

7-6. If the beam is subjected to a shear of  $V = 15$  kN, determine the web's shear stress at  $A$  and  $B$ . Indicate the shear-stress components on a volume element located at these points. Show that the neutral axis is located at  $\bar{y} = 0.1747$  m from the bottom and  $I_{NA} = 0.2182(10^{-3})$  m<sup>4</sup>.

$$\bar{y} = \frac{(0.015)(0.125)(0.03) + (0.155)(0.025)(0.25) + (0.295)(0.2)(0.03)}{0.125(0.03) + (0.025)(0.25) + (0.2)(0.03)} = 0.1747 \text{ m}$$

$$I = \frac{1}{12}(0.125)(0.03^3) + 0.125(0.03)(0.1747 - 0.015)^2$$

$$+ \frac{1}{12}(0.025)(0.25^3) + 0.25(0.025)(0.1747 - 0.155)^2$$

$$+ \frac{1}{12}(0.2)(0.03^3) + 0.2(0.03)(0.295 - 0.1747)^2 = 0.218182(10^{-3}) \text{ m}^4$$

$$Q_A = \bar{y}A'_A = (0.310 - 0.015 - 0.1747)(0.2)(0.03) = 0.7219(10^{-3}) \text{ m}^3$$

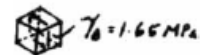
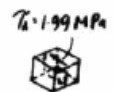
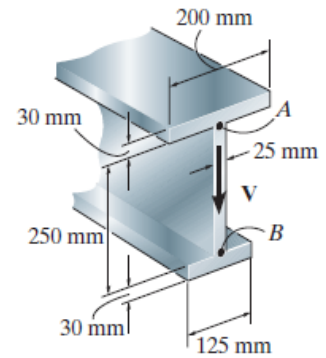
$$Q_B = \bar{y}A'_B = (0.1747 - 0.015)(0.125)(0.03) = 0.59883(10^{-3}) \text{ m}^3$$

$$\tau_A = \frac{VQ_A}{It} = \frac{15(10^3)(0.7219)(10^{-3})}{0.218182(10^{-3})(0.025)} = 1.99 \text{ MPa}$$

Ans.

$$\tau_B = \frac{VQ_B}{It} = \frac{15(10^3)(0.59883)(10^{-3})}{0.218182(10^{-3})(0.025)} = 1.65 \text{ MPa}$$

Ans.



7-14. Determine the maximum shear force  $V$  that the strut can support if the allowable shear stress for the material is  $\tau_{\text{allow}} = 40 \text{ MPa}$ .

*Section Properties:*

$$I_{NA} = \frac{1}{12} (0.12)(0.084^3) - \frac{1}{12} (0.04)(0.06^3)$$

$$= 5.20704(10^{-6}) \text{ m}^4$$

$$Q_{\text{max}} = \Sigma \bar{y}' A'$$

$$= 0.015(0.08)(0.03) + 0.036(0.012)(0.12)$$

$$= 87.84(10^{-6}) \text{ m}^3$$

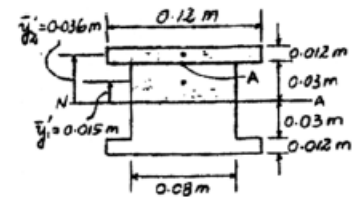
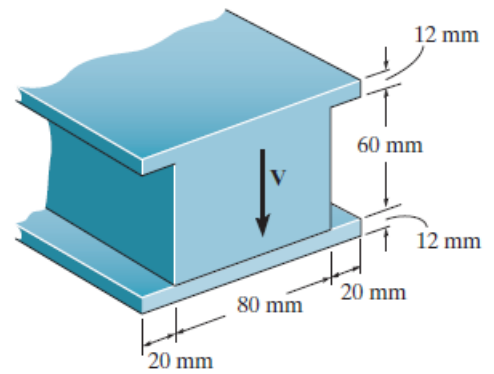
*Allowable shear stress:* Maximum shear stress occurs at the point where the neutral axis passes through the section.

