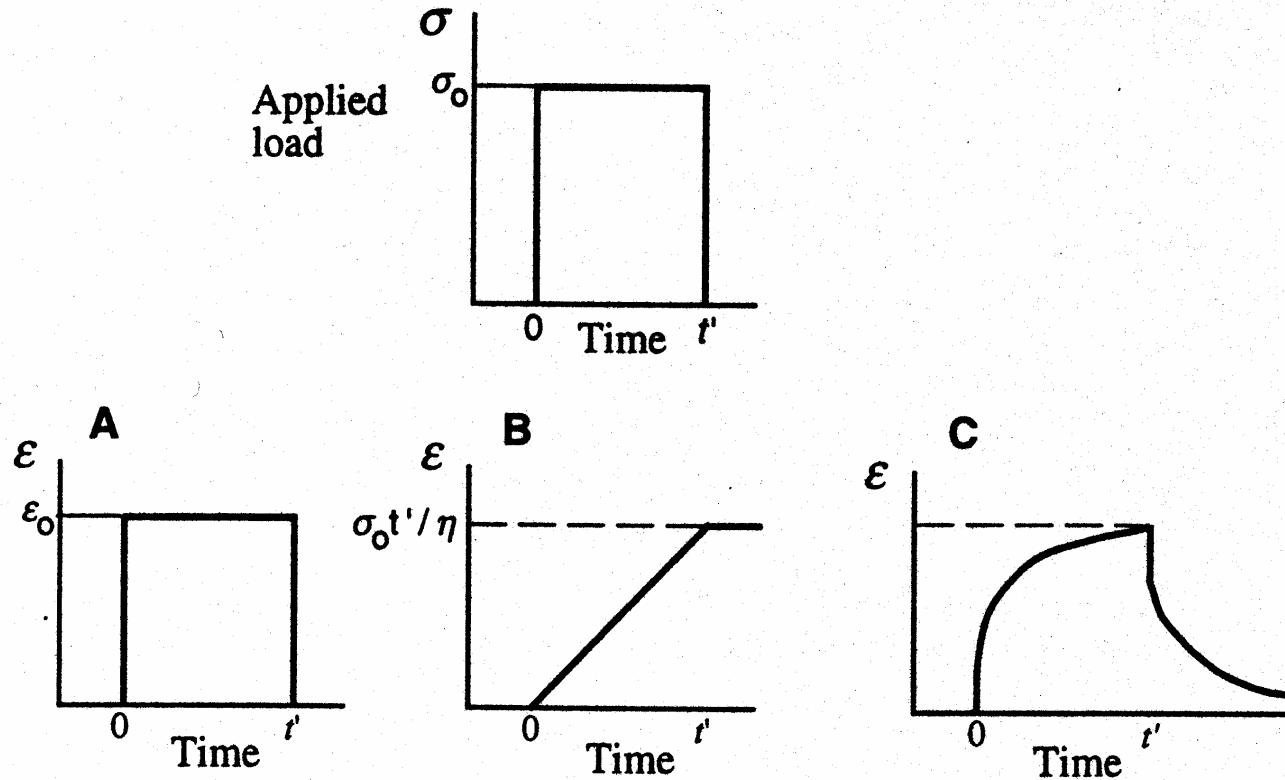
Linear viscoelasticity: $\sigma = \varepsilon \cdot f(t)$

(For a fixed elapsed time, the stress is directly proportional to the strain, e.g. most polymers.)

Viscoelastic Behavior of Polymers (Cont.)



Viscoelastic Behavior of Polymers (Cont.)



A, elastic; **B**, viscous; and **C**, viscoelastic

Viscoelastic Behavior of Polymers (Cont.)

