

King Fahd University of Petroleum & Minerals
 CIVIL ENGINEERING DEPARTMENT
 CE 201 STATICS (Sections 1 & 2)
 Second Semester 1432 / 2011 (102)

Name: Key
 ID #: _____

Quiz # 4

Score 10

Determine the magnitude of the moment that the force F exerts about the y axis of the shaft. Solve the problem using a Cartesian vector approach and using a scalar approach.

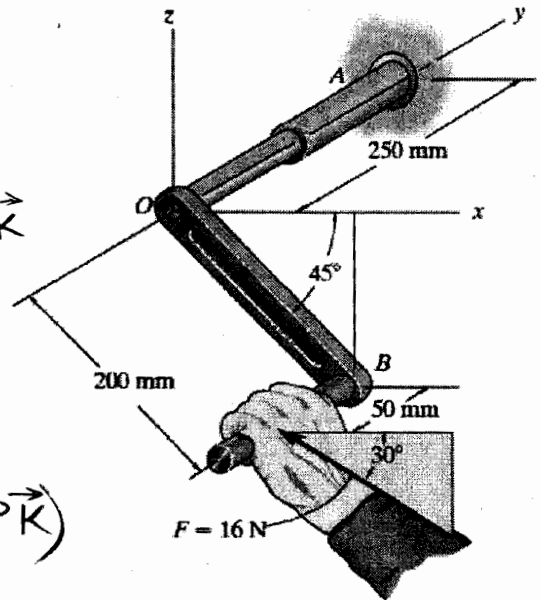
Cartesian Vector Approach

Position vector,

$$\begin{aligned} \vec{r}_{OB} &= 0.2 \cos 45^\circ \vec{i} + 0 \vec{j} - 0.2 \sin 45^\circ \vec{k} \\ &= 0.1414 \vec{i} - 0.1414 \vec{k} \end{aligned}$$

Force vector,

$$\begin{aligned} \vec{F} &= 16(-\cos 30^\circ \vec{i} + 0 \vec{j} + \sin 30^\circ \vec{k}) \\ &= -13.8560 \vec{i} + 8 \vec{k} \end{aligned}$$



Unit vector along y -axis, $\vec{u}_y = 0 \vec{i} + \vec{j} + 0 \vec{k} = \vec{j}$

Moment about y -axis, $M_y = \vec{u}_y \cdot (\vec{r}_{OB} \times \vec{F})$

$$M_y = \begin{vmatrix} 0 & 1 & 0 \\ 0.1414 & 0 & -0.1414 \\ -13.8560 & 0 & 8 \end{vmatrix} = -1(0.1414 \times 8 - 13.8560 \times 0.1414)$$

$$\Rightarrow M_y = 0.828 \text{ N}\cdot\text{m}$$

Scalar Approach:

$$M_y = \pm F_x \times (z) \pm F_z \times (x)$$

$$\begin{aligned} M_y &= +16 \cos 30^\circ \times (0.2 \sin 45^\circ) - 16 \sin 30^\circ \times (0.2 \cos 45^\circ) \\ &= 1.9595 - 1.1314 \end{aligned}$$

$$\Rightarrow M_y = 0.828 \text{ Nm}, \text{ as before}$$

Note: Take care of the signs by inspection