Applying the shear formula

$$\tau_{\text{max}} = \tau_{\text{allow}} = \frac{VQ_{\text{max}}}{It}$$

$$40(10^6) = \frac{V(87.84)(10^{-6})}{5.20704(10^{-6})(0.08)}$$

$$V = 189\,692 \text{ N} = 190 \text{ kN}$$



Ans.

\*7-24. Determine the maximum shear stress in the T-beam at the critical section where the internal shear force is maximum.

The FBD of the beam is shown in Fig. *a*,

The shear diagram is shown in Fig. *b*. As indicated,  $V_{\max} = 27.5$  kN

The neutral axis passes through centroid *c* of the cross-section, Fig. *c*.

$$\bar{y} = \frac{\sum \tilde{y} A}{\sum A} = \frac{0.075(0.15)(0.03) + 0.165(0.03)(0.15)}{0.15(0.03) + 0.03(0.15)}$$

$$= 0.12 \text{ m}$$

$$I = \frac{1}{12}(0.03)(0.15^3) + 0.03(0.15)(0.12 - 0.075)^2$$

$$+ \frac{1}{12}(0.15)(0.03^3) + 0.15(0.03)(0.165 - 0.12)^2$$

$$= 27.0(10^{-6}) \text{ m}^4$$

From Fig. *d*,

$$Q_{\max} = \bar{y}' A' = 0.06(0.12)(0.03)$$

$$= 0.216(10^{-3}) \text{ m}^3$$

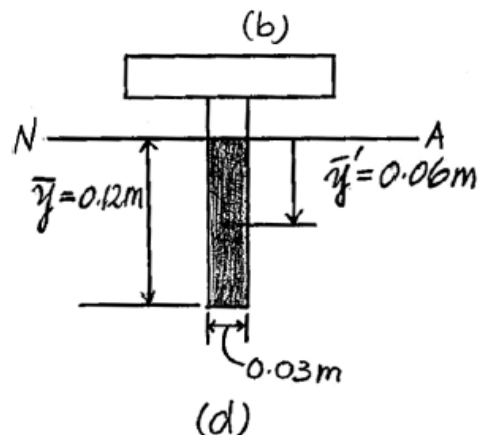
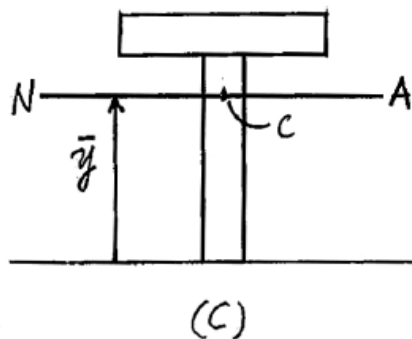
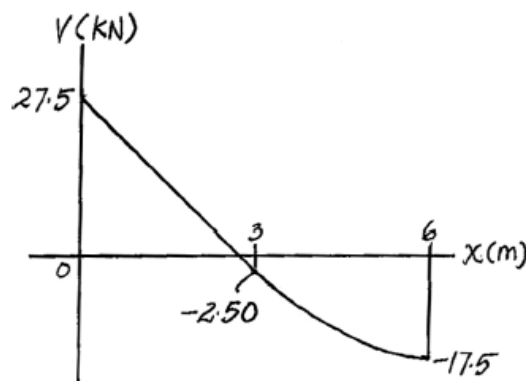
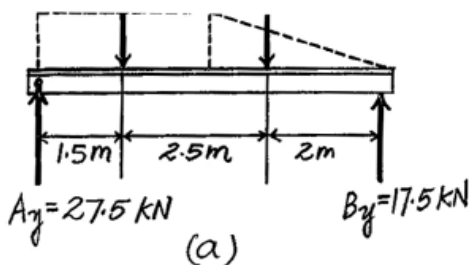
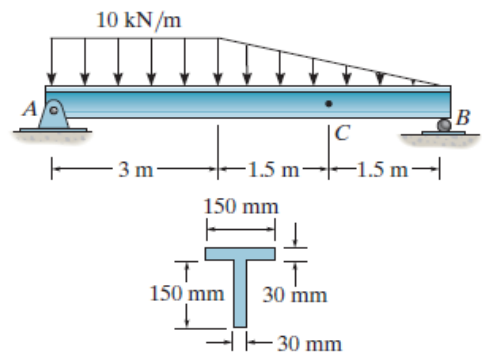
The maximum shear stress occurs at points on the neutral axis since  $Q$  is maximum and thickness  $t = 0.03$  m is the smallest.