The most characteristic features of viscoelastic materials are that they exhibit:

Creep: a time dependent strain response to a constant stress

and

Relaxation: a time dependent stress response to a constant strain

and

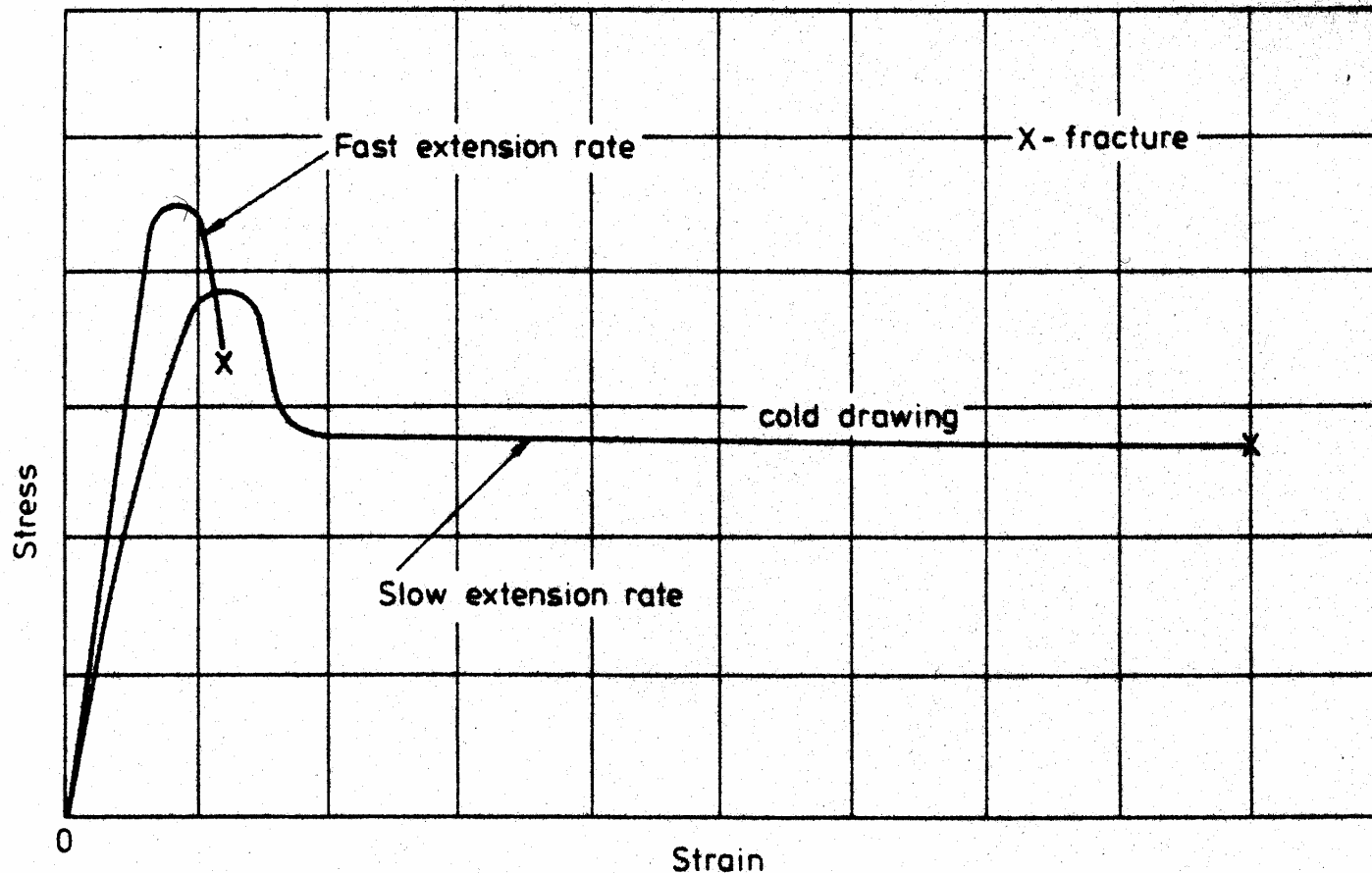
when the applied stress is removed the materials have the ability to recover slowly over a period of time.

