## **DEPARTMENT OF CIVIL ENGINEERING - KFUPM**

**Numerical and Statistical Methods in Civil Engineering** 

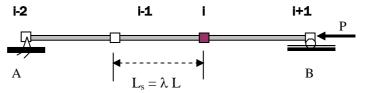
CE 318-1, '11 Assignment No. 05

**Subjects:** Finite Differences Solution of Ordinary and Partial Differential Equations (ODE & PDE)

Date: Date: Dec. 06, '11

- 1. Study some basics on theory and analytical solution of column instability (bucking) as presented in the textbook pages 762-765. Then, for a uniform column AB with one end pinned and with the other end having a roller-support (as shown in Fig. P-1), determine values of the critical axial load  $P_{cr}$  for a column with L = 3 m, E = 10 GPa, and  $I = 1.3 \times 10^{-5}$  m<sup>4</sup>. For this:
  - a. determine the analytical (exact) value of P<sub>cr</sub>;
  - b. determine an approximate (numerical) value of  $P_{cr}$  using the method of finite differences with nodal spacing ration  $\lambda_1 = 1/3$  and  $\lambda_2 = 1/4$  such that  $L_s = \lambda L$ ; and
  - c. compare the results with different  $\lambda$  and with the analytical solution.
- 2. Use the method of finite difference to formulate the system of linear equations to solve problem 27.23 of the textbook page 780. Then i) determine the nodal values  $u(x_i) = u_i$ , and ii) plot  $u_i$  versus  $x_i$ .

Fig. P-1: mesh discretization of the column.



B.C.'s: transverse displacements at A and B are both zero.

3. The square cross section shown below) is subjected to a torque T. The stress function  $\phi$  can be used to determine the stress at points on the cross section. The governing differential partial differential equation (type is Poisson's Equation) is given as

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial y^2} + 2 = 0$$

B.C.'s:

 $\phi = 0$  at all boundary points of the cross section. Note: Assume the dimension of the cross section is 8 cm.

Complete the numbering scheme on the cross section, determine the values of  $\phi$  at all *nine interior* points (numbered as: 1,2,3,4, 5 "the center point") on the cross section.

5

8 cm