$$\tau_{\max} = \frac{V_{\max} Q_{\max}}{I t} = \frac{27.5(10^3)[0.216(10^{-3})]}{27.0(10^{-6})(0.03)}$$

$$= 7.333(10^6) \text{ Pa}$$

$$= 7.33 \text{ MPa}$$

Ans.



7-42. The T-beam is nailed together as shown. If the nails can each support a shear force of 4.5 kN, determine the maximum shear force  $V$  that the beam can support and the corresponding maximum nail spacing  $s$  to the nearest multiples of 5 mm. The allowable shear stress for the wood is  $\tau_{\text{allow}} = 3$  MPa.

$$\bar{y} = \frac{\sum \bar{y}A}{\sum A} = \frac{325 * 50 * 300 + 150 * 300 * 50}{50 * 300 + 50 * 300}$$

$$\bar{y} = 237.5 \text{ mm}$$

$$I = \frac{1}{12} * 50 * 300^3 + 50 * 300 * (150 - 237.5)^2 + \frac{1}{12} * 300 * 50^3 + 50 * 300 * (325 - 237.5)^2$$

$$I = 345312500 \text{ mm}^4$$

$$Q_{\text{max}} = \bar{y}'_1 A'_1 = 118.75 * 237.5 * 50$$

$$Q_{\text{max}} = 1410156.25 \text{ mm}^3$$

$$Q_A = \bar{y}'_2 A'_2 = 87.5 * 50 * 300$$

$$Q_A = 1312500 \text{ mm}^3$$

The maximum shear stress occurs at the points on the neutral axis where  $Q$  is maximum and  $t = 50$  mm

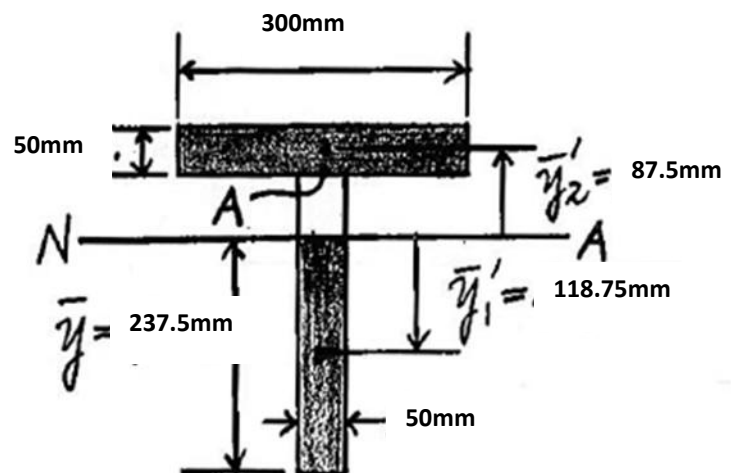
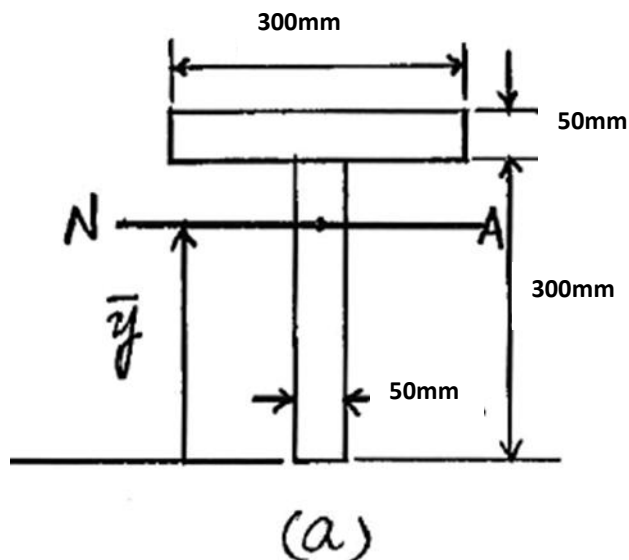
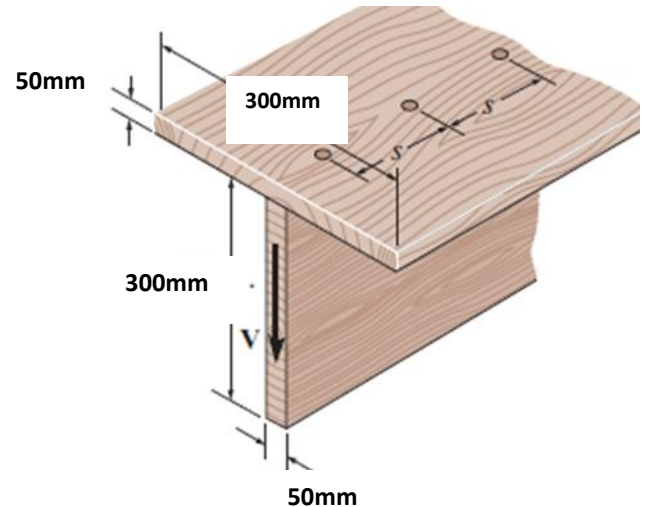
$$\tau_{\text{allow}} = \frac{VQ_{\text{max}}}{It}; 3 = \frac{V * 1410156.25}{345312500 * 50};$$