These effects can also be observed in metals but the difference is that in plastics they occur at room temperature whereas in metals they only occur at very high temperatures

Short-Term Testing of Plastics

Results of a single short-term test should only be used as a means of quality control
– not as design data

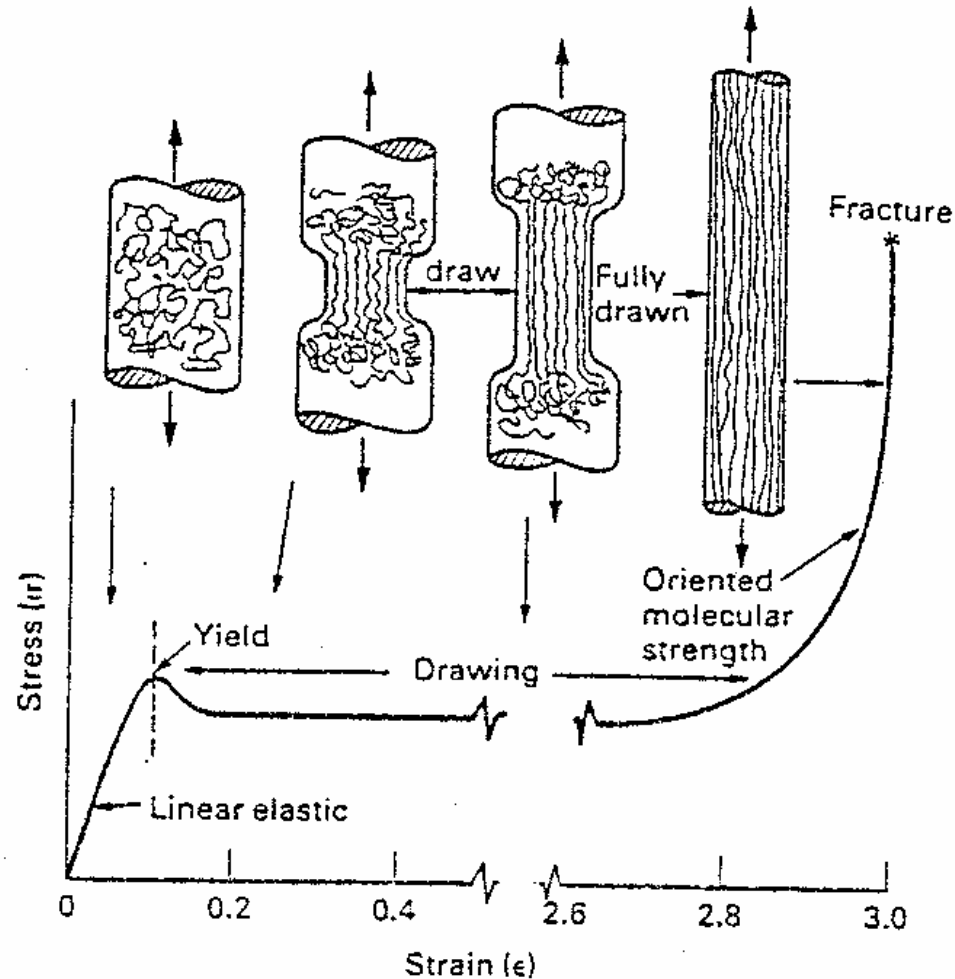
Typical tensile behavior of unplasticized PVC



Short-Term Testing of Plastics (Cont.)

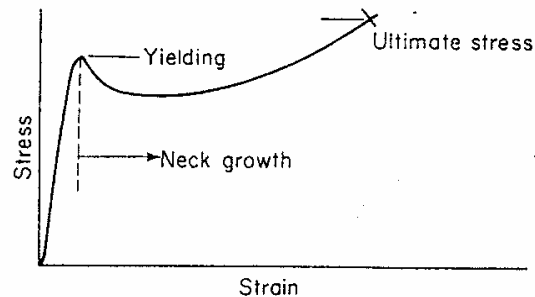
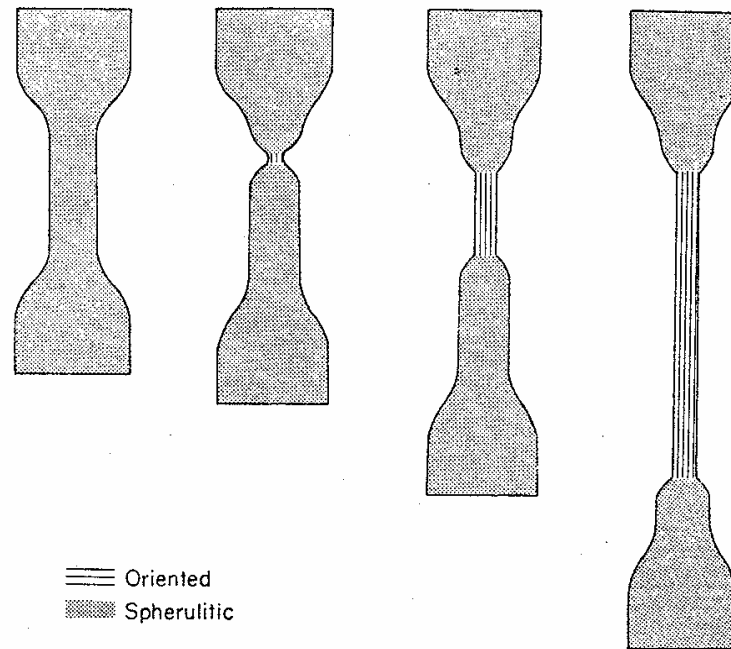
Cold drawing of an amorphous polymer

