

Shear Force Diagram (SFD)

Bending Moment Diagram (BMD)

* You have already studied one method for drawing the SFD & BMD in Statics. The FBD's and equations were used. Review!!

* Now, a new method called Summation (or integration or area) method will be developed. No need for FBD's and equations. It is a very quick and convenient method.

SFD & BMD by Summation Method:

In the FBD, the distributed load is replaced by an equivalent concentrated load (Resultant):

$$R = [w(x + \lambda \Delta x)] \Delta x$$

$$0 \leq \lambda \leq 1$$

$$\uparrow \sum F_y = 0 \Rightarrow$$

$$V(x) + [w(x + \lambda \Delta x)] \Delta x - V(x + \Delta x) = 0$$

Divide by Δx , rearrange, and let $\Delta x \rightarrow 0$

$$\lim_{\Delta x \rightarrow 0} \frac{V(x + \Delta x) - V(x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} w(x + \lambda \Delta x)$$

$$\Rightarrow \boxed{\frac{dV}{dx} = w(x)}$$

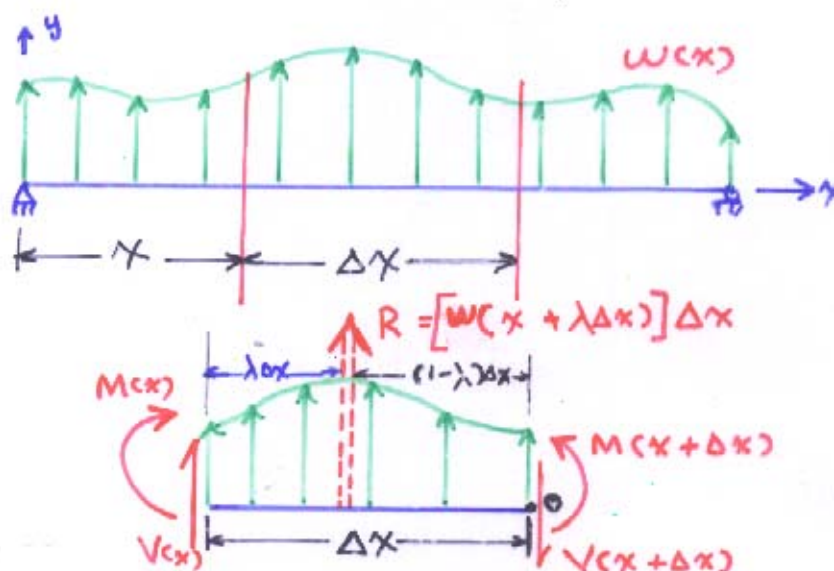
$$\uparrow \sum M_o = 0 \Rightarrow$$

$$-M(x) + M(x + \Delta x) - V(x) \Delta x - [w(x + \lambda \Delta x)] (\Delta x)(1 - \lambda) \Delta x = 0$$

Divide by Δx , rearrange, and let $\Delta x \rightarrow 0$

$$\lim_{\Delta x \rightarrow 0} \frac{M(x + \Delta x) - M(x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} V(x) + \lim_{\Delta x \rightarrow 0} [w(x + \lambda \Delta x)] (1 - \lambda) \Delta x$$

$$\Rightarrow \boxed{\frac{dM}{dx} = V(x)}$$



FBD