$$V = 36731 \text{ N} \quad \text{Ans.}$$

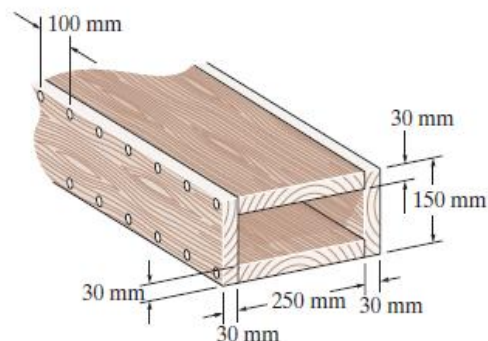
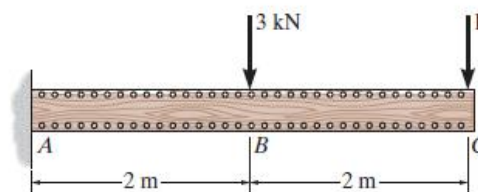
$$q_{\text{allow}} = \frac{F}{s} = 4.5 * \frac{1000}{s} \text{ N/mm}$$

$$q_{\text{allow}} = \frac{VQ_A}{I}; 4.5 * \frac{1000}{s} = \frac{36731 * 1312500}{345312500}$$

$$s = 32.23 \text{ mm} \quad \text{Ans.}$$



•7-45. The beam is constructed from four boards which are nailed together. If the nails are on both sides of the beam and each can resist a shear of 3 kN, determine the maximum load  $P$  that can be applied to the end of the beam.



**Support Reactions:** As shown on FBD.

**Internal Shear Force:** As shown on shear diagram,  $V_{AB} = (P + 3)$  kN.

**Section Properties:**

$$I_{NA} = \frac{1}{12} (0.31)(0.15^3) - \frac{1}{12} (0.25)(0.09^3)$$

$$= 72.0(10^{-6}) \text{ m}^4$$

$$Q = \bar{y}' A' = 0.06(0.25)(0.03) = 0.450(10^{-3}) \text{ m}^3$$

**Shear Flow:** There are two rows of nails. Hence the allowable shear flow is

$$q = \frac{3(2)}{0.1} = 60.0 \text{ kN/m.}$$

$$q = \frac{VQ}{I}$$

$$60.0(10^3) = \frac{(P + 3)(10^3)0.450(10^{-3})}{72.0(10^{-6})}$$

$$P = 6.60 \text{ kN}$$

Ans.