At low extension rates the molecular chains in the plastic have time to align themselves under the influence of the applied stress



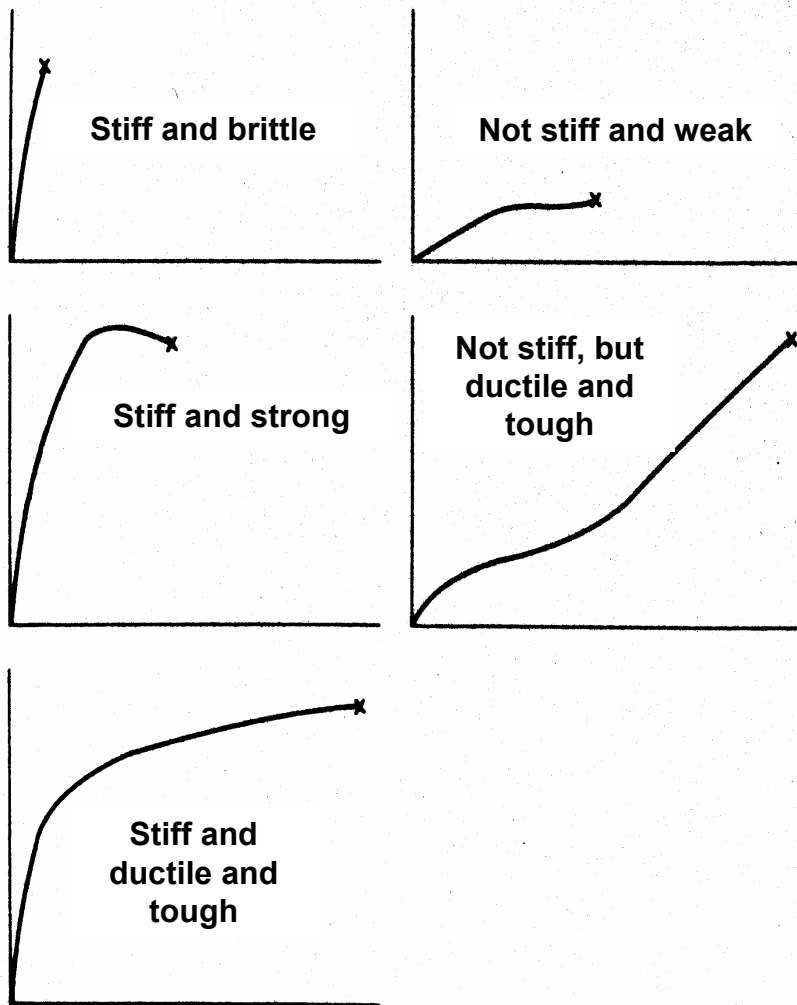
Short-Term Testing of Plastics (Cont.)

Cold drawing (Cont.) - Successive stages in the drawing (elongation) of a spherulitic (semi-crystalline) polymer



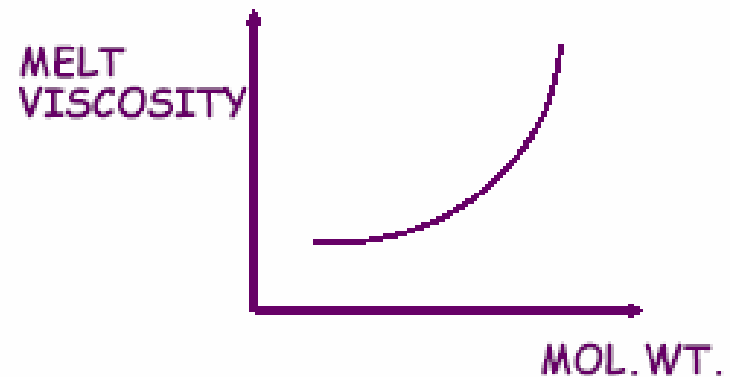
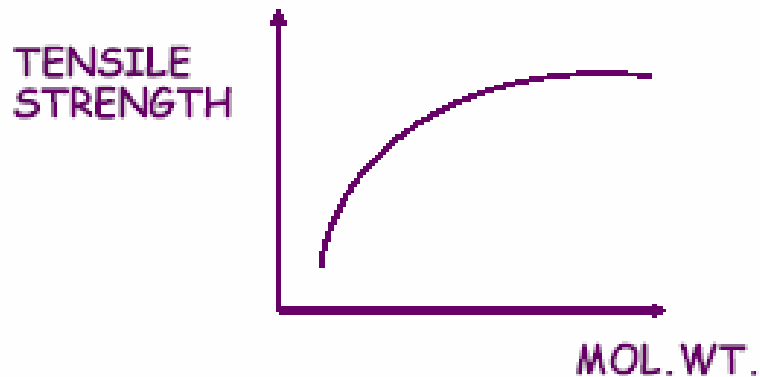
Short-Term Testing of Plastics (Cont.)

Types of stress-strain curves



Effect of Molecular Weight of Polymers on Their Strength

There is no direct effect but for many polymers it has been observed that tensile strength increases with M_w .



Molecular Weight of Polymers

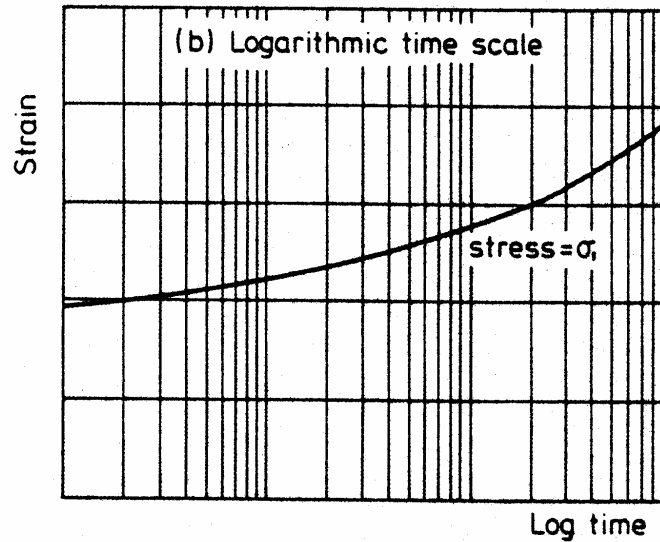
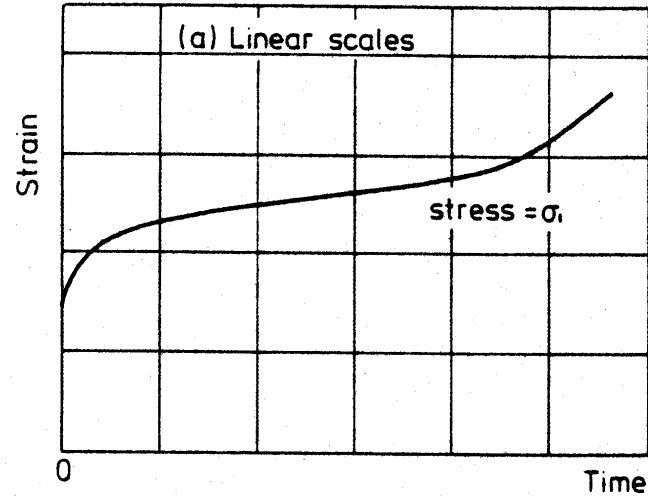
| | | |
|---|-------|--------|
| CH_4 | ----- | 16 |
| $\text{CH}_3 - \text{CH}_3$ | ----- | 30 |
| $\text{CH}_3 - \text{CH}_2 - \text{CH}_3$ | ----- | 44 |
| $\text{CH}_3 - \text{CH}_2 - \text{CH}_2 - \text{CH}_3$ | ----- | 58 |
| Gases | | |
| $\text{CH}_3 - (\text{CH}_2)_6 - \text{CH}_3$ | ----- | 114 |
| Liquids | | |
| $\text{CH}_3 - (\text{CH}_2)_{30} - \text{CH}_3$ | ----- | 450 |
| "Semi-solid" | | |
| $\text{CH}_3 - (\text{CH}_2)_{30000} - \text{CH}_3$ | ----- | 420030 |
| Solids | | |

Increasing
Molecular Weight

States at room temperature.

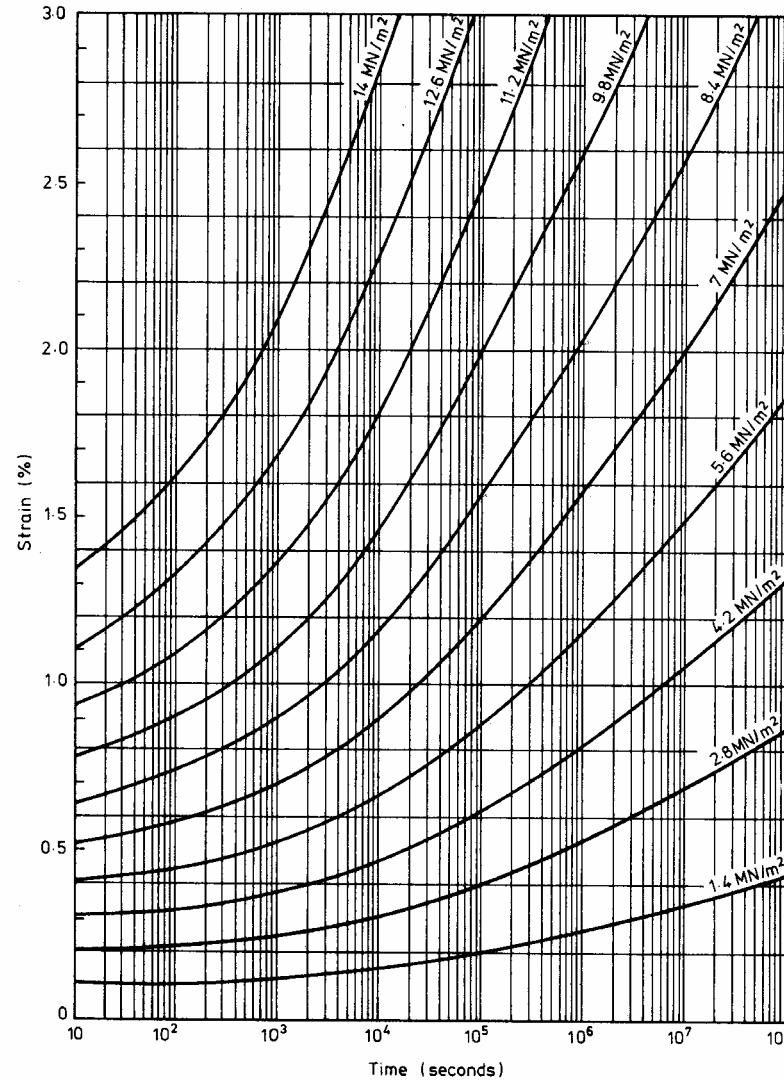
Long-Term Testing of Plastics

Typical creep curves



Long-Term Testing of Plastics (Cont.)

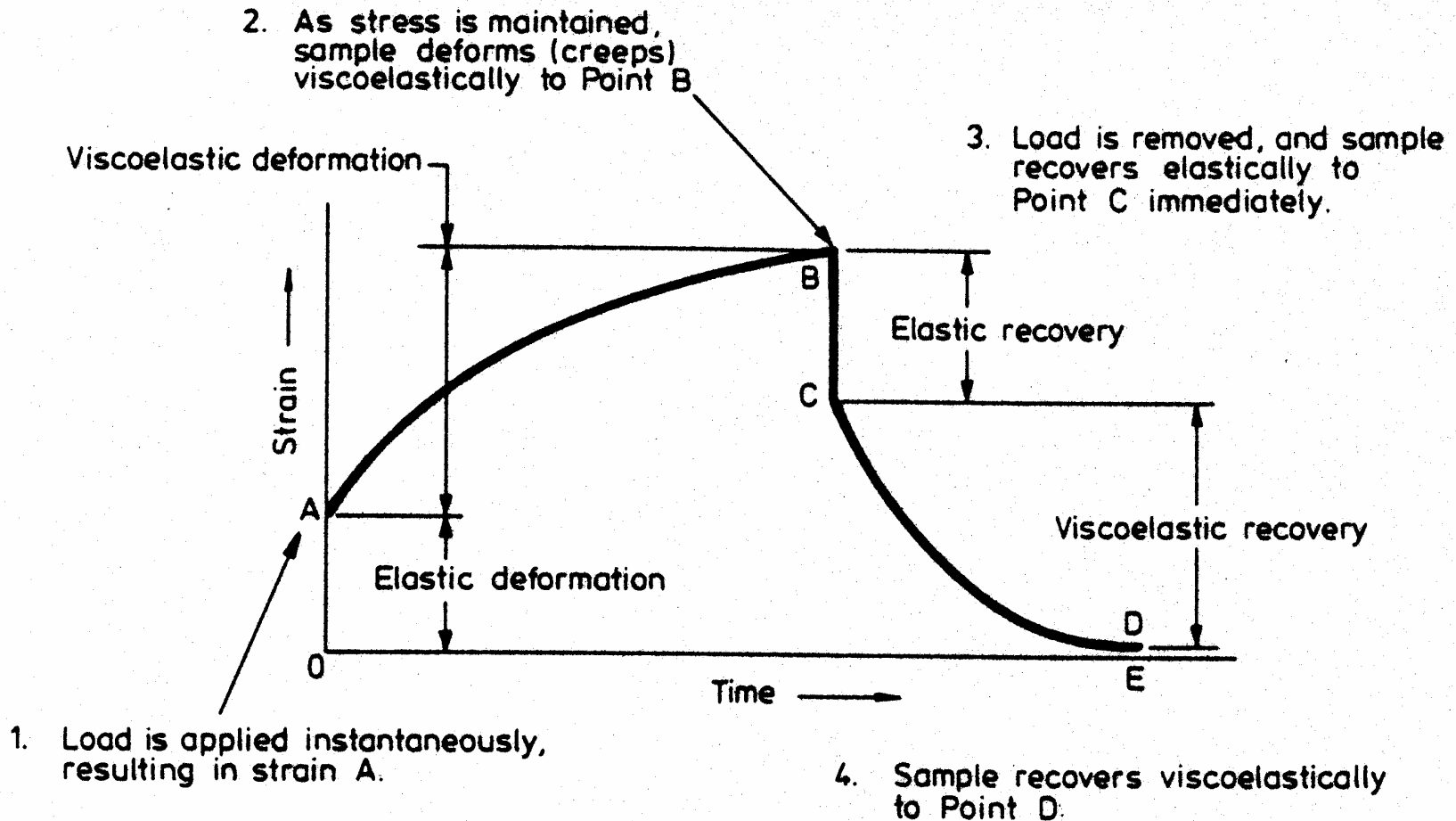
Creep curves for polypropylene at 20°C (density 909 kg/m³)



[Plastics Engineering, 2nd Ed., R. J. Crawford, Pergamon Press, Oxford, 1987]

Long-Term Testing of Plastics (Cont.)

Typical creep and recovery behavior of a plastic



References

1. Rodriguez, F., Principles of Polymer Systems, 4th Ed., Taylor & Francis, Washington, 1996.
2. R. J. Crawford, Plastics Engineering, 2nd Ed., Pergamon Press, Oxford, 1987.
3. Polymer Science and Technology, Joel R. Fried, Prentice Hall, Englewood Cliffs, 1995.
4. Web site of Prof. Duane D. Johnson at University of Illinois at Urbana-Champaign
5. Callister, W. D., Jr., Materials Science and Engineering – An Introduction, 4thEd., John Wiley & Sons, New York, 1